컨텍스트 터널링

구분할 호출환경 배달하기: 고정관념에 도전하기

전민석



Aug.21.2025 @ SIGPL 여름학교

문제

• 아래 문장은 어떤 동화를 한 문장으로 요약한 것이다, 몇점짜리 요약일까?

문제

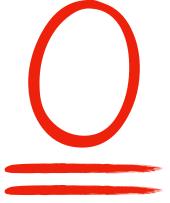
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"The End"

문제

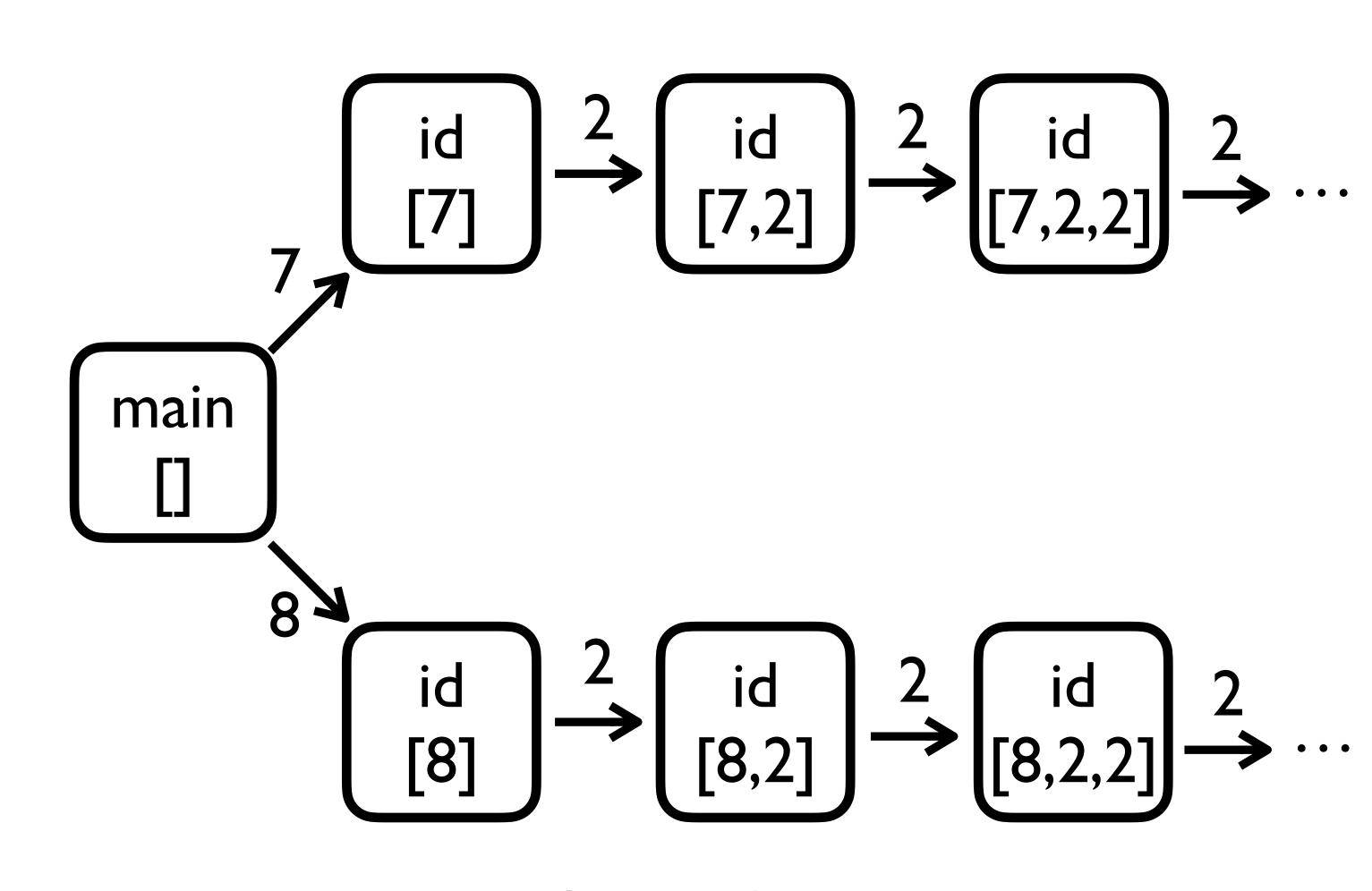
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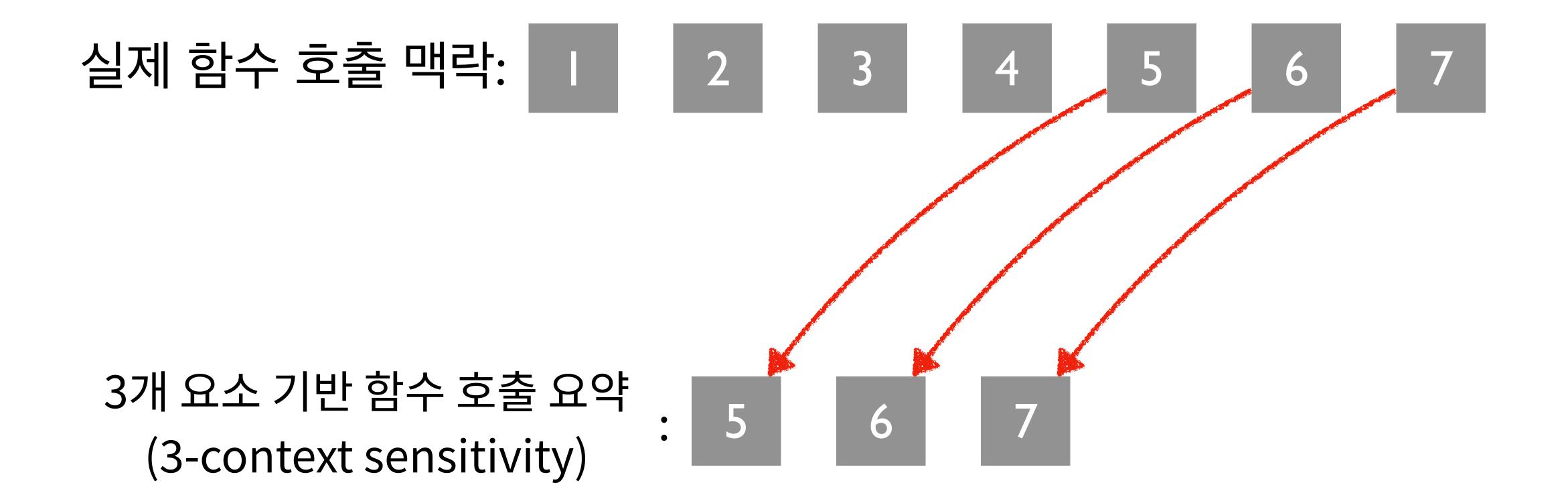


함수호출 요약의 필요성

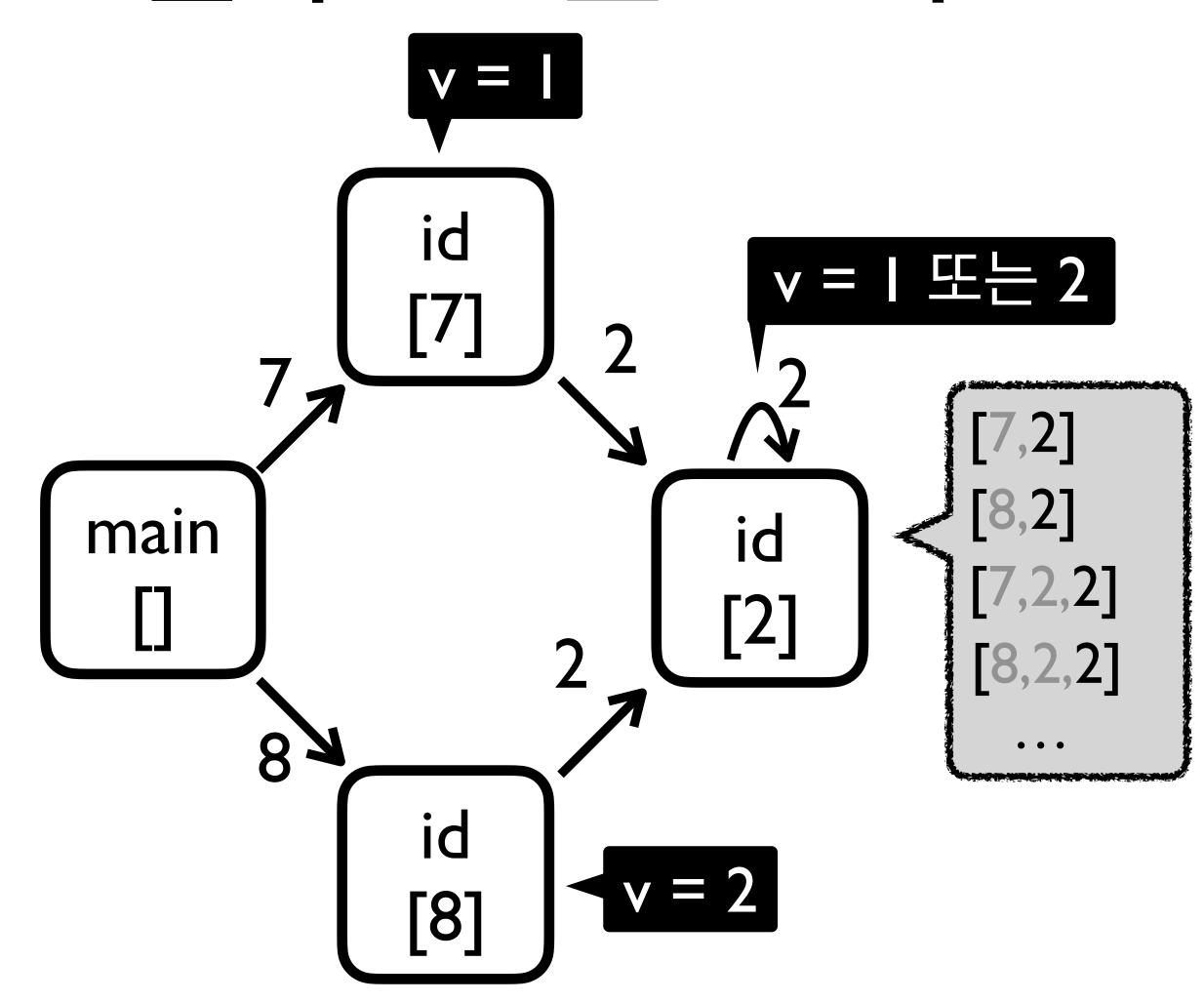
```
0: id(v, i){
   if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
   i = input();
   vI = id(I, i);//A
   v2 = id(2, i);//B
8:
    assert (vI != v2);//query
9:
   예제 프로그램
```



함수 호출 그래프

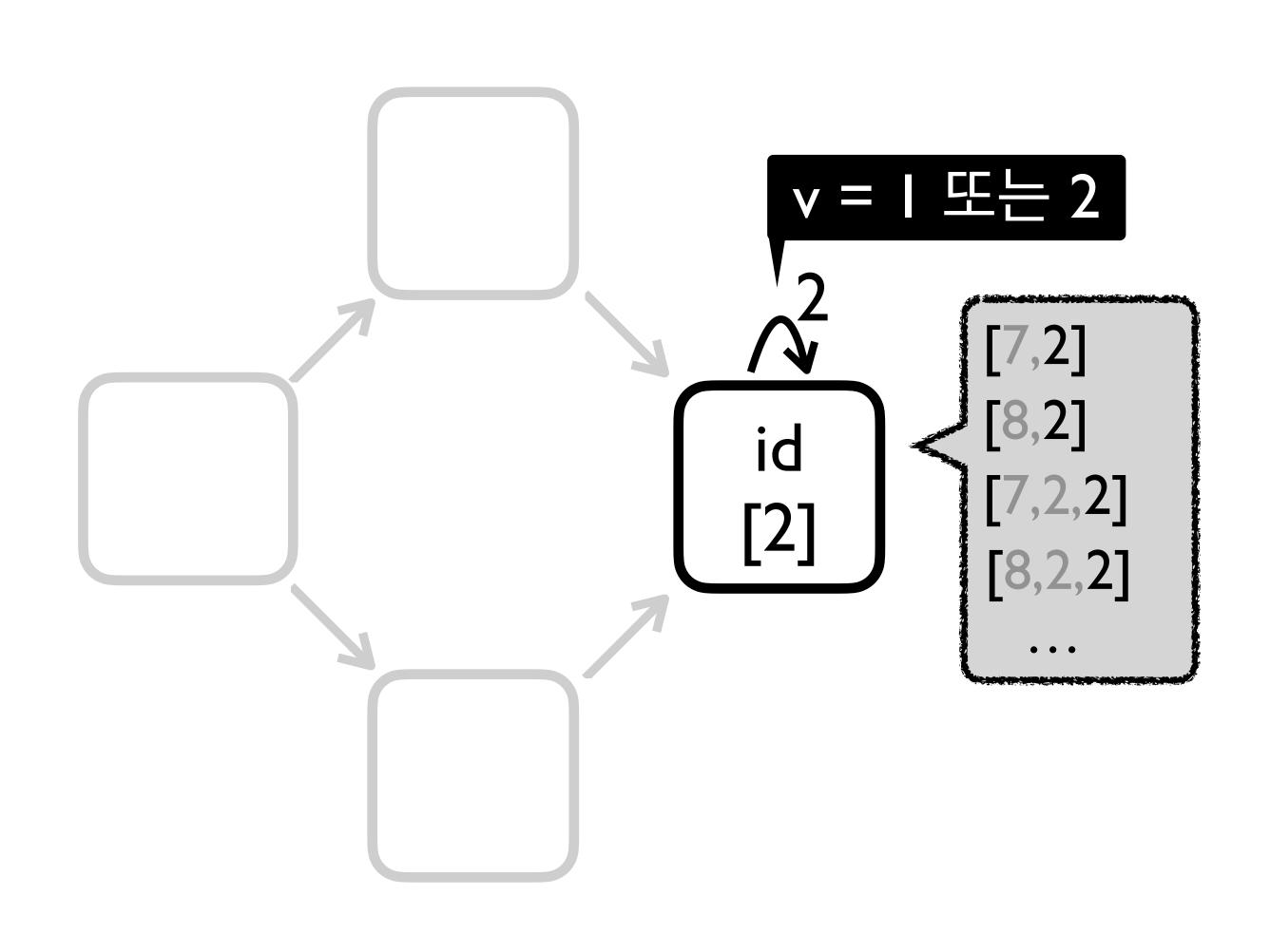


```
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   예제 프로그램
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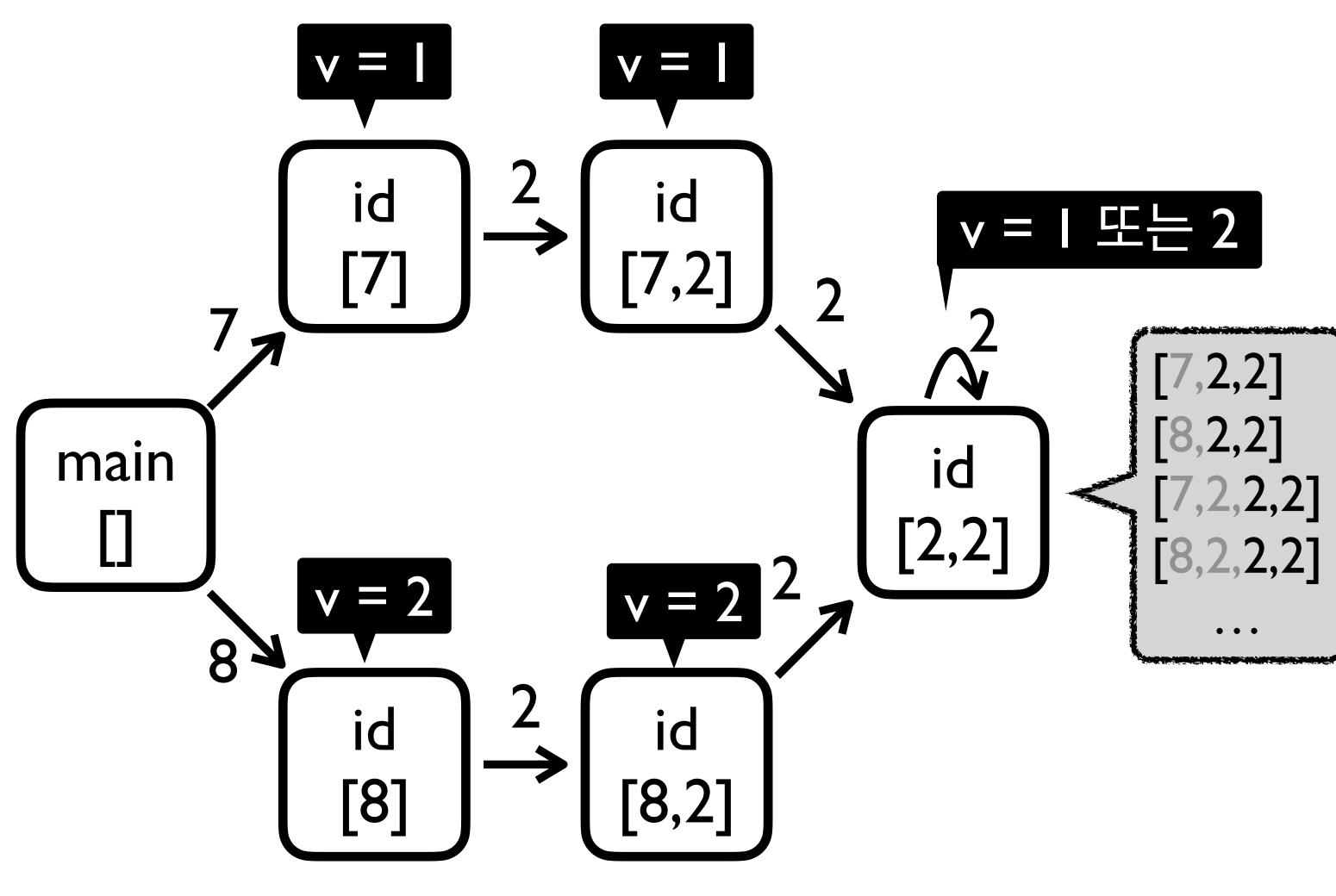


I개 요소 기반 함수 호출 요약

```
0: id(v, i){
1: if (i > 0)
    return id(v, i-1);}
    return_v;} v = [ 年2
    v2 = id(2, i);
8:
    assert (vI != v2);//query
9:
10: }
       1 또는 2
                1 또는 2
   예제 프로그램
```



```
0: id(v, i){
   if (i > 0){
     return id(v, i-1);}
    return v;}
4:
5: main(){
   i = input();
   vI = id(I, i);//A
    v2 = id(2, i);//B
8:
    assert (vI != v2);//query
9:
    예제 프로그램
```



2-개 요소 기반 함수 호출 요약

```
0: id(v, i){
    if (i > 0){
     return id(v, i-1);}
     return v;}
4:
5: main(){
    i = input();
    vI = id(I, i);//A
    v2 = id(2, i);//B
8:
     assert (vI != v2);//query
9:
    예제 프로그램
```

```
id
main
                      id
           id
          [8]
         3-개 요소 기반 함수 호출 요약
          10
```

고정관념: 마지막 k개 기반 요약

• 마지막 k개 기반 요약 방식이 널리 강의 되는 중

Call-Site Sensitivity



- The best-known flavor of context sensitivity, which uses callsites as contexts.
- A method is analyzed under the context that is a sequence of the last *k* call-sites

Partial Context-sensitivity

- The most common way: keep only the top-most k continuations (so-called k-CFA)
 - k = 0: ignore all contexts, i.e., context-insensitive
 - $k = \infty$: keep all contexts, i.e., fully context-sensitive



Partial Context-sensitivity



- The most common way: keep only the top-most k callstrings (called k-CFA)
- Approach: set an upper bound for length of contexts, denoted by k



- For call-site sensitivity, each context consists of the last k
 call sites of the call chains
- In practice, k is a small number (usually ≤3)
- Method contexts and heap contexts may use different k
 - e.g., k=2 for method contexts, k=1 for heap contexts

(검색 키워드: Context Sensitivity Static Analysis Lecture)

고정 관념: 마지막 k개 기반 요약

• 리뷰 코멘트

"A key part of the appeal of last k-based context abstraction is its simplicity and universal applicability."

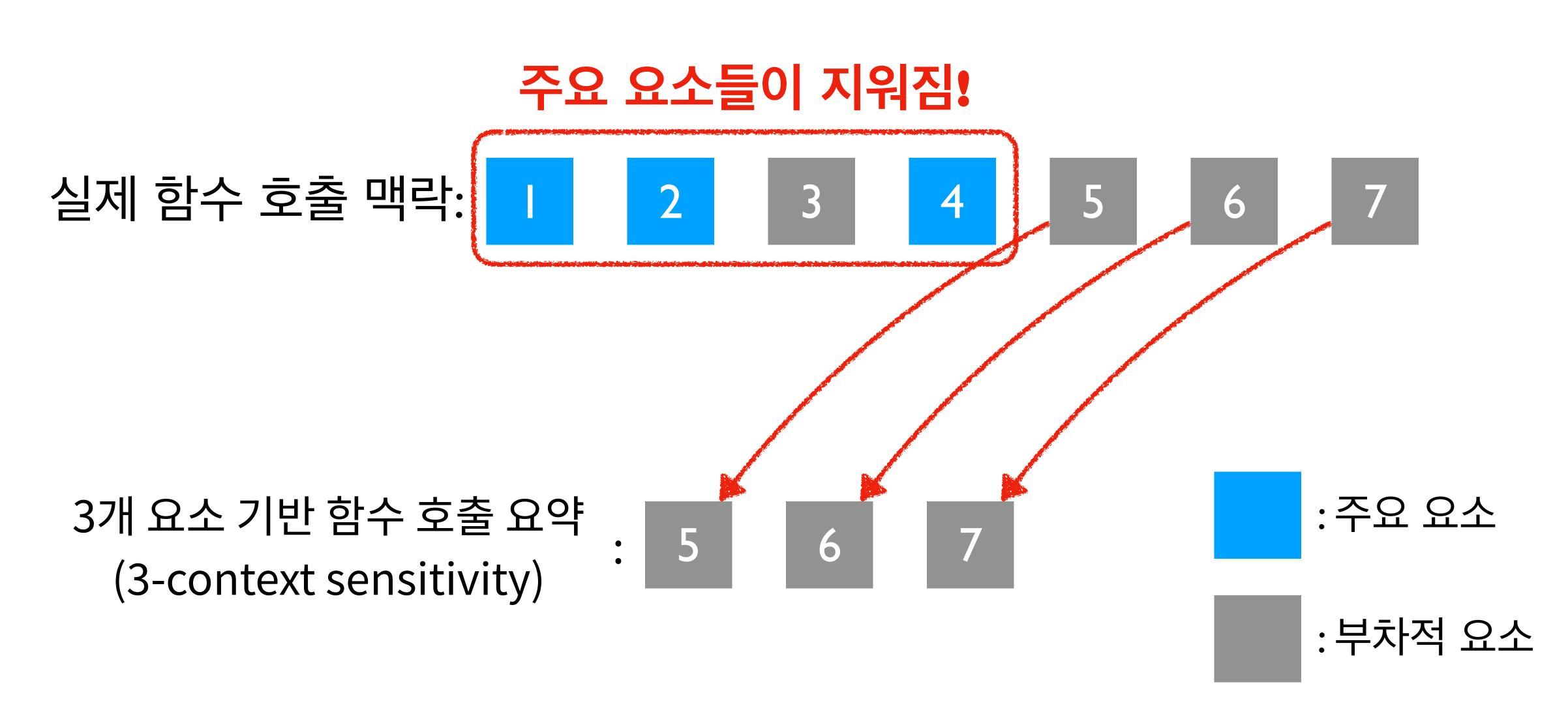
- A reviewer [expert]

- k = 0: ignore all contexts, i.e., context-insensitive
- k = ∞: keep all contexts, i.e., fully context-sensitive



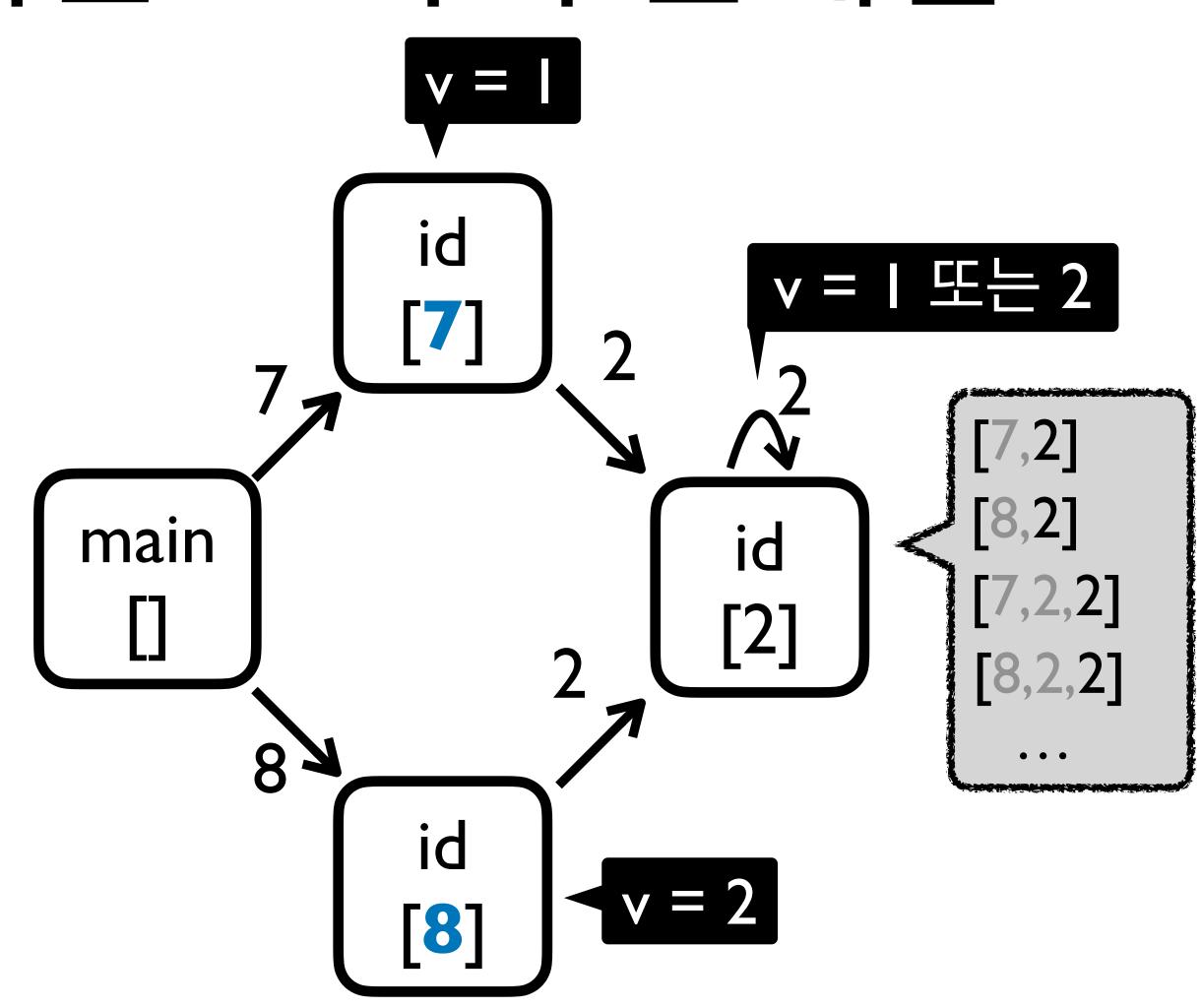
- In practice, k is a small number (usually ≤3)
- Method contexts and heap contexts may use different k
 - e.g., k=2 for method contexts, k=1 for heap contexts

마지막 K개 기반 요약의 문제점



마지막 K개 기반 요약의 문제점

```
0: id(v, i){
  if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
   i = input();
   vI = id(I, i);
   v2 = id(2, i);
8:
    assert (vI != v2);//query
9:
   예제 프로그램
```



I개 요소 기반 함수 호출 요약

발견하게된계기

Exercise

```
class S {
 Object id(Object a) { return a; }
 Object id2(Object a) { return id(); }
class C extends S {
 void fun1() {
   Object a1 = new A1();
   Object b1 = id2(a1);
  }}
class D extends S {
 void fun2() {
   Object a2 = new A2();
   Object b2 = id2(a2);
 }}
```

● What is the result of 1-call-site-sensitive analysis? < 부정확함

발견하게된계기

Exercise

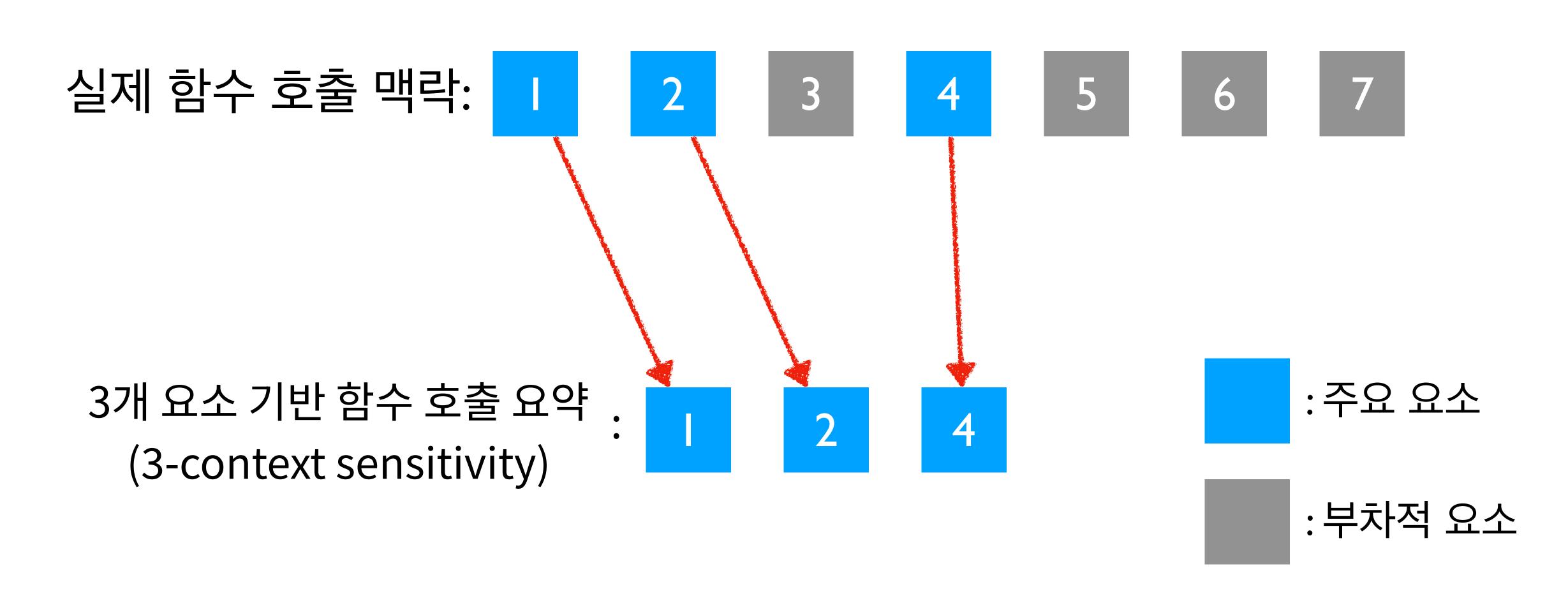
```
class S {
 Object id(Object a) { return a; }
 Object id2(Object a) { return id(); }
class C extends S {
 void fun1() {
   Object a1 = new A1();
   Object b1 = id2(a1);
  }}
class D extends S {
 void fun2() {
   Object a2 = new A2();
   Object b2 = id2(a2);
  }}
```

질문:

I-call-site sensitivity로 정확하게 분석할 순 없나?

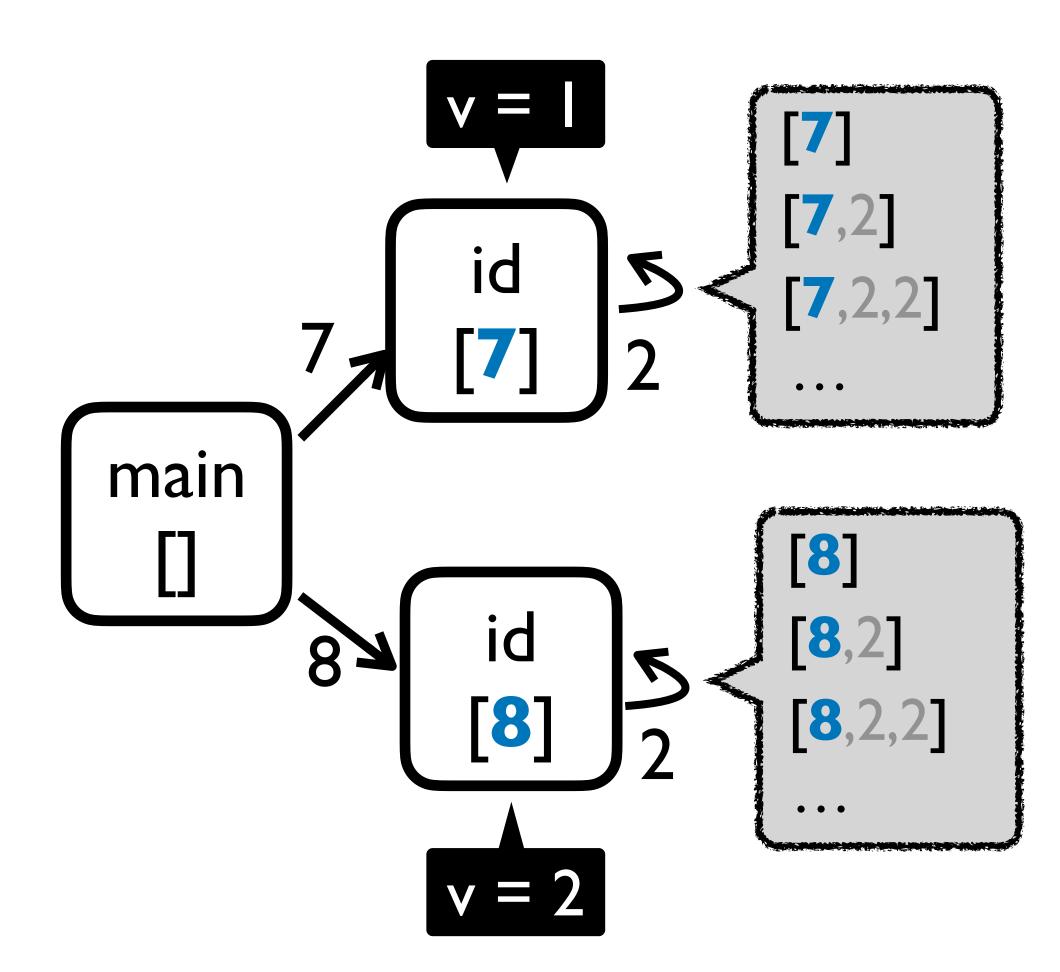
● What is the result of 1-call-site-sensitive analysis? ✔ 부정확함

호출 환경 배달하기: 주요 K개 기반 요약

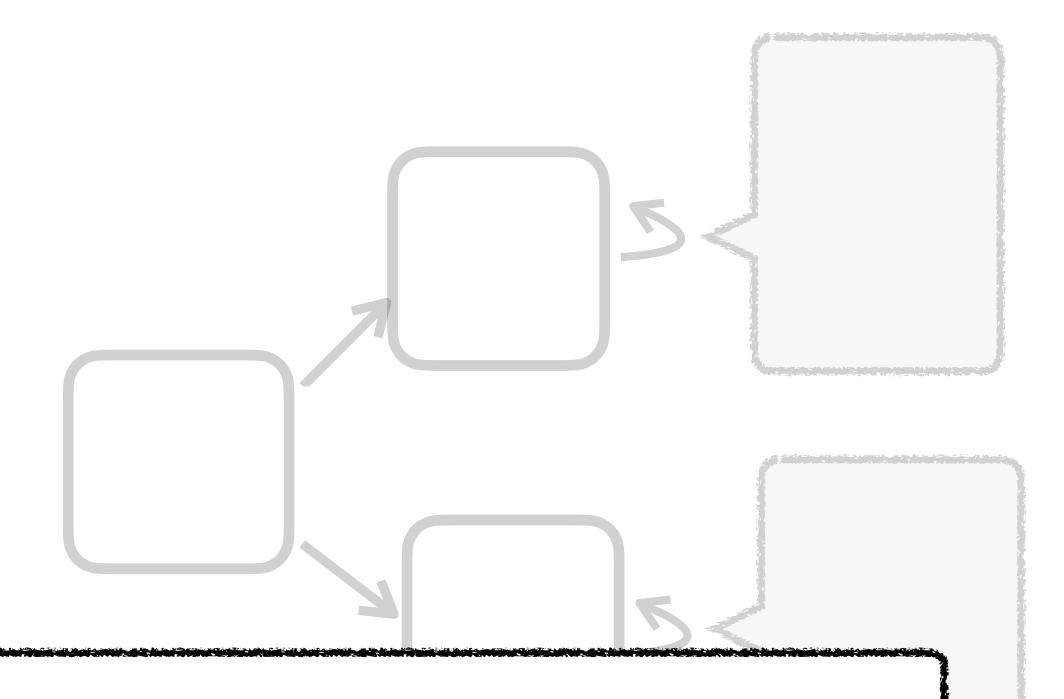


호출 환경 배달하기: 주요 K개 기반 요약

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    assert (vI != v2);//query
   예제 프로그램
```



I개 주요 요소 기반 함수 호출 요약(주요 요소 = {7,8})



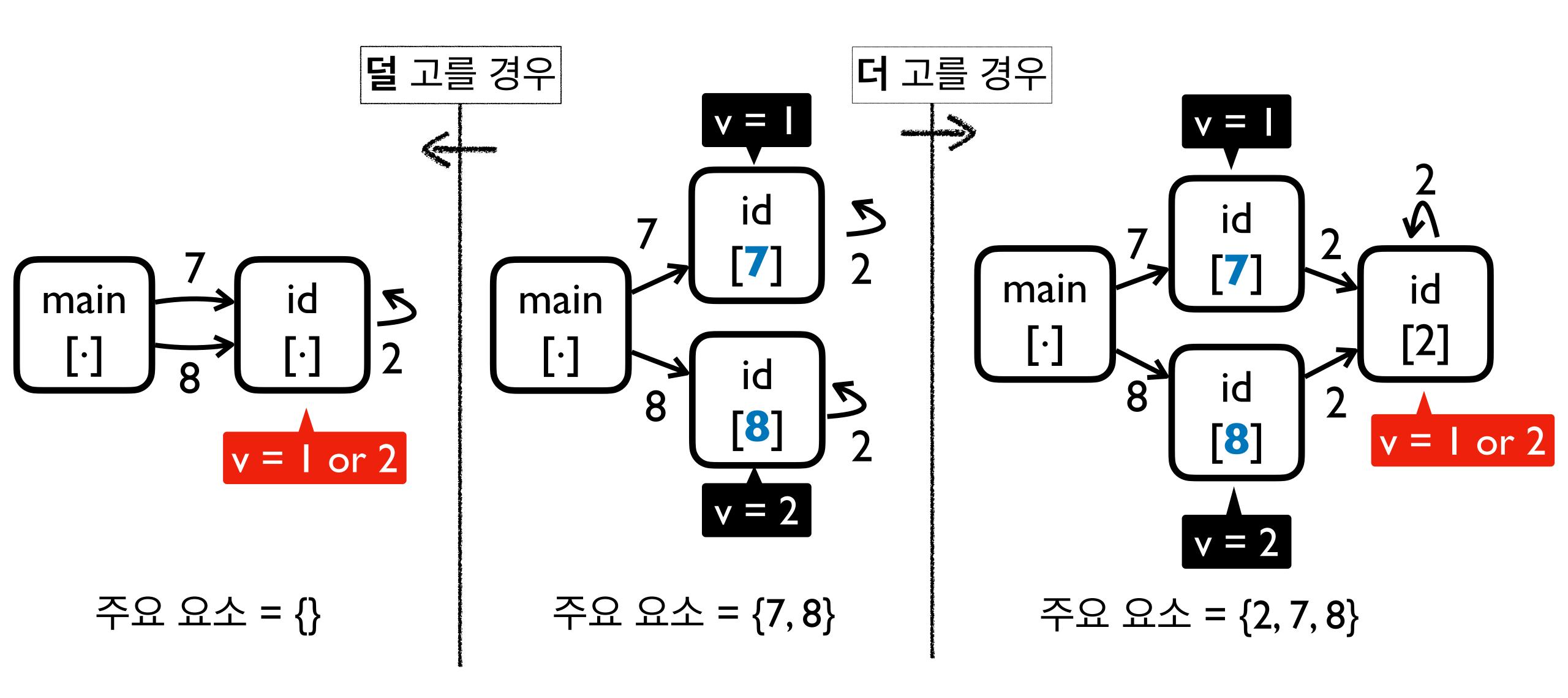
Challenge:

분석 전에 주요 요소를 **정확**하게 알아내야 함

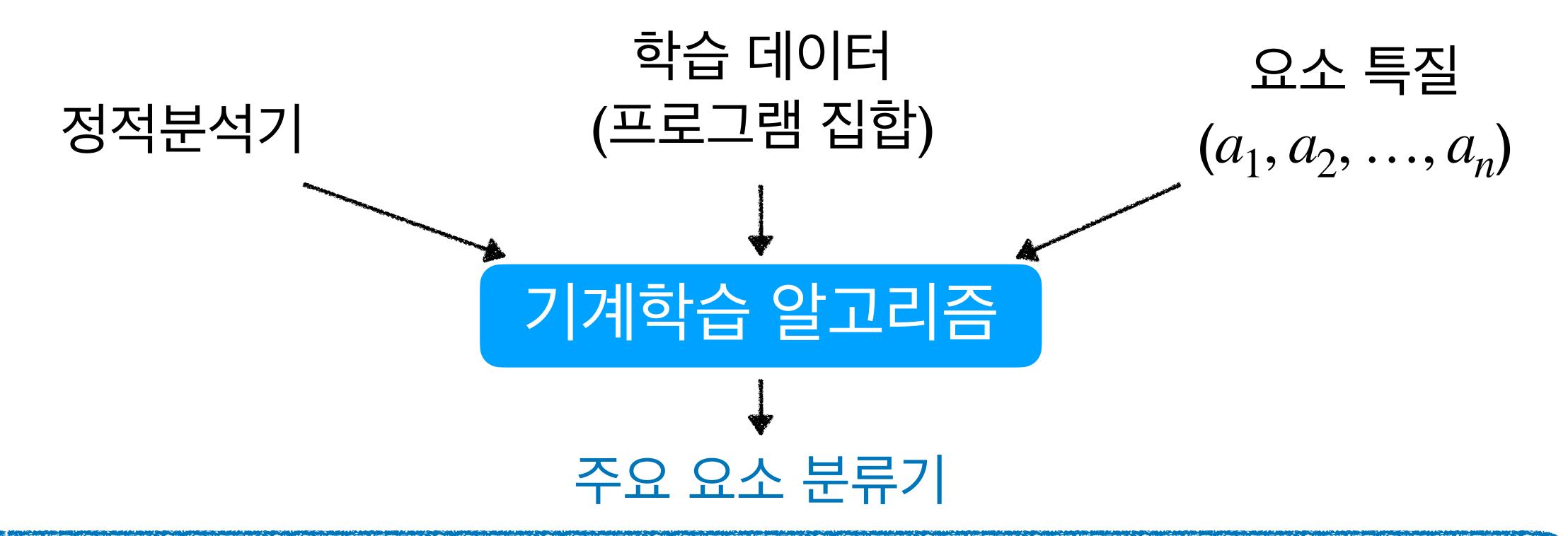
1개 주요 맥락 기산 함수 호출 요익

(주요 요소 = {7,8})

• 정확하게 분류해야만 분석의 정확도를 향상시킬 수 있음



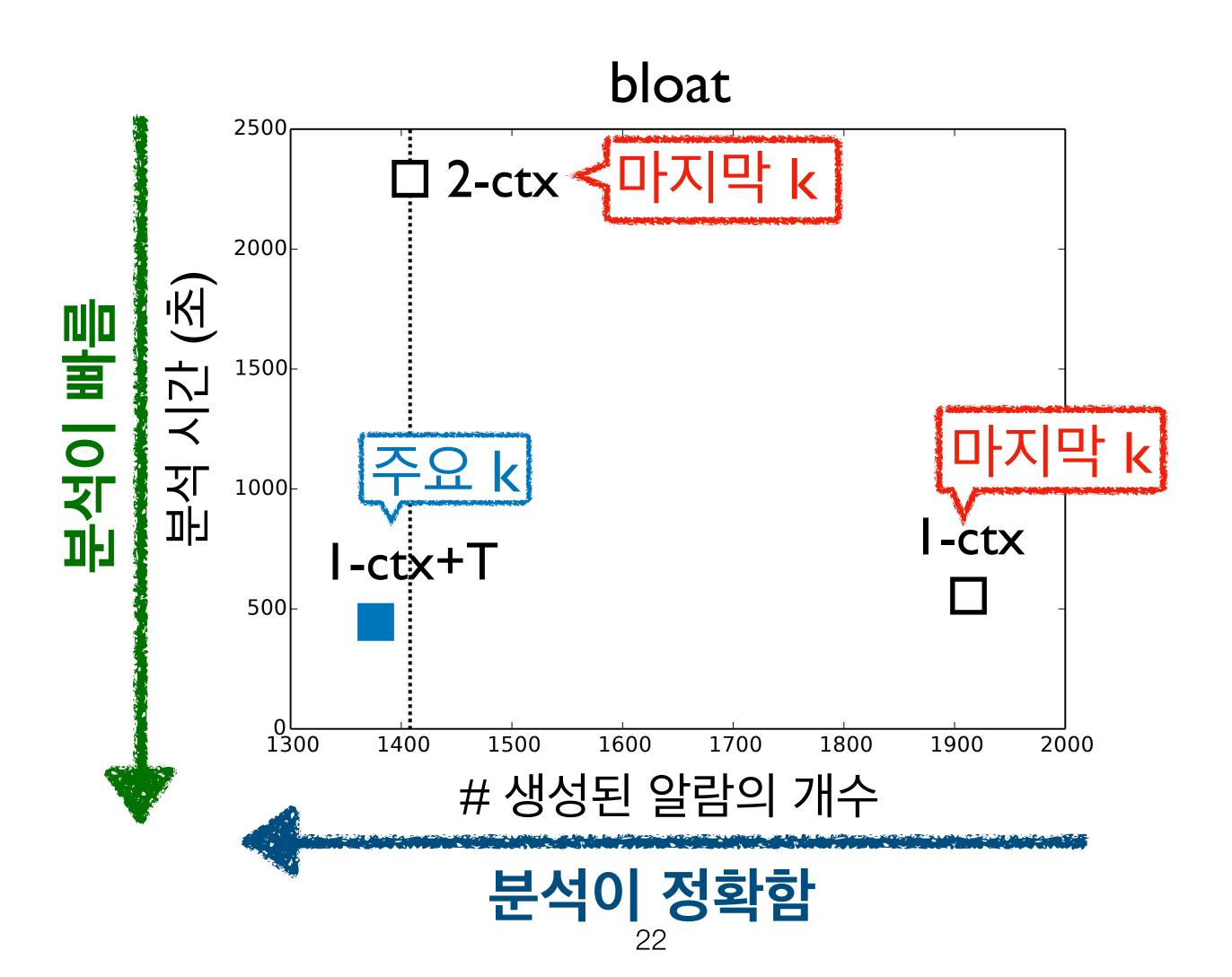
접근 방법: 데이터 기반 컨텍스트 터널링



$$f = (a_1 \land \neg a_2 \land \neg a_3 \land \ldots) \lor (a_1 \land \neg a_3 \land a_7 \land \ldots) \lor \ldots$$

마지막 k 기반 요약 vs 주요 k기반 요약

• 주요 1개 기반 요약이 마지막 2개 기반 요약보다 더 높은 정확도를 보임



2-ctx **4** 2000 주요 k 1000 -ctx+T1500

• 2-ctx 는 연구에서 정확도 상한선으로 사용되어 왔음

" ...it covers more than two-thirds of the precision advantage of 20bjH" -Smaragdakis et al. [PLDI' 14]

"... 98.8% of the precision of 2obj can be preserved..."

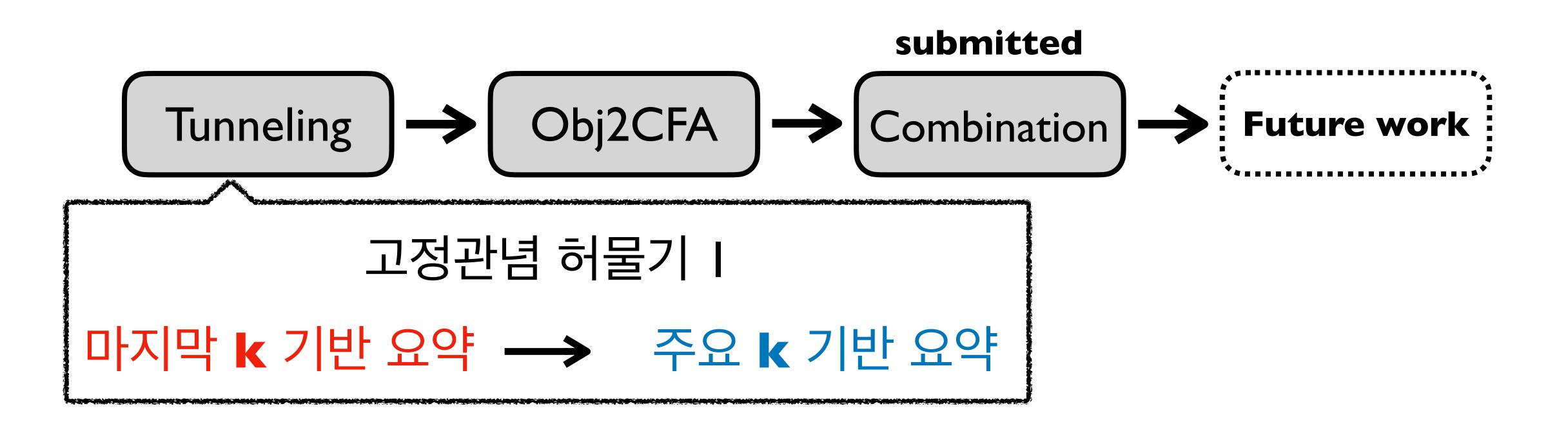
-Li et al. [OOPSLA' 18]

"Scaler still attains most of the precision gains of 20bj ..."
-Li et al. [FSE' 18]

• • •

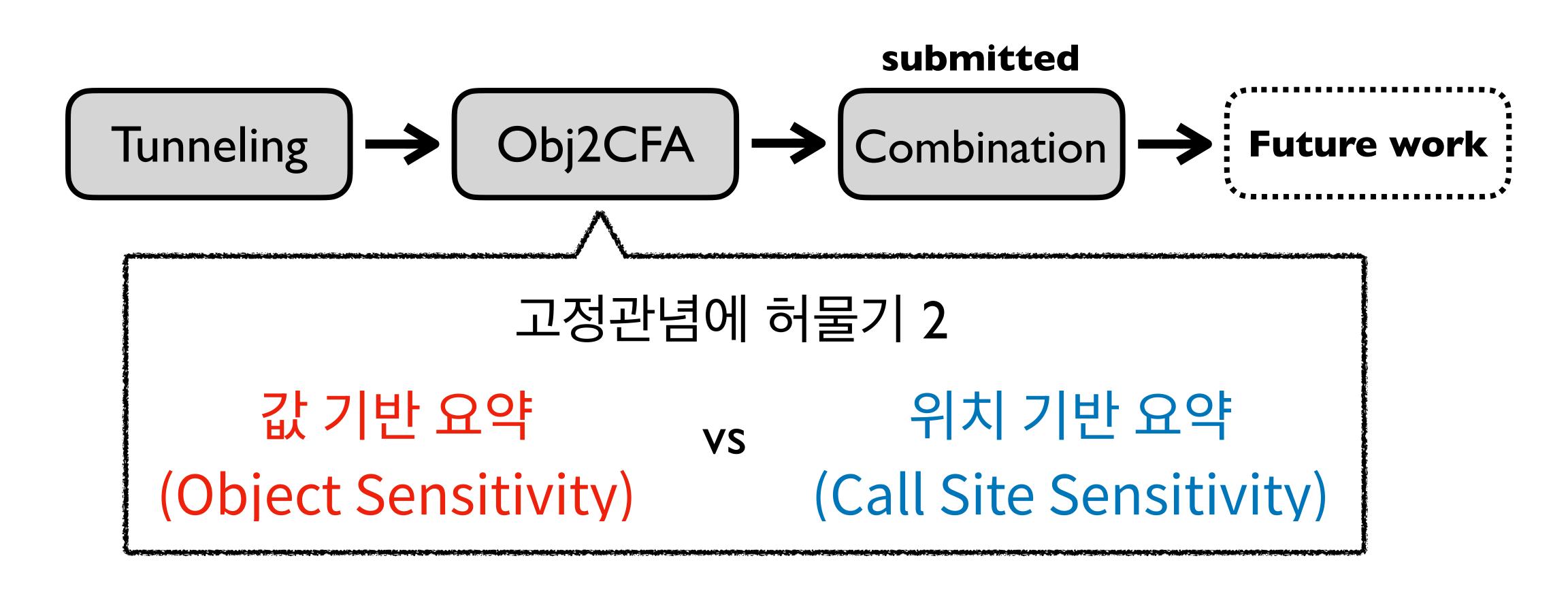
고정관념에 도전하기

• 목표: 주요 k기반 요약 방식을 표준으로 만들기



고정관념에 도전하기

• 목표: 주요 k기반 요약 방식을 표준으로 만들기



위치 기반 요약 vs 값 기반 요약

위치 기반 요약 (1981) 값 기반 요약 (2002) "무엇"을 기반으로 요약 • "어디"를 기반으로 요약 goo goo **OI** or **O2** 0: foo(){ 0: foo(: goo(); foo foo goo goo 2: goo(); p.goo(); Call graph Call graph

위치기반요약vs값기반요약

Parameterized Object Sensitivity for Points-to Analysis for Java

NA MILANOVA

Rensselaer Polytechnic Institute ATANAS ROUNTEV

Ohio State University

BARBARA G. RYDER Rutgers University

he goal of points-to analysis for Java is to determine the set of objects pointed to by a refere The goal of points-to analysis for Java is to determine the set of objects pointed to by a reference available or a reference object field. We present object sensitivity, a new form of context sensitivity for flow-insensitive points-to analysis for Java. The key idea of our approach is to analyze a meth separately for each of the object names that represent run-time objects on which this method me invoked. To ensure flexibility and practicality, we propose a parameterization framework thallows analysis designers to control the tradeoffs between cost and precision in the object-sensitive about the processing of the processing the sensitive analysis designers to control the tradeoffs between cost and precision in the object-sensitive analysis.

naysis.

Side-effect analysis determines the memory locations that may be modified by the execution of a rogram statement. Def-use analysis identifies pairs of statements that set the value of a memory ocation and subsequently use that value. The information computed by such analyses has a wide ariety of uses in compilers and software tools. This work proposes new versions of these analyses at are based on object-sensitive points-to analysis.

is. On a set of 23 Java programs, our experiments show that these analyses have comparable cost o a context-insensitive points-to analysis for Java which is based on Andersen's analysis for C. Our sults also show that object sensitivity significantly improves the precision of side-effect analys nd call graph construction, compared to (1) context-insensitive analysis, and (2) context-sensiti pints-to analysis that models context using the invoking call site. These experiments demon hat object-sensitive analyses can achieve substantial precision improvement, while at the san

preliminary version of this article appeared in Proceedings of the International Symposium

his research was supported in part by National Science Foundation (NSF) grant CCR-990098 author's addresses: A. Milanova, Department of Computer Science, Rensselaer Polytechnic Institute, 1108th Street, Troy, NY 12180; email: milanova@cs.rpi.edu; A. Rountey, Department of Com uter Science and Engineering, Ohio State University, 2015 Neil Avenue, Columbus, OH 43210 multi-vontev@ese.ohio-state.edu; B. G. Ryder, Department of Computer Science, Rutgers Univer ity, 100 Frelinghuysen Road, Piscataway, NJ 08854; email: ryder@sc.rutgers.edu.

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Context-sensitive points-to analysis: is it worth it?*

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olhotak@uwaterloo.ca hendren@sable.mcgill.ca

School of Computer Science, University of Waterloo, Waterloo, ON, Canada School of Computer Science, McGill University, Montreal, QC, Canada

Abstract. We present the results of an empirical study evaluating the precision of subset-based points-to analysis with several variations of context sensiti ava benchmarks of significant size. We compare the use of call site strings as the context abstraction, object sensitivity, and the BDD-based context-sensitive algorithm proposed by Zhu and Calman, and by Whaley and Lam. Our study includes analyses that context-sensitively specialize only pointer variables, as well as ones that also specialize the heap abstraction. We measure both characteristics of the points-to sets themselves, as well as effects on the precision of client analyses. To guide development of efficient analysis imple f contexts, the number of distinct contexts, and the number of distinct points-to sets that arise with each context sensitivity variation. To evaluate precision, we measure the size of the call graph in terms of methods and edges, the number of The results of our study indicate that object-sensitive analysis implementations are likely to scale better and more predictably than the other approaches; that object-sensitive analyses are more precise than comparable variations of the other approaches; that specializing the heap abstraction improves precision more than extending the length of context strings; and that the profusion of cycles in Java call graphs severely reduces precision of analyses that forsake context sensitivity in cyclic regions.

Does context sensitivity significantly improve precision of interprocedural analysis o object-oriented programs? It is often suggested that it could, but lack of scalable implementations has hindered thorough empirical verification of this intuition.

Of the many context sensitive points-to analyses that have been proposed (e.g. [1,4, 8,11,17-19,25,28-31]), which improve precision the most? Which are most effective for specific client analyses, and for specific code patterns? For which variations are we likely to find scalable implementations? Before devoting resources to finding efficient imple mentations of specific analyses, we should have empirical answers to these questions.

This study aims to provide these answers. Recent advances in the use of Binary De cision Diagrams (BDDs) in program analysis [3, 12, 29, 31] have made context sensitive analysis efficient enough to perform an empirical study on benchmarks of significant size.

Evaluating the Benefits of Context-Sensitive Points-to Analysis Using a BDD-Based Implementation

ONDŘEJ LHOTÁK

University of Waterloo

LAURIE HENDREN McGill University

we present Paddle, a framework of BID-based context-sensitive points-to and call graph analyses for Java, as well as client analyses that use their results. Paddle supports several variations of context-sensitive analyses, including call site strings and object sensitivity, and context-sensitively specializes both pointer variables and the heap abstraction. We empirically evaluate the precision of these context-sensitive analyses on significant Java programs. We find that that object sensitive analyses are more precise than comparable variations of the other approaches, and that specializing the heap abstraction improves precision more than extending the length of context strings.

General Terms: Languages, Design, Experimentation, Measurement

Additional Key Words and Phrases: Interprocedural program analysis, context sensitivity, binar decision diagrams, Java, points-to analysis, call graph construction, cast safety analysis ACM Reference Format:

Lhoták, O. and Hendren, L. 2008. Evaluating the benefits of context-sensitive points-to ana using a BD-based implementation. ACM Trans. Softw. Engin. Method. 18, 1, Article 3 (Septem 2008), 53 pages. DOI = 10.1145/1391984.1391987 http://doi.acm.org/10.1145/1391984.139198

This is a revised and extended version of an article which appeared in Proceedings of the 15th International Conference on Compiler Construction, Lecture Notes in Computer Science, vol. 3923

Springer, 47–64. Authors' addresses: O. Lhoták, D. R. Cheriton School of Computer Science, University of Waterlo Authors addresses: O. Lhotak, D. K. Cherhon Senson of Computer Science, Interest of a case of Computer Science, Interest of the Computer Science, McGill University, 3480 University Street, Room 318, Montreal, QC, H3A 2A

Strictly Declarative Specification of Sophisticated Points-to Analyses

University of Massachusetts, Amherst Amherst, MA 01003, USA martin.bravenboer@acm.org yannis@cs.umass.edu

We present the Door framework for points-to analysis of Java programs. Doop builds on the idea of specifying pointer analysis algorithms declaratively, using Datalog: a logice declarative approach further than past work by describing the full end-to-end analysis in Datalog and optimizing

ing the full end-to-end analysis in Datalog and optimizing aggressively using a novel technique specifically targeting highly recursive Datalog programs.

As a result, Door achieves several benefits, including full order-of-magnitude improvements in runtime. We compare Door with Lhoták and Hendren's Pannia, which defines the state of the art for context-sensitive analyses. For the exact same logical points to definitions (and, consequently, identical precision) Door is more than 15x faster than Papons for al precision) Door is more than 15x faster than Padole for a 1-call-site sensitive analysis of the DaCapo benchmarks, compared to the prior state of the art, Door often achieves speedups of an order-of-magnitude for several important analyses. Additionally, Door scales to very precise analyses that are impossible with Papua and Whaley et al.'s bddbddb, directly addressing open problems in past literature. Finally, our implementation is modular and can be easily configured to analyses with a wide range of characteristics, largely due to its declarativeness.

Compared to the prior state of the art, Door often achieves speedups of an order-of-magnitude for several important analyses. The main elements of our approach are the use of the bard to grant analysis to this low-level [13,23,29] and to state of the art, Door often achieves speedups of an order-of-magnitude for several important analyses. The main elements of our approach are the use of the bard to grant analysis of the prior state of the art, Door often achieves speedups of an order-of-magnitude for several important analyses. The main elements of our approach are the use of the bard to grant analyses, and the along the prior state of the art, Door often achieves speedups of an order-of-magnitude for several important analyses.

Categories and Subject Descriptors F.3.2 [Logics and Meanings of Programs]: Semantics of Programming Languages—Program Analysis; D.1.6 [Programming Techniques]: Logic Programming General Terms Algorithms, Languages, Performance

tion forms the basis for practically all higher-level program

has been devoted to efficient and precise pointer analysis techniques. Context-sensitive analyses are the most common class of precise points-to analyses. Context sensitive analysi approaches qualify the analysis facts with a context abstration, which captures a static notion of the dynamic contex of a method. Typical contexts include abstractions of metho

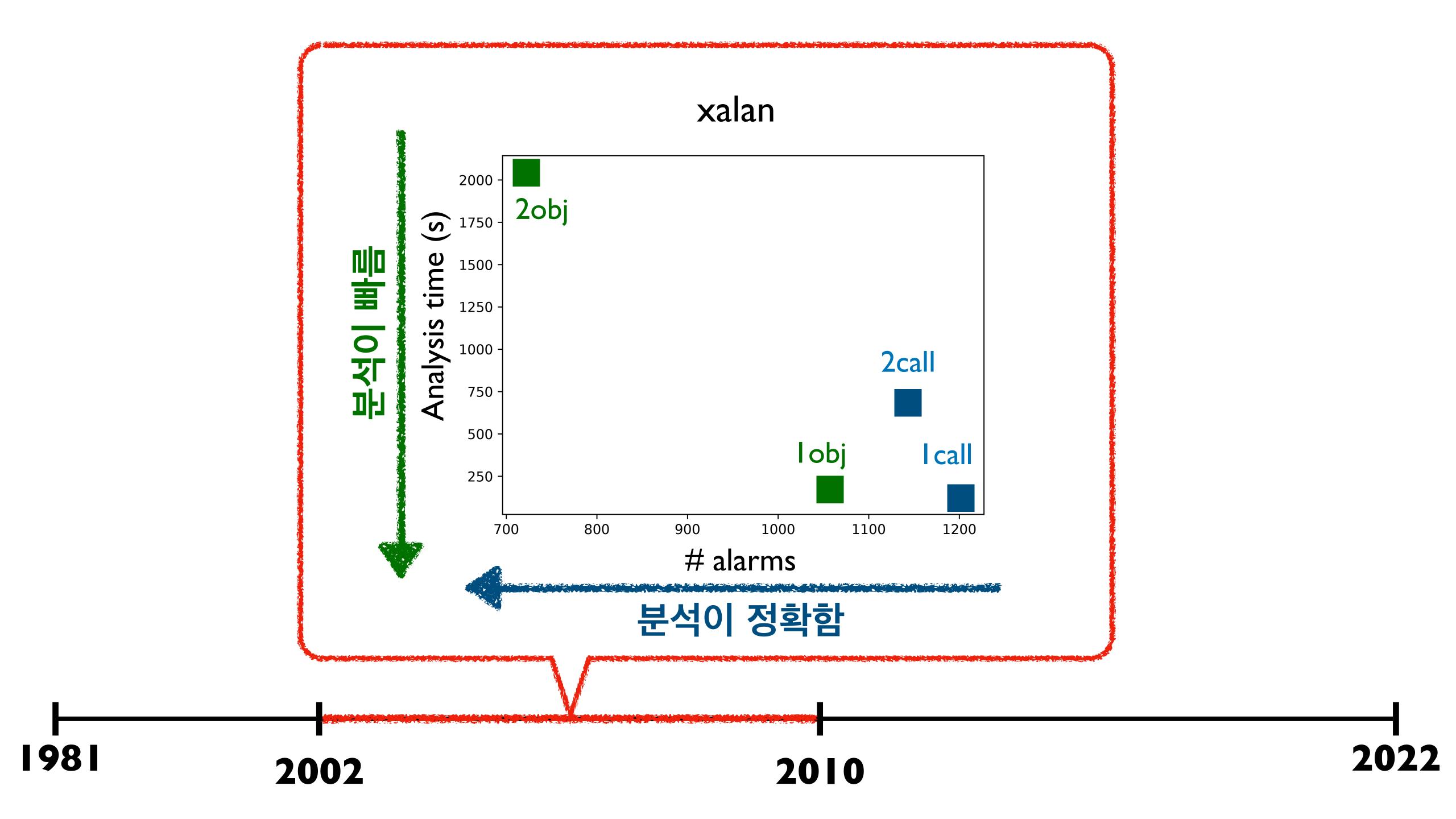
points-to analysis framework that makes feasible the mos precise context-sensitive analyses reported in the literature Door implements a range of algorithms, including conter insensitive, call-site sensitive, and object-sensitive analys insensitive, call-site sensitive, and object-sensitive analyses all specified modularly as variations on a common code base Compared to the prior state of the art, Door often achieve speedups of an order-of-magnitude for several importan analyses.

The main elements of our approach are the use of the Data

high-level [6,9]) is far from new. Our novel optimization proach, however, accounts for several orders of magnitude of performance improvement: unoptimized analyses typically run over 1000 times more slowly. Generally our optimiza-tions fit well the approach of handling program facts as a database, by specifically targeting the indexing scheme ar thermore, our approach is entirely Datalog based, encoding incrimore, our approach is entirely Dataiog based, encount declaratively the logic required both for eall graph construction as well as for handling the full semantic complexit of the Java language (e.g., static initialization, finalization reference objects, threads, exceptions, reflection, etc.). Thi makes our pointer analysis specifications elegant, modular but also difficult and easy to have Generally, our work in

2022 2010

1981



• 값 기반 요약 방식이 우수하다고 강의되는 중

Object-Sensitivity

- The dominant flavor of context-sensitivity for object languages.
- It uses object abstractions (i.e. allocation sites) as qualifying a method's local variables with the alloc receiver object of the method call.

```
class A { void m() { return; } }
b = new B();
b.m();
The context of m is the allocation site of b.
```

Object-Sensitivity (vs. call-site sensitivity)

```
program
class S {
  Object id(Object a) { return a; }
Object id2(Object a) { return id(a)
class C extends S {
  void fun1() {
    Object al = new Al();
    0bject b1 = id2(a1);
class D extends S {
  void fun2() {
    Object a2 = new A2();
                                      id2
    0bject b2 = id2(a2);
```

Object-sensitive pointer

- Milanova, Rountev, and Ryder. Parameteriz sensitivity for points-to analysis for Java. AC Eng. Methodol., 2005.
- Context-sensitive interprocedural pointer analysis
- For context, use stack of receiver objects
- (More next week?)
- Lhotak and Hendren. Context-sensitive poir worth it? CC 06
- Object-sensitive pointer analysis more precise that for Java
- Likely to scale better

Lecture Notes: **Pointer Analysis**

15-819O: Program Analysis Jonathan Aldrich jonathan.aldrich@cs.cmu.edu

1 Motivation for Pointer Analysis

In programs with pointers, program analysis can become mo Consider constant-propagation analysis of the following prog

> 2: p := &z3: *p := 2

In order to analyze this program correctly we must be instruction 3 p points to z. If this information is available we

 $f_{CP}[*p := y](\sigma) = [z \mapsto \sigma(y)]\sigma$ where must-point-to

When we know exactly what a variable x points to, we sa must-point-to information, and we can perform a strong updat variable z, because we know with confidence that assigning to z. A technicality in the rule is quantifying over all z such point to z. How is this possible? It is not possible in C or Java; names for the same location are in scope.

Of course, it is also possible that we are uncertain to wh distinct locations p points. For example:

Pointer Analysis

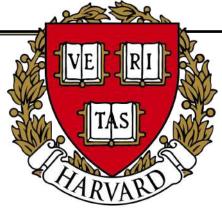
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National and Kapodistrian University of Athens



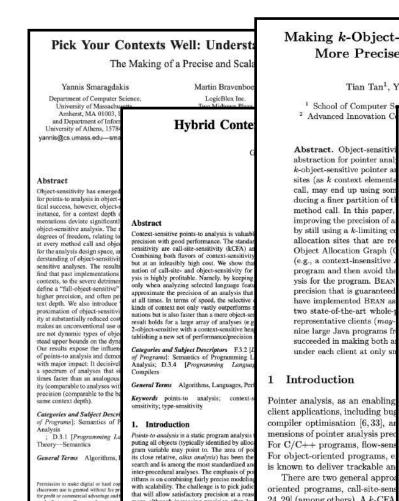








값 기반 요약을 대상으로 하는 연구가 쏟아짐



Making k-Object-Sensitive Pointer A More Precise with Still k-Limiting

Tian Tan¹, Yue Li¹, and Jingling Xue^{1,2}

School of Compu

Abstract. Object-sens

abstraction for pointer a k-object-sensitive pointe sites (as k context eleme call, may end up using s ducing a finer partition of method call. In this pap improving the precision o

by still using a k-limiting allocation sites that are re (e.g., a context-insensitive A nine large Java programs fr succeeded in making both a under each client at only sn

Introduction

Advanced Innovation

emonstrate its effectiveness by discussi hy it is a better alternative of the alloca or type-dependent clients and evaluating for many program analyses where call gra

is known to deliver trackable There are two general approx oriented programs, call-site-se [24, 29] (among others). A k-CFA call by using a sequence of ksite). In contrast, a k-object-se k labels with each denoting a

Modeling the He

Mainstream points-to analysis techn languages rely predominantly on the alloca tion to model heap objects. We present M

program and then avoid the sysis for the program. BEAN precision that is guaranteed have implemented BEAN as two state-of-the-art whole-prepresentative clients (may-right) system of the program and then avoid the sysis of the program. BEAN heap abstraction that is specifically developed the needs of an important class of type-described the needs of an important class of type-describe points-to analysis to run significantly faster nearly the same precision for type-dependen

in cost and precision for specific gro lems. We do not need a different po



Scalability-First

Self-Tuning

Precision-Guided Context Sensitivity for Pointer Ana

TIAN TAN, Aarhus University, Denmar ANDERS MØLLER, Aarhus Universit YANNIS SMARAGDAKIS, University

Context sensitivity is an essential techniq observed that applying context sensitivit balance between analysis precision and do not provide much insight into what cl principled approach for identifying precis explain where most of the imprecision ari an efficient algorithm to recognize these

tradeoffs between analysis precision and s Our experimental results on standard b applies context sensitivity partially, only on (98.8%) of the precision of a highly-precise with a context-sensitive heap), with a sul CCS Concepts: • Theory of computation Additional Key Words and Phrases: static a

ACM Reference Format: Yue Li, Tian Tan, Anders Møller, and Yar Pointer Analysis. Proc. ACM Program. Lang.

Pointer analysis is a fundamental f

Smaragdakis et al. 2011], which allows

to separate the static abstractions of dif

found during the pre-analysis,

Sridharan et al. 2007].

CCS CONCEPTS KEYWORDS

choose one that leads to reasonable analysis time and

We present the SCALER framework that addresses this

context-sensitivity. It then selects an appropriate va-

ich method so that the total amount of points-to info

unded, while utilizing the available space to maximiz

ictable scalability for all the evaluated programs (e.g., s

can reach 10x for 2-object-sensitivity), while providing

pointer variables in a program. Such tic analysis, points-to analysis, Java inter-procedural control flow in object engineering tools, e.g., for bug detec

yueli@cs.au.dk

ABSTRACT

analysis [Arzt et al. 2014; Grech and S tion [Fink et al. 2008; Pradel et al. 2012 For decades, numerous analysis ted precise and more efficient, especially for ointer analysis is a family of static analysis techn Balatsouras 2015; Sridharan et al. 2 oundation for many other analyses and software e precision is context sensitivity [Mila

sks, such as program slicing [36, 39], reflection analysi g detection [13, 26], security analysis [1, 23], program

a common type. We formulate the type-consistency of two objects as

Data-Driven Context-Sensitivity for Points-to Analysis

SEHUN JEONG, Korea University, Repu MINSEOK JEON*, Korea University, Repub SUNGDEOK CHA, Korea University, Ro HAKJOO OH7, Korea University, Repub

We present a new data-driven approach to a for Java. While context-sensitivity has great other precision-improving techniques, it is d most from context-sensitivity and decide how designing such rules is a nontrivial and labor overcome these challenges, we propose an auto context-sensitivity from codebases. In our app heuristic rules, in disjunctive form of properties context-sensitivity. We present a greedy also We implemented our approach in the Doop experimental results show that our approac CCS Concepts: • Theory of computation

> Additional Key Words and Phrases: Data-ACM Reference Format: Sehun Jeong, Minseok Jeon, Sungdeok Cha, ar

Analysis. Proc. ACM Program. Lang. 1, OOPSI

Points-to analysis is one of the most in memory locations that a pointer variab for many program verification tasks (e.g., of subsequent higher-level program an

For object-oriented languages, cont guish method's local variables and obje-The first and second authors contributed equal

sion to make digital or hard copies of all or provided that copies are not made or distribu Abstracting with credit is permitted. To copy of prior specific permission and/or a fee. Request y © 2017 Association for Computing Machiner 2475-1421/2017/10-ART100

· program size is far from a reliable predict ever, 2type is not scalable for the former bu



Learning Graph-based Heuristic without Handcrafting Application

MINSEOK JEON, MYUNGHO LEE, and HAK We present Graphick, a new technique for automatical Striking a balance between precision and scalability of

heuristics. For example, because applying context se impractical, pointer analysis typically uses a heuristic to Past research has shown that exploiting the program's cost-effective analysis heuristics, promoting the recent graph representations of programs obtained from a pre such heuristics remains challenging, requiring a great d aim to reduce this burden by learning graph-based heuri application-specific features. To do so, we present a features. algorithm for learning analysis heuristics within the lang used it to learn graph-based heuristics for object sens show that our approach is general and can generate his heuristics are as competitive as the existing state-of-the CCS Concepts: • Software and its engineering → Au

Additional Key Words and Phrases: Data-driven static an analysis, Context sensitivity, Heap abstraction

ACM Reference Format: Minseok Jeon, Myungho Lee, and Hakjoo Oh. 2020. Le without Handcrafting Application-Specific Features. (November 2020), 31 pages. https://doi.org/10.1145/3428

1 INTRODUCTION

Pointer analysis is a fundamental program analys various software engineering tools. The goal of poestimate heap objects that pointer variables may essential for virtually all kinds of program analy et al. 2015; Livshits and Lam 2003; Naik et al. 2006 et al. 2014; Avots et al. 2005; Grech and Smarag program verifiers [Fink et al. 2008], symbolic exe repair tools [Gao et al. 2015; Hong et al. 2020; I

*Corresponding author





Precision-Preserving Yet Fast Object-Sensitive Pointer Analysis with Partial Context Sensitivity

JINGBO LU, UNSW Sydney, Austra JINGLING XUE, UNSW Sydney, A

Object-sensitivity is widely used as a sensitively for object-oriented langu programs, k-object-sensitive pointe values of k, where $k \leq 2$ typically. A k-obj to analyze only some methods analysis. While already effective, thes that makes k-obj run significantly fa EAGLE is to enable k-obj to analyze a n some of its selected variables/allocati reasoning about context-free-lang based on a new CFL-reachability for comparing it with the prior art in ter-

CCS Concepts: • Theory of computa Additional Key Words and Phrases: I

ACM Reference Format: Jingbo Lu and Jingling Xue. 2019.

Authors' addresses: Jingbo Lu, UNSW Sy jingling@cse.unsw.edu.au.

Making Pointer Analysis More Precise by Unleashing the **Power of Selective Context Sensitivity** consequently, are limited in the efficien

Partial Context Sensitivity. Proc. ACI https://doi.org/10.1145/3360574

INTRODUCTION

For object-oriented languages suc precision for pointer analysis [Ll insensitive pointer analysis, such as once, producing one points-to set allocation site in the method. In multiple times under different ca thereby producing multiple points

abstract objects for modeling ever To tame the combinatorial expl sequence of k context elements. object-oriented programs: (1) k-call of a method by its k-most-recent

TIAN TAN, Nanjing University, China YUE LI*, Nanjing University, China

XIAOXING MA, Nanjing University, China CHANG XU, Nanjing University, China YANNIS SMARACDAKIS, University of Athens, Greece

Fraditional context-sensitive pointer analysis is hard to scale for large and complex Java programs. To addre this issue, a series of selective context-sensitivity approaches have been proposed and exhibit promising result In this work, we move one step further towards producing highly-precise pointer analyses for hard-to-analyze Java programs by presenting the Unity-Relay framework, which takes selective context sensitivity to the next level. Briefly, Unity-Relay is a one-two punch: given a set of different selective context-sensitivity approaches say $S = S_1, \ldots, S_n$, Unity-Relay first provides a mechanism (called Unity) to combine and maximize the precision of all components of S. When Unity fails to scale, Unity-Relay offers a scheme (called Relay) to pass and accumulate the precision from one approach S_l in S to the next, S_{l+1} , leading to an analysis that is

more precise than all approaches in S. As a proof-of-concept, we instantiate Unity-Relay into a tool called BATON and extensively evaluate it or a set of hard-to-analyze Java programs, using general precision metrics and popular clients. Compared with the state of the art, Baton achieves the best precision for all metrics and clients for all evaluated programs. The difference in precision is often dramatic-up to 71% of alias pairs reported by previously-best algorithm are found to be spurious and eliminated.

CCS Concepts: • Theory of computation \rightarrow Program analysis.

Article 147 (October 2021), 27 pages. https://doi.org/10.1145/3485524

ACM Reference Format: Tian Tan, Yue Li, Xiaoxing Ma, Chang Xu, and Yannis Smaragdakis. 2021. Making Pointer Analysis More Precise by Unleashing the Power of Selective Context Sensitivity. Proc. ACM Program. Lang. 5, OOPSLA,

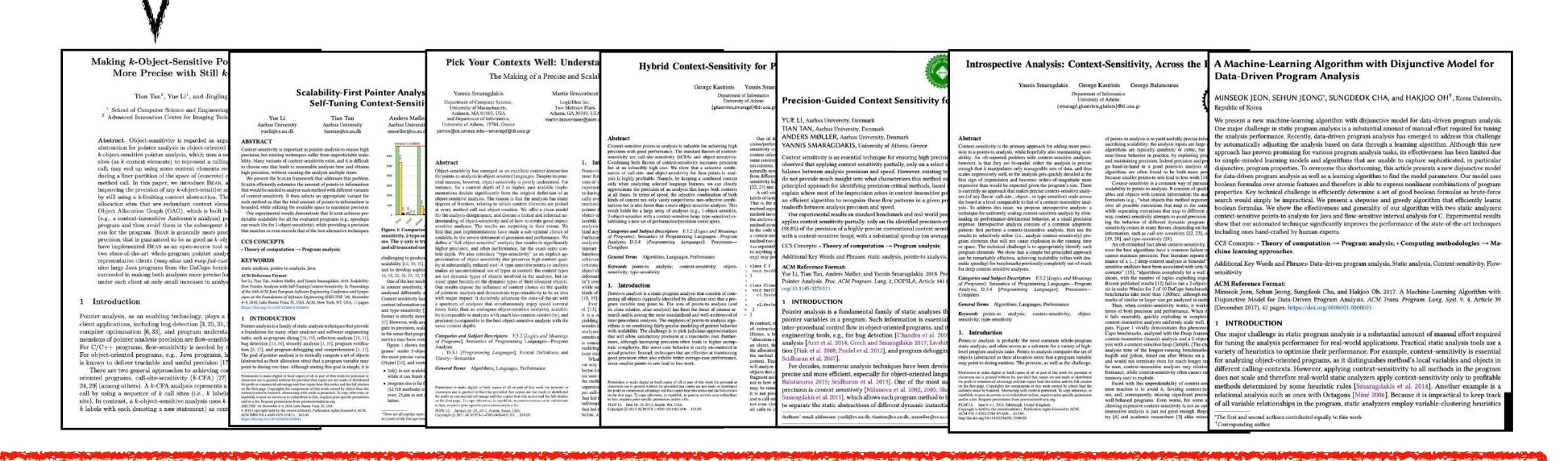
Additional Key Words and Phrases: Pointer Analysis, Alias Analysis, Context Sensitivity, Java

Pointer analysis is important for an array of real-world applications such as bug detection [Chandra et al. 2009; Naik et al. 2006], security analysis [Arzt et al. 2014; Livshits and Lam 2005], program verification [Fink et al. 2008; Pradel et al. 2012] and program understanding [Li et al. 2016; Sridharan

Corresponding author

"For comparison, we have included 2call to demonstrate the superiority of object sensitivity over call-site sensitivity"

- Tan et al. [2016]



"We do not consider call-site sensitive analyses as they are typically both less precise and scalable..."

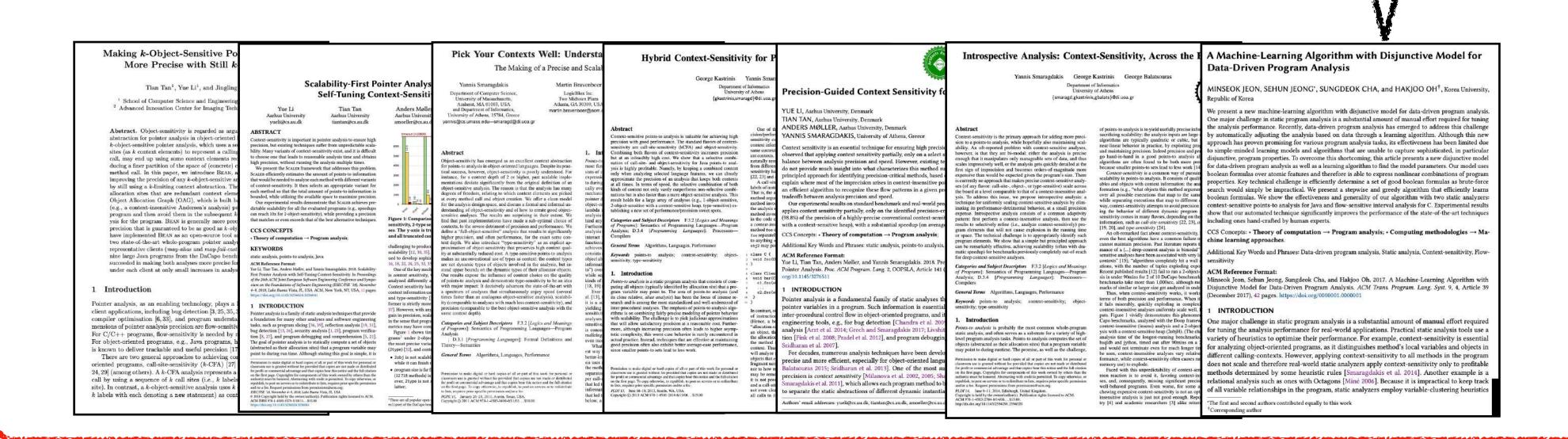
- Li et al. [2018]



"We do not discuss the performance of our approach for call-sitesensitivity since call-site-sensitivity is less important than others

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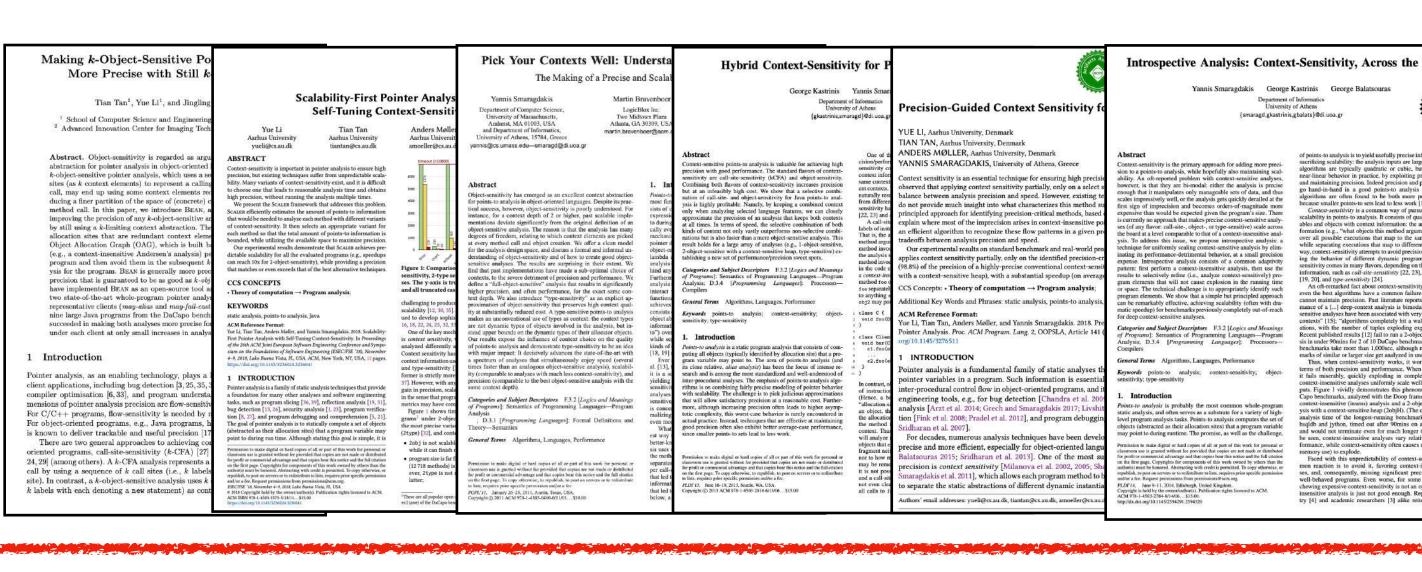
- Jeon et al. [2019]

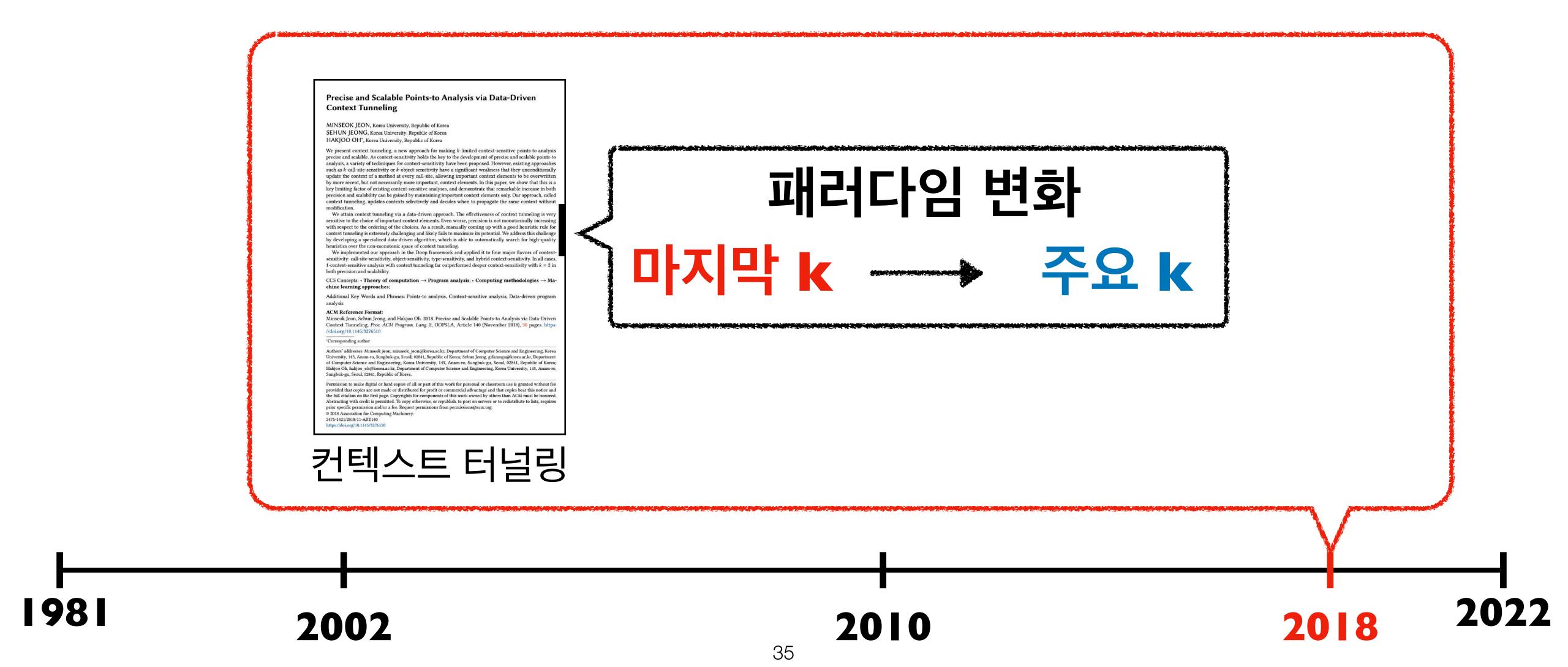


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- Jeon et al. [2019]





Return of CFA: Call-Site Sensitivity Can Be Superior to Object Sensitivity Even for Object-Oriented Programs

MINSEOK JEON and HAKJOO OH*, Korea University, Republic of Korea

In this paper, we challenge the commonly-accepted wisdom in static analysis that object sensitivity is superior to call-site sensitivity for object-oriented programs. In static analysis of object-oriented programs, object sensitivity has been established as the dominant flavor of context sensitivity thanks to its outstanding precision. On the other hand, call-site sensitivity has been regarded as unsuitable and its use in practice has been constantly discouraged for object-oriented programs. In this paper, however, we claim that call-site sensitivity is generally a superior context abstraction because it is practically possible to transform object sensitivity into more precise call-site sensitivity. Our key insight is that the previously known superiority of object sensitivity holds only in the traditional k-limited setting, where the analysis is enforced to keep the most recent k context elements. However, it no longer holds in a recently-proposed, more general setting with context tunneling. With context tunneling, where the analysis is free to choose an arbitrary *k*-length subsequence of context strings, we show that call-site sensitivity can simulate object sensitivity almost completely, but not vice versa. To support the claim, we present a technique, called OBJ2CFA, for transforming arbitrary context-tunneled object sensitivity into more precise, context-tunneled call-site-sensitivity. We implemented Obj2CfA in Doop and used it to derive a new call-site-sensitive analysis from a state-of-the-art object-sensitive pointer analysis. Experimental results confirm that the resulting call-site sensitivity outperforms object sensitivity in precision and scalability for real-world Java programs. Remarkably, our results show that even 1-call-site sensitivity can be more precise than the conventional 3-object-sensitive analysis.

1 INTRODUCTION

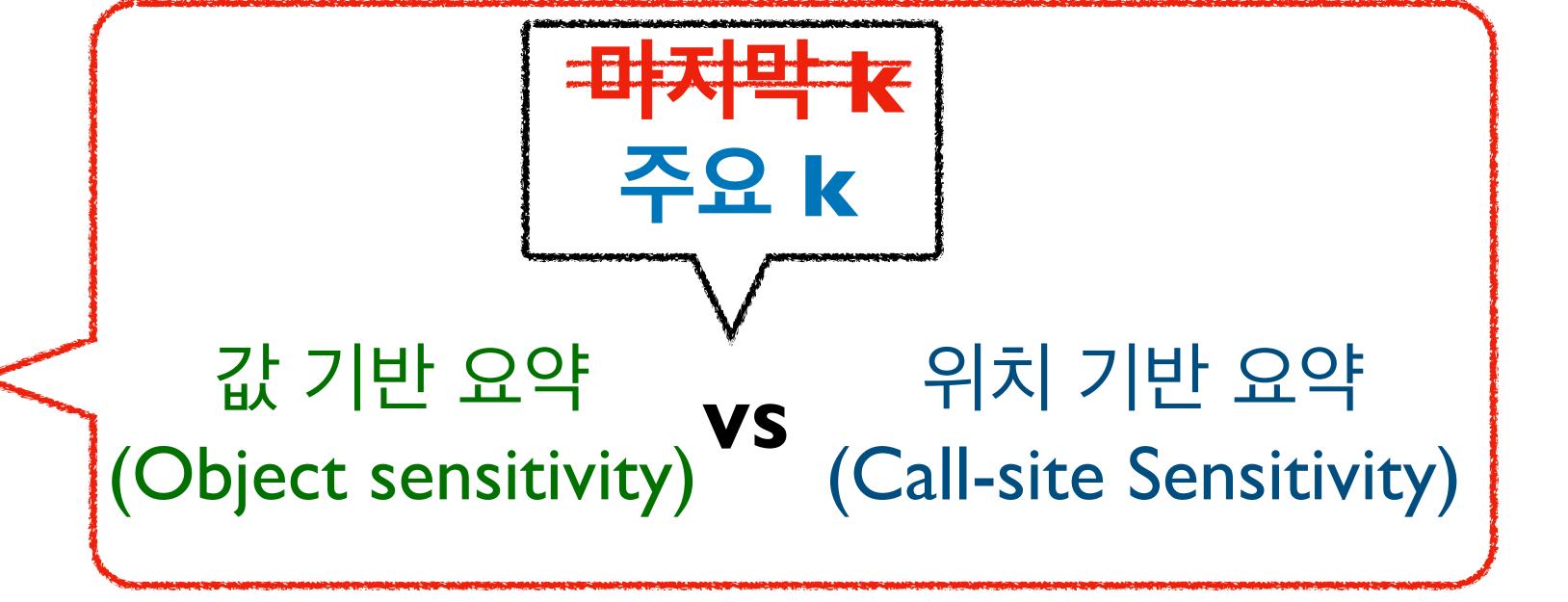
"Since its introduction, object sensitivity has emerged as the dominant flavor of context sensitivity for object-oriented languages."

-Smaragdakis and Balatsouras [2015]

Context sensitivity is critically important for static program analysis of object-oriented programs. A context-sensitive analysis associates local variables and heap objects with context information of method calls, computing analysis results separately for different contexts. This way, context sensitivity prevents analysis information from being merged along different call chains. For object-oriente

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The and Ph the chi 1981] i allocat salvsis

sensitive analysis [Milanova et al. 2002, 2005; Smaragdakis et al. 2011] maintains a sequence of



1981 2002

2010

Exercise

```
class S {
 Object id(Object a) { return a; }
 Object id2(Object a) { return id(); }
class C extends S {
 void fun1() {
   Object a1 = new A1();
   Object b1 = id2(a1);
 }}
class D extends S {
 void fun2() {
   Object a2 = new A2();
   Object b2 = id2(a2);
 }}
 ● What is the result of 1-object-sensitive analysis? 		 정확함

    Explain the strength of object-sensitivity over call-site-sensitivity.
```

AAA616 2022 Fall, Lecture 8 Hakjoo Oh

28 / 31

```
Exercise
class S {
  Object id(Object a) { return a; }
  Object id2(Object a) { return id(); }
class C extends S {
  void fun1() {
    Object a1 = new A1();
    Object b1 = id2(a1);
  }}
class D extends S {
  void fun2() {
    Object a2 = new A2();
    Object b2 = id2(a2);
  }}
   • What is the result of 1-call-site-sensitive analysis?
                                                   정확함
   What is the result of 1-object-sensitive analysis?
  • Explain the strength of object-sensitivity over call-site-sensitivity. Lobi > call
```

Exercise

```
class S {
   Object id(Object a) { return a; }
   Object id2(Object a) { return id(); }
}
class C extends S {
   void fun1() {
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      Object b1 = id2(a1);
   }}
class D extends S {
   void fun2() {
      Object a2 = new A2();
      Object b2 = id2(a2);
   }}
```

- What is the result of 1-call-site-sensitive analysis?
- What is the result of 1-object-sensitive analysis?
- Explain the strength of object-sensitivity over call-site-sensitivity.

질문:

이를 보일 수 있는 예제를 만들어 보자

Hakjoo Oh AAA616 2022 Fall, Lecture 8

October 18, 2022

28 / 31

```
Exercise
class S {
  Object id(Object a) { return a; }
  Object id2(Object a) { return id(); }
class C extends S {
  void fun1() {
    Object a1 = new A1();
    Object b1 = id2(a1);
class D extends S {
  void fun2() {
    Object a2 = new A2();
    Object b2 = id2(a2);
  }}
  • What is the result of 1-call-site-sensitive analysis?
```

- What is the result of 1-object-sensitive analysis?
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질문:

이를 보일 수 있는 예제를 만들어 보자

(6개월 후) 도저히 안만들어짐

가설: Call > Obj

Return of CFA: Call-Site Sensitivity Can Be Superior to Object Sensitivity Even for Object-Oriented Programs

MINSEOK JEON and HAKJOO OH*, Korea University, Republic of Korea

In this paper, we challenge the commonly-accepted wisdom in static analysis that object sensitivity is superior to call-site sensitivity for object-oriented programs. In static analysis of object-oriented programs, object sensitivity has been established as the dominant flavor of context sensitivity thanks to its outstanding precision. On the other hand, call-site sensitivity has been regarded as unsuitable and its use in practice has been constantly discouraged for object-oriented programs. In this paper, however, we claim that call-site sensitivity is generally a superior context abstraction because it is practically possible to transform object sensitivity into more precise call-site sensitivity. Our key insight is that the previously known superiority of object sensitivity holds only in the traditional k-limited setting, where the analysis is enforced to keep the most recent k context elements. However, it no longer holds in a recently-proposed, more general setting with context tunneling. With context tunneling, where the analysis is free to choose an arbitrary *k*-length subsequence of context strings, we show that call-site sensitivity can simulate object sensitivity almost completely, but not vice versa. To support the claim, we present a technique, called OBJ2CFA, for transforming arbitrary context-tunneled object sensitivity into more precise, context-tunneled call-site-sensitivity. We implemented Obj2CfA in Doop and used it to derive a new call-site-sensitive analysis from a state-of-the-art object-sensitive pointer analysis. Experimental results confirm that the resulting call-site sensitivity outperforms object sensitivity in precision and scalability for real-world Java programs. Remarkably, our results show that even 1-call-site sensitivity can be more precise than the conventional 3-object-sensitive analysis.

1 INTRODUCTION

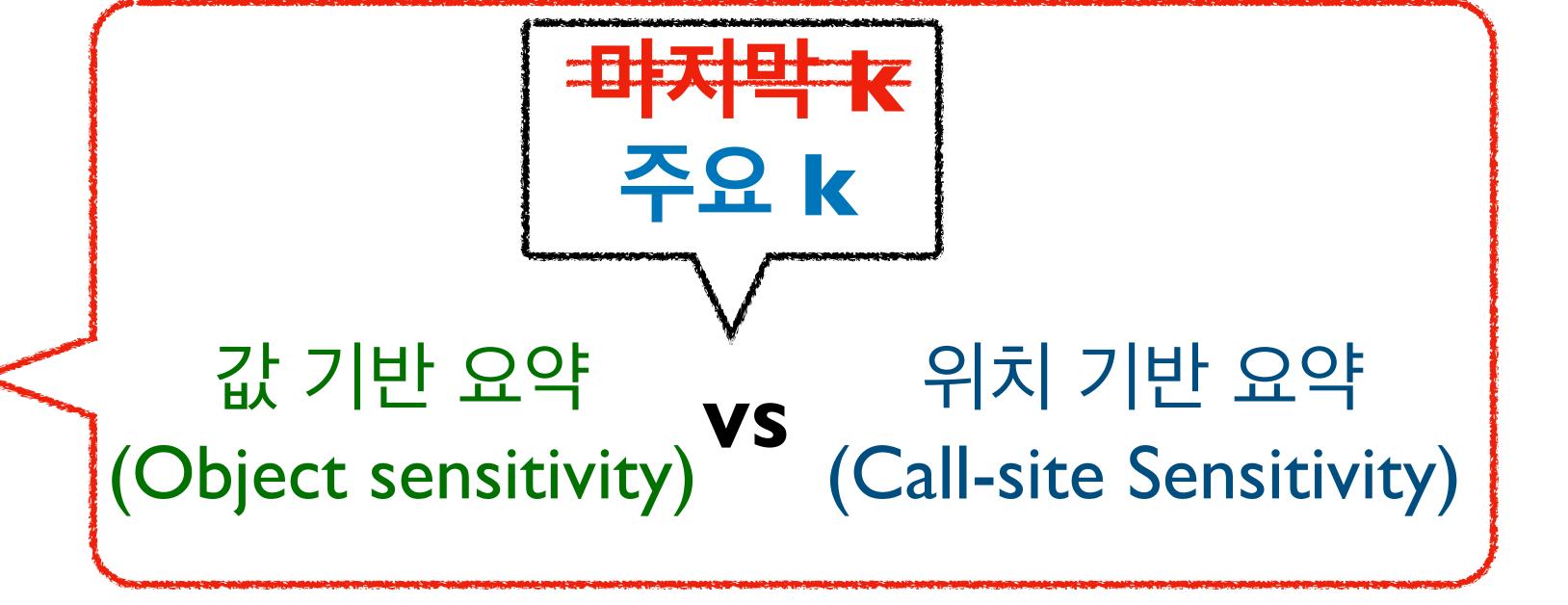
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-Smaragdakis and Balatsouras [2015]

Context sensitivity is critically important for static program analysis of object-oriented programs. A context-sensitive analysis associates local variables and heap objects with context information of method calls, computing analysis results separately for different contexts. This way, context sensitivity prevents analysis information from being merged along different call chains. For object-oriente

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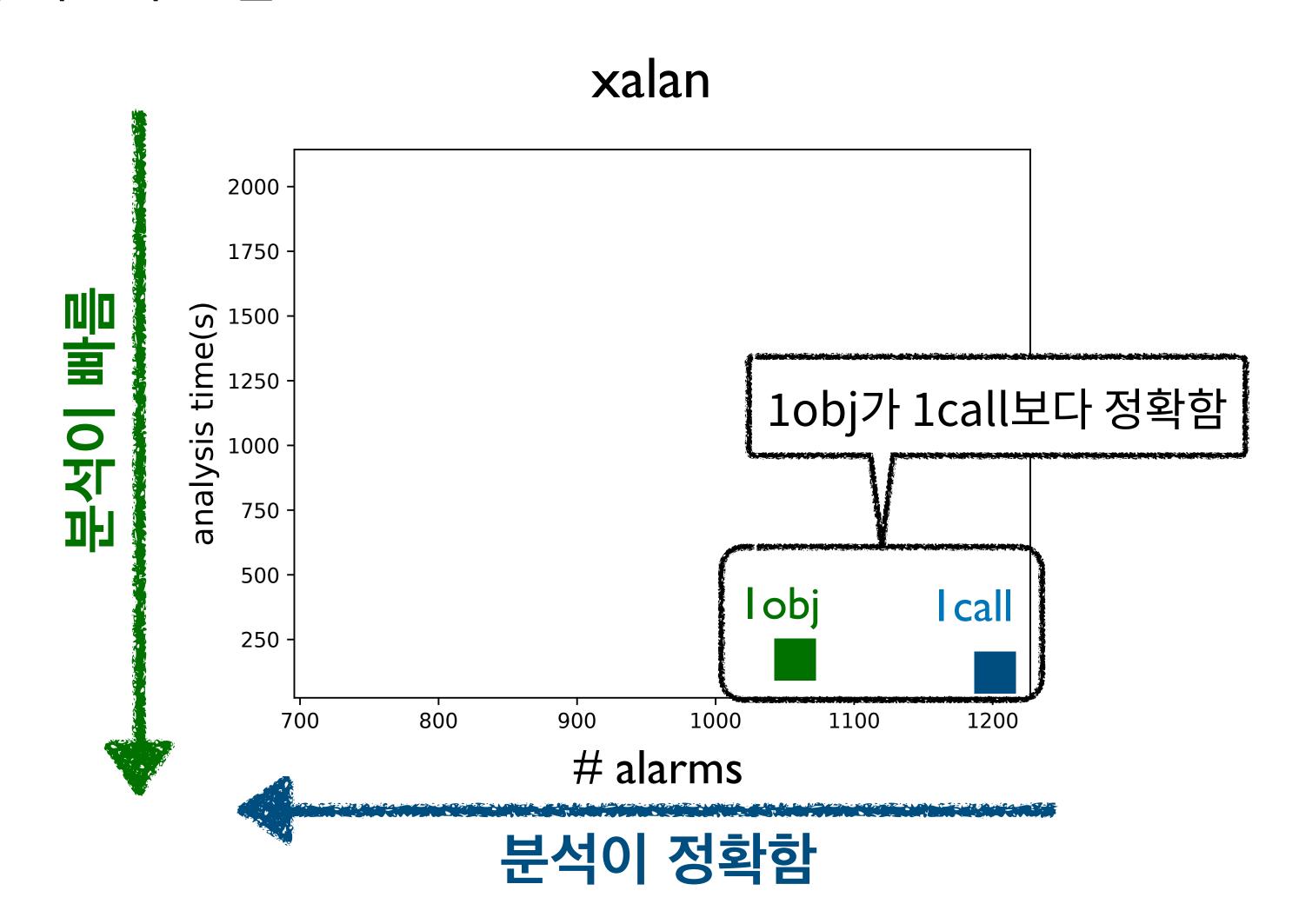
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2018 2022

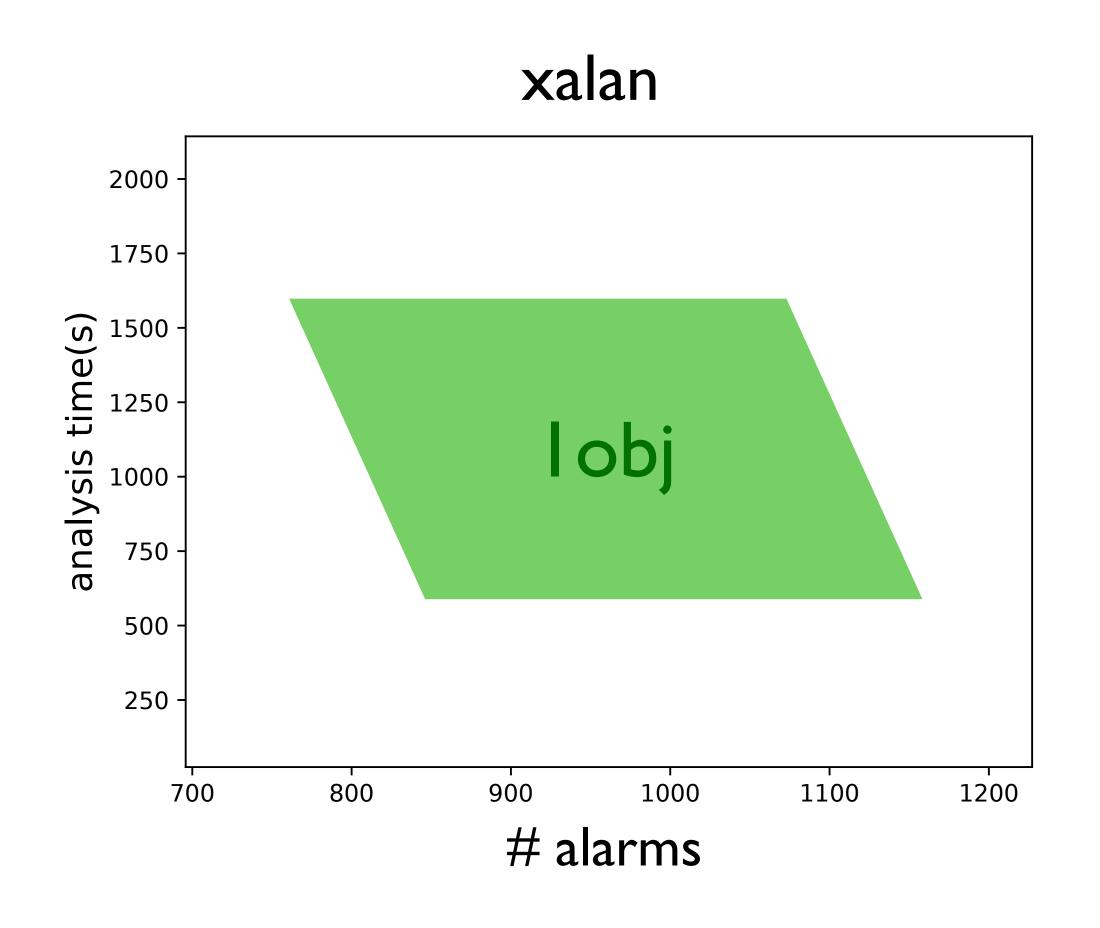
마지막 k 기반 요약에서의 성능 비교

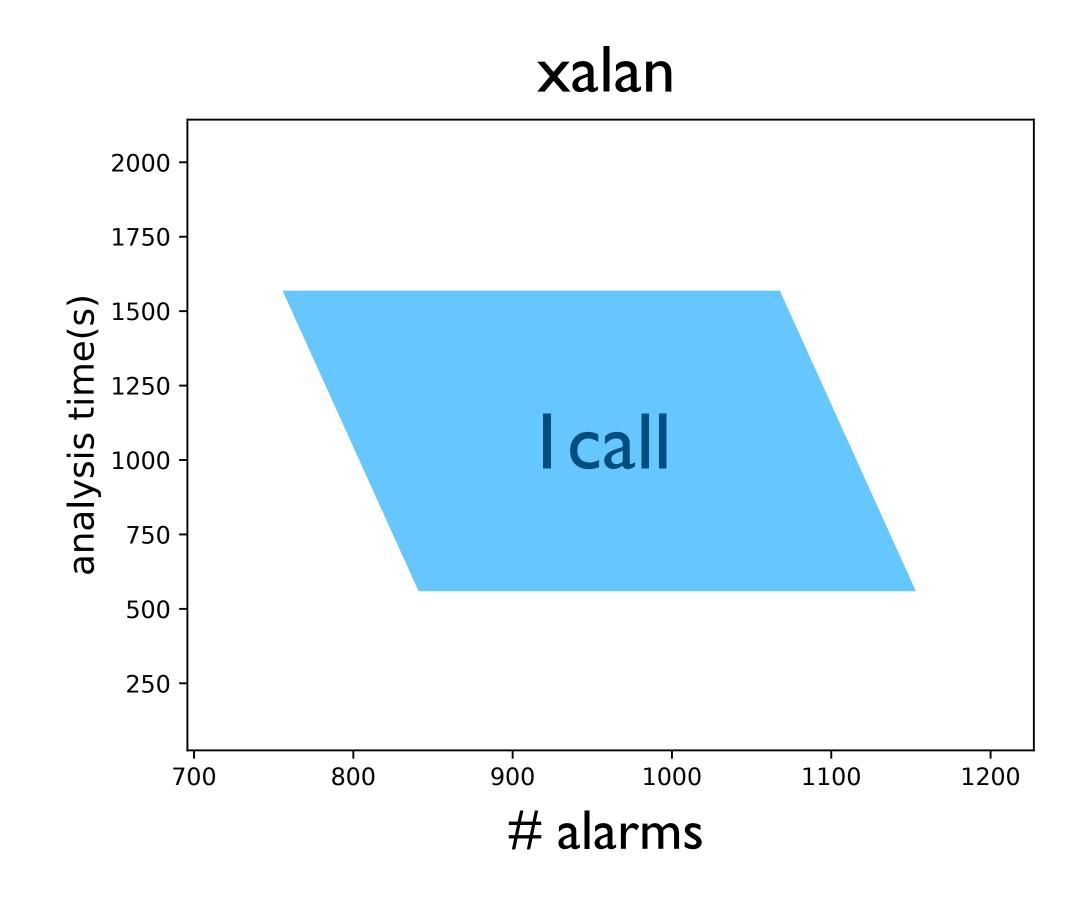
• 분석의 성능을 직접 비교하면 됨



주요 k 기반에서의 성능 비교

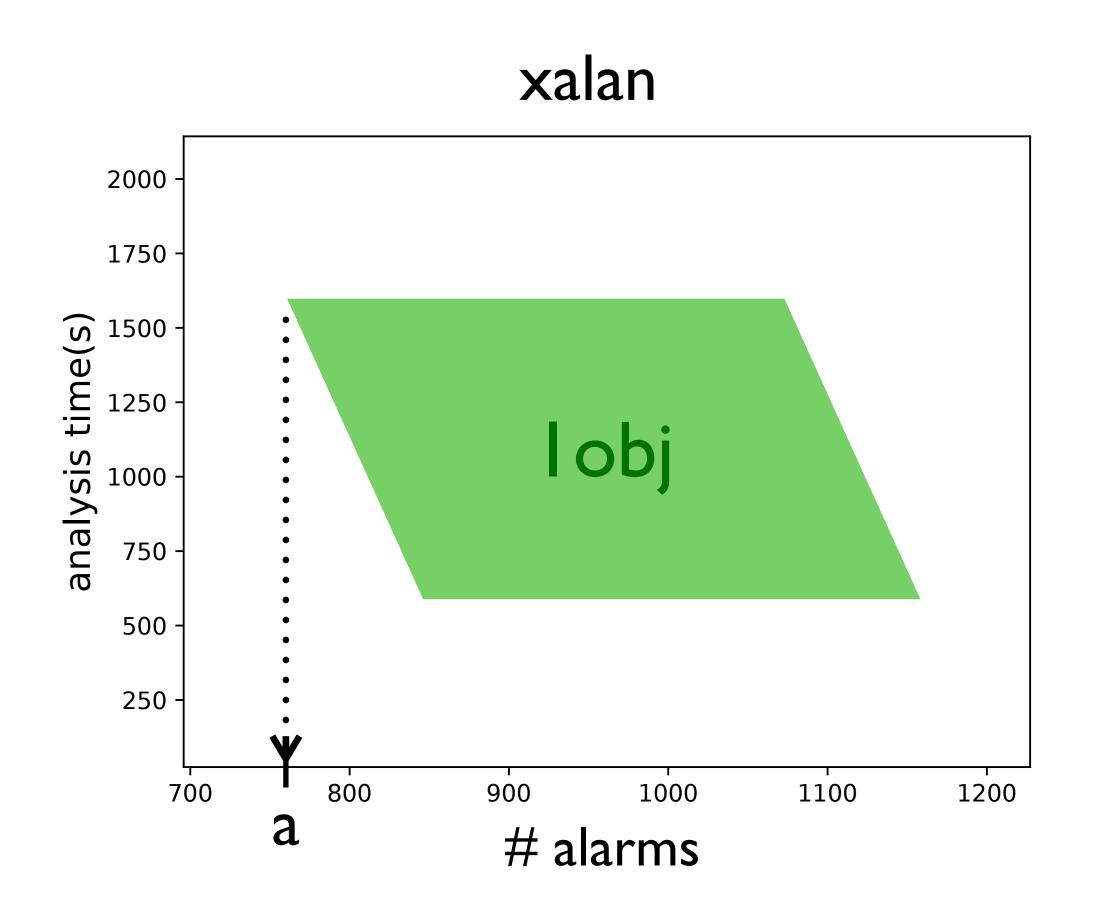
• 주요 요소 분류에 따라 성능이 바뀜

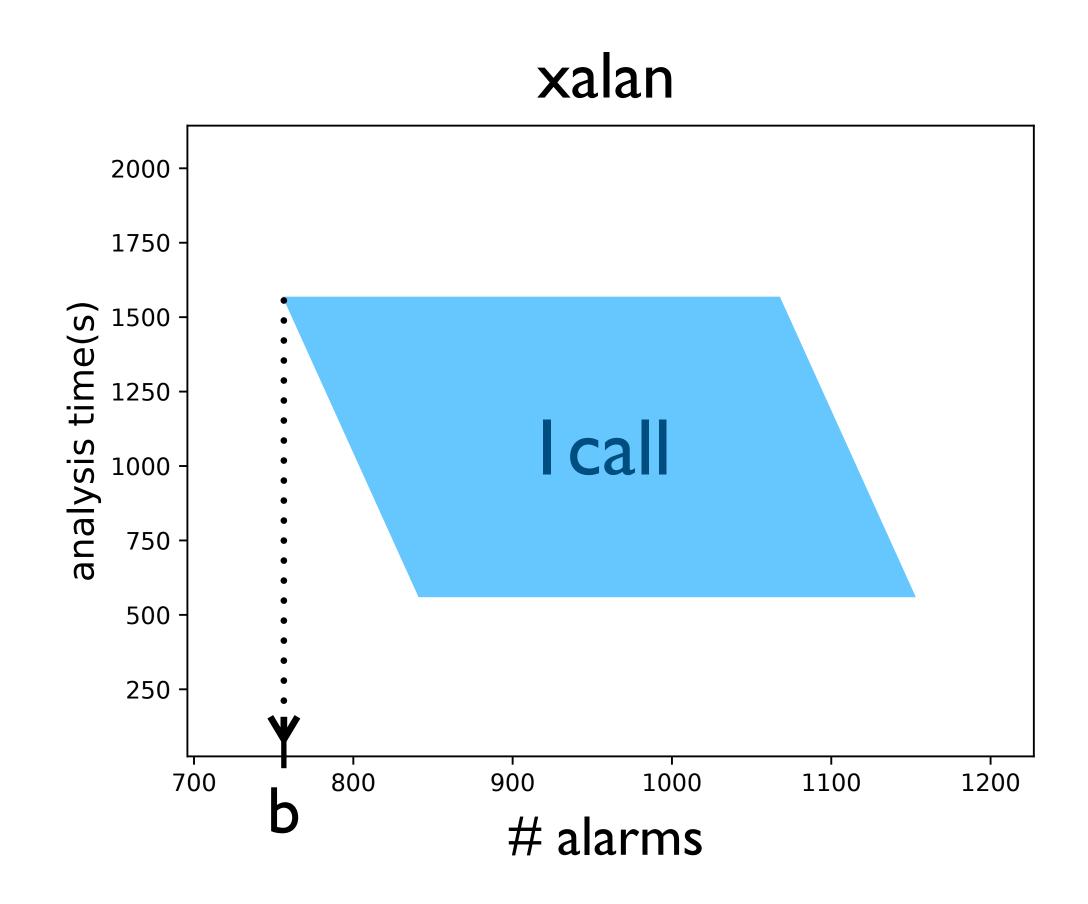




주요 k 기반에서의 성능 비교

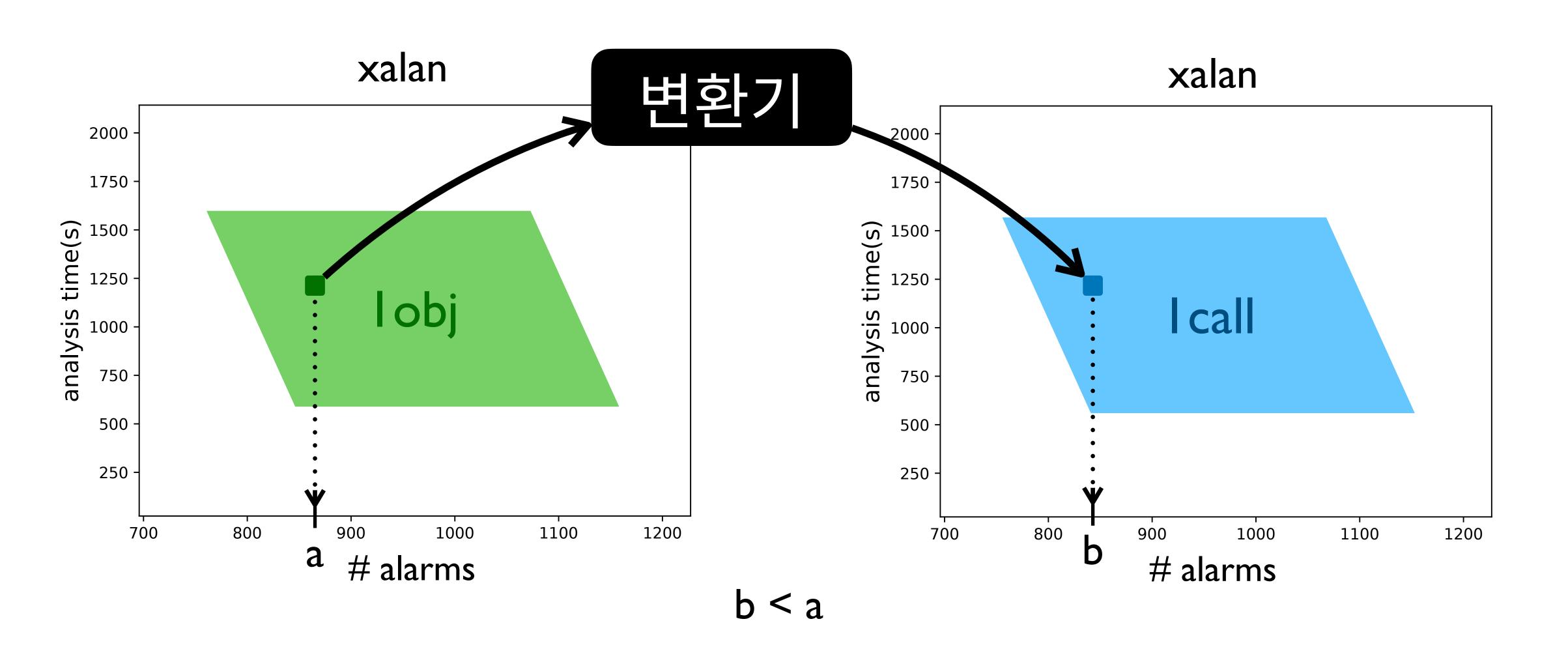
• **방법 1:** 최고 성능을 내는 분류를 알아내서 성능 비교하기 (e.g., b < a)





주요 k 기반에서의 성능 비교

• 방법 2: 주어진 obj를 더 정확한 call로 변환해주는 함수가 존재한다는 것을 보이기



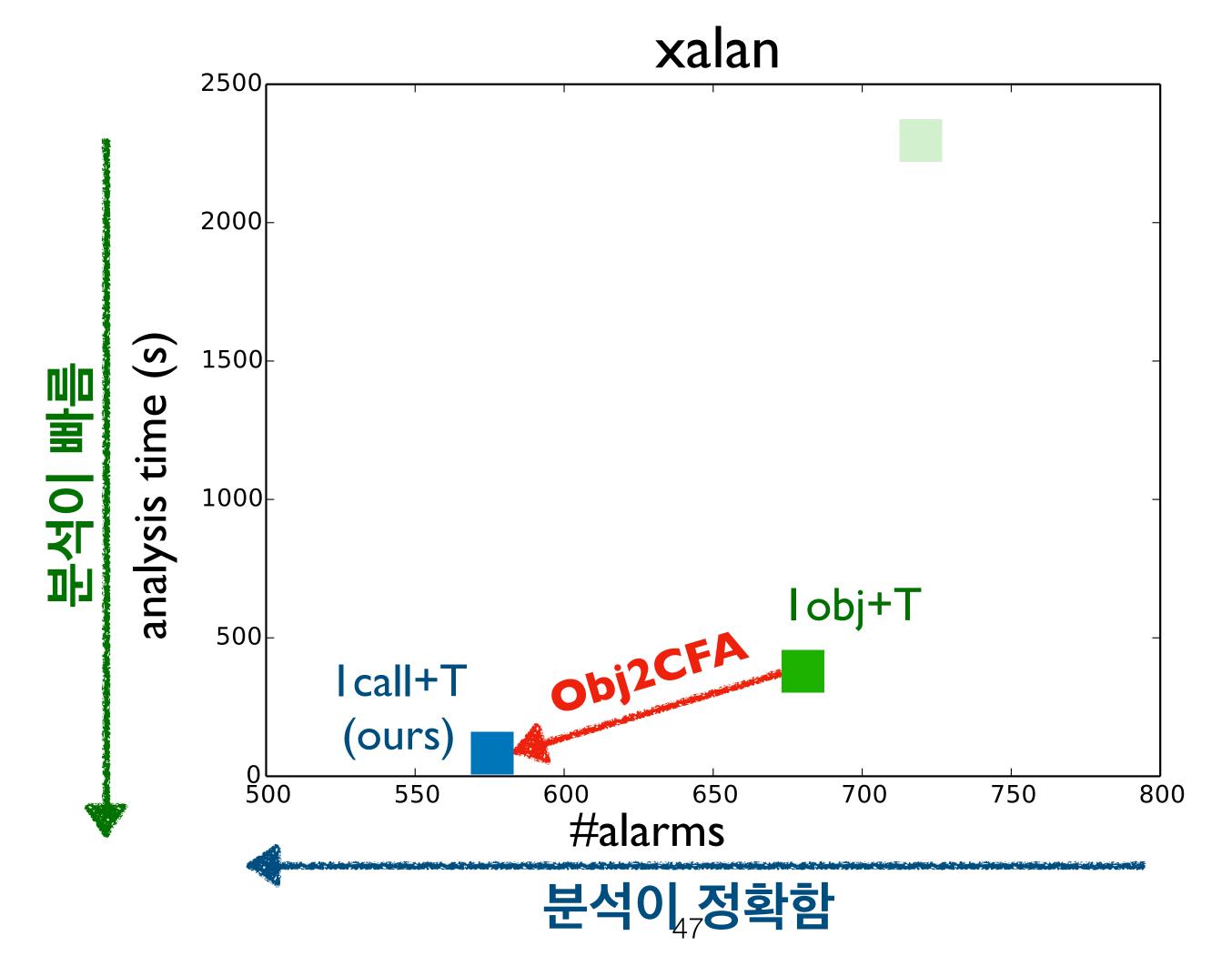
변환기: Obj2CFA

• Obj2CFA 는 주어진 값 기반 요약을 더 정확한 위치 기반 요약으로 바꾸어주는 함수



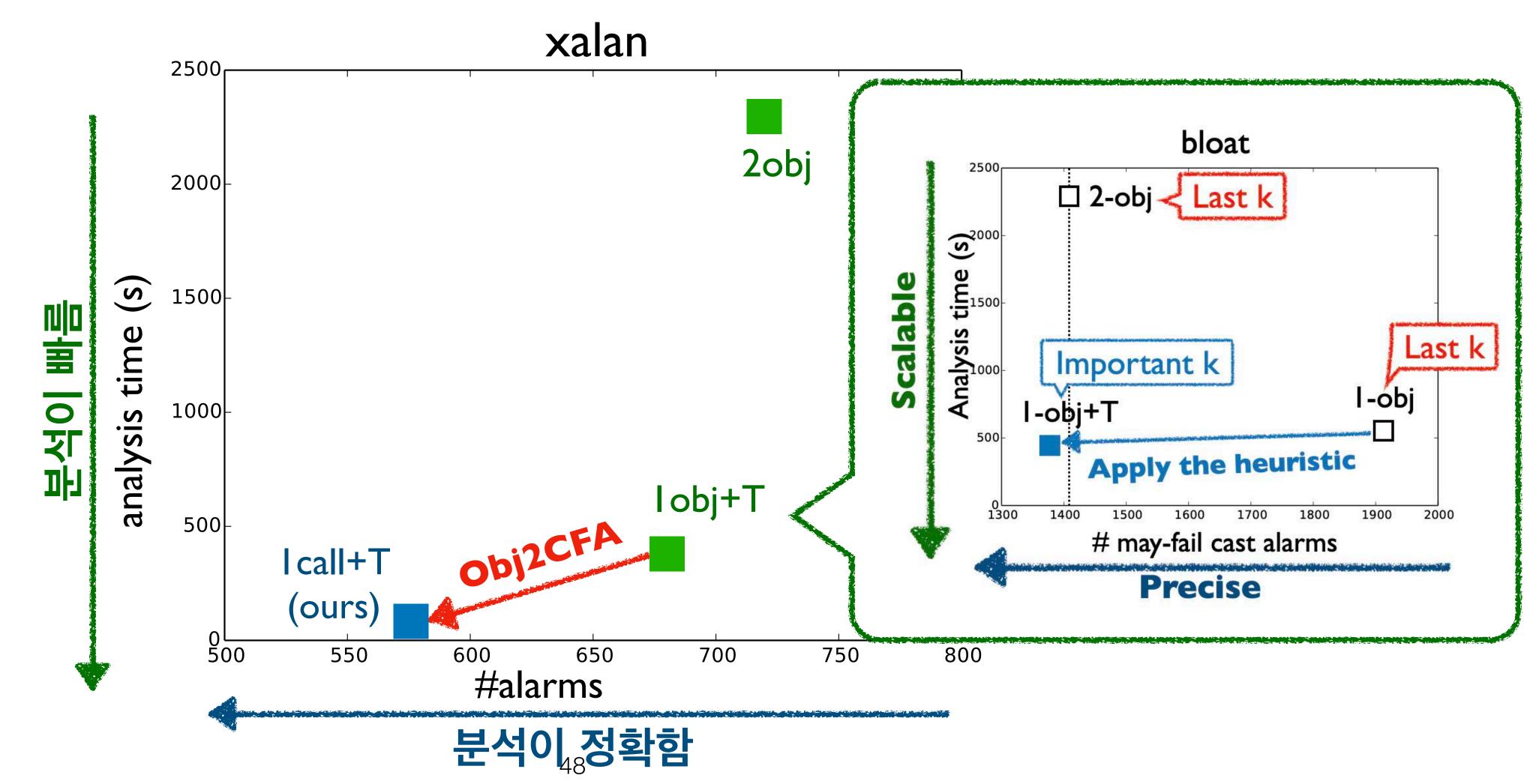
변환기: Obj2CFA

• Obj2CFA 는 주어진 값 기반 요약을 더 정확한 위치 기반 요약으로 바꾸어줌



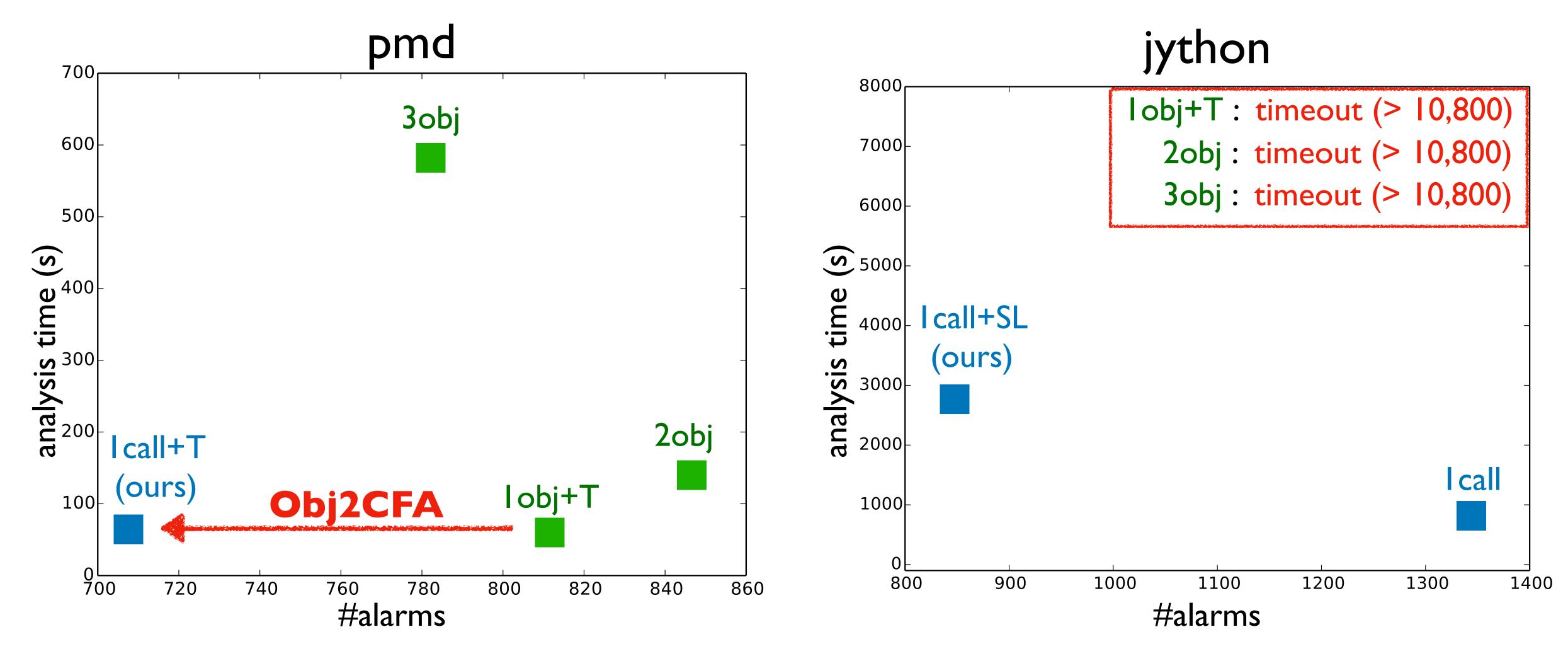
변환기: Obj2CFA

• Obj2CFA 는 주어진 값 기반 요약을 더 정확한 위치 기반 요약으로 바꾸어줌



위치 기반 요약 vs 값 기반 요약

● 변환된 위치 기반 요약은 현존하는 값 기반 요약들보다 높은 정확도와 속도를 보임



Some parts of the paper is too strong; this paper should be rejected. - A reviewer [Expert] POPL should accept this paper to encourage discussions. - A reviewer [Expert] **ICSE 2020** OOPSLA2019 **PLDI 2020** OOPSLA 2021 **POPL 2022** (Rejected) (Rejected) (Rejected) (Rejected) (Accepted)

논문 출판후

Call-Site vs. Object Sensitivity

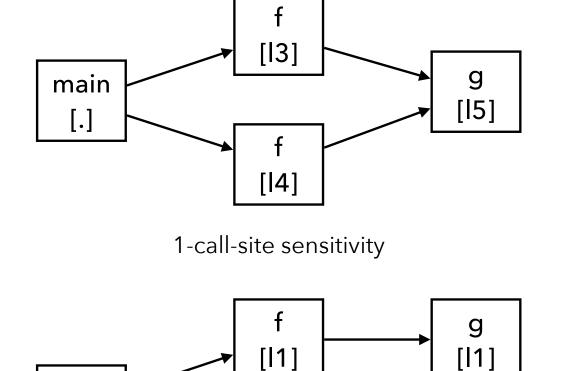
- In theory, their precision is incomparable
- In practice, object sensitivity generally outperforms call-site sensitivity for OO languages (like Java)

Call-site vs. Object Sensitivity

Typical example that benefits from object sensitivity:

```
class A:
    def g(self):
        return
    def f(self):
        return self.g() // 15

def main():
    a = A() // 11
    b = A() // 12
    a.f() // 13
    b.f() // 14
```



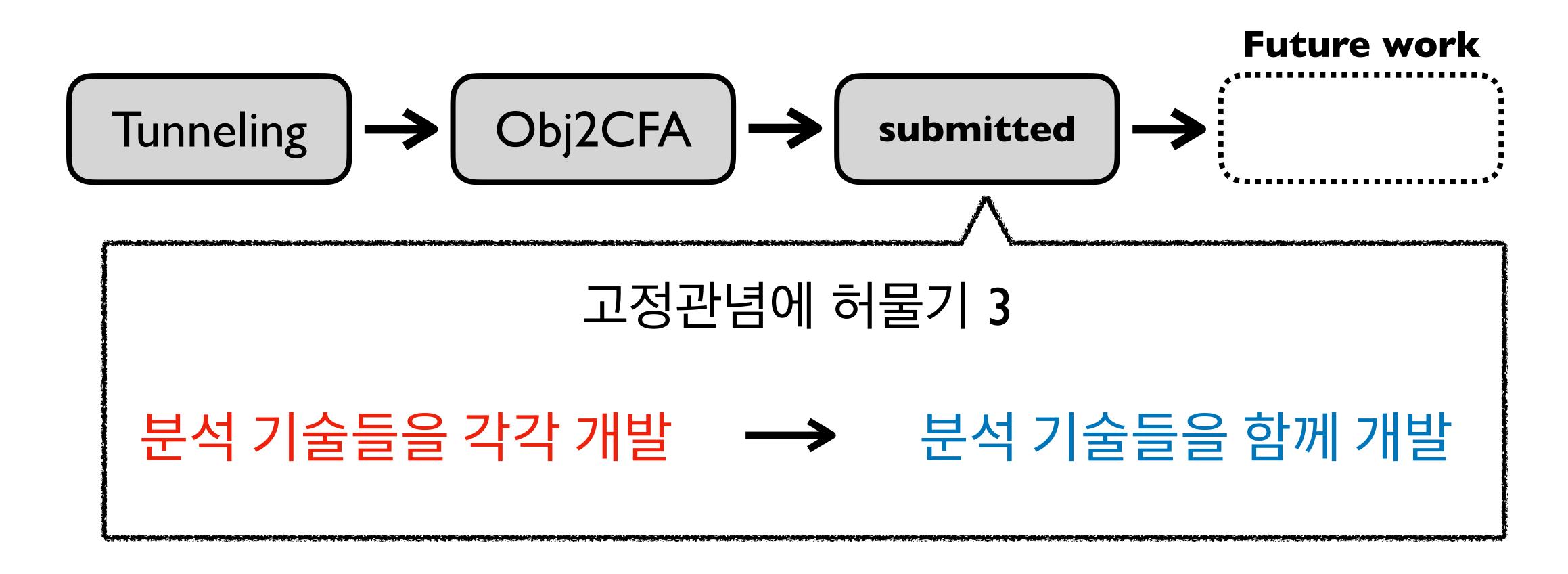
1-object sensitivity

main

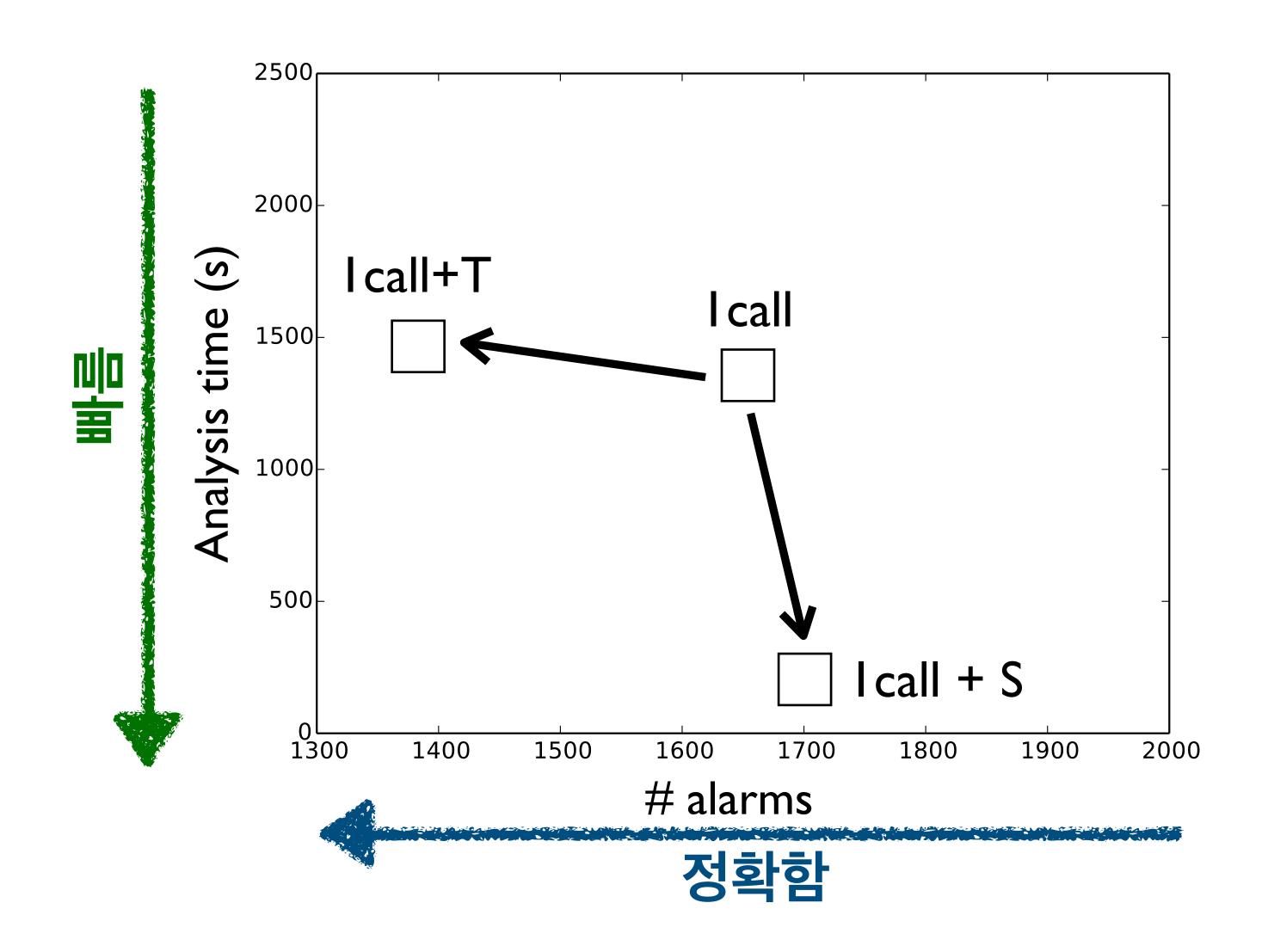
Tian Tan @ Nanjing University

고정관념에 도전하기

• 목표: 주요 k기반 요약 방식을 표준으로 만들기

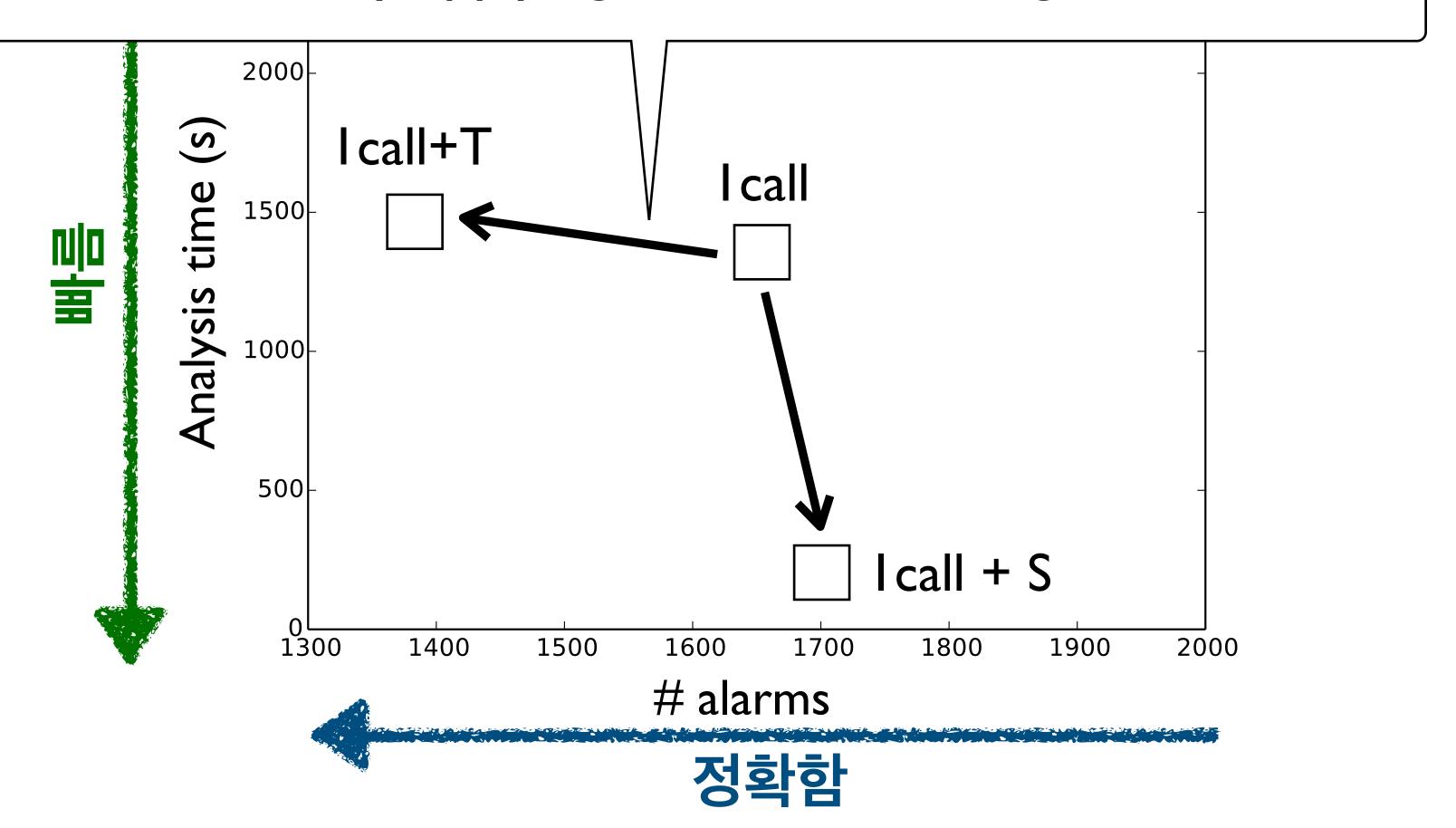


- 호출 환경 배달하기: 속도를 유지한채 정확도를 올려주는 기술
- 적당히 함수 호출 분석 (selective ctx sensitivity): 정확도를 유지한채 속도를 올려주는 기술

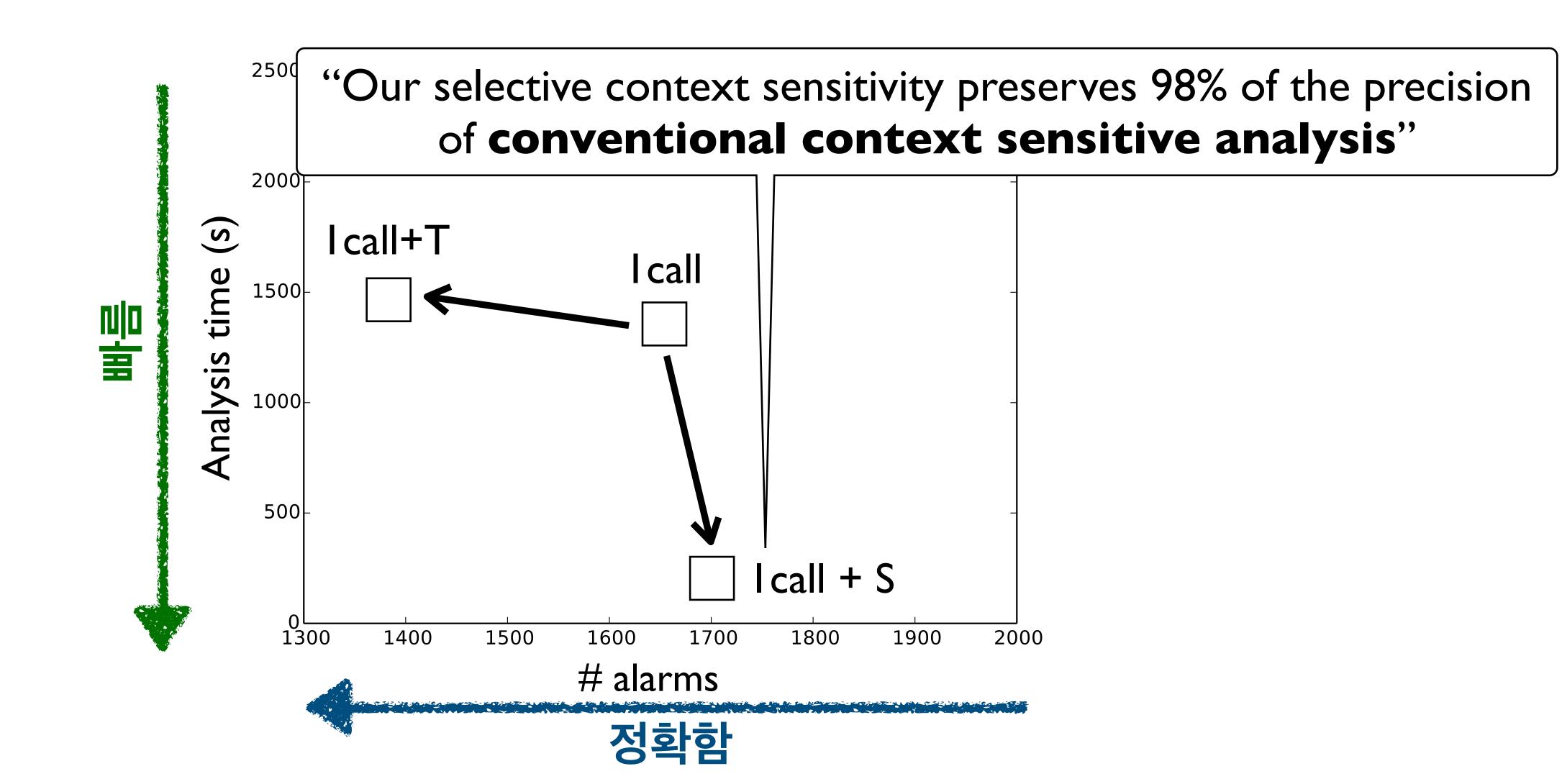


• 호출 환경 배달하기: 속도를 유지한채 정확도를 올려주는 기술

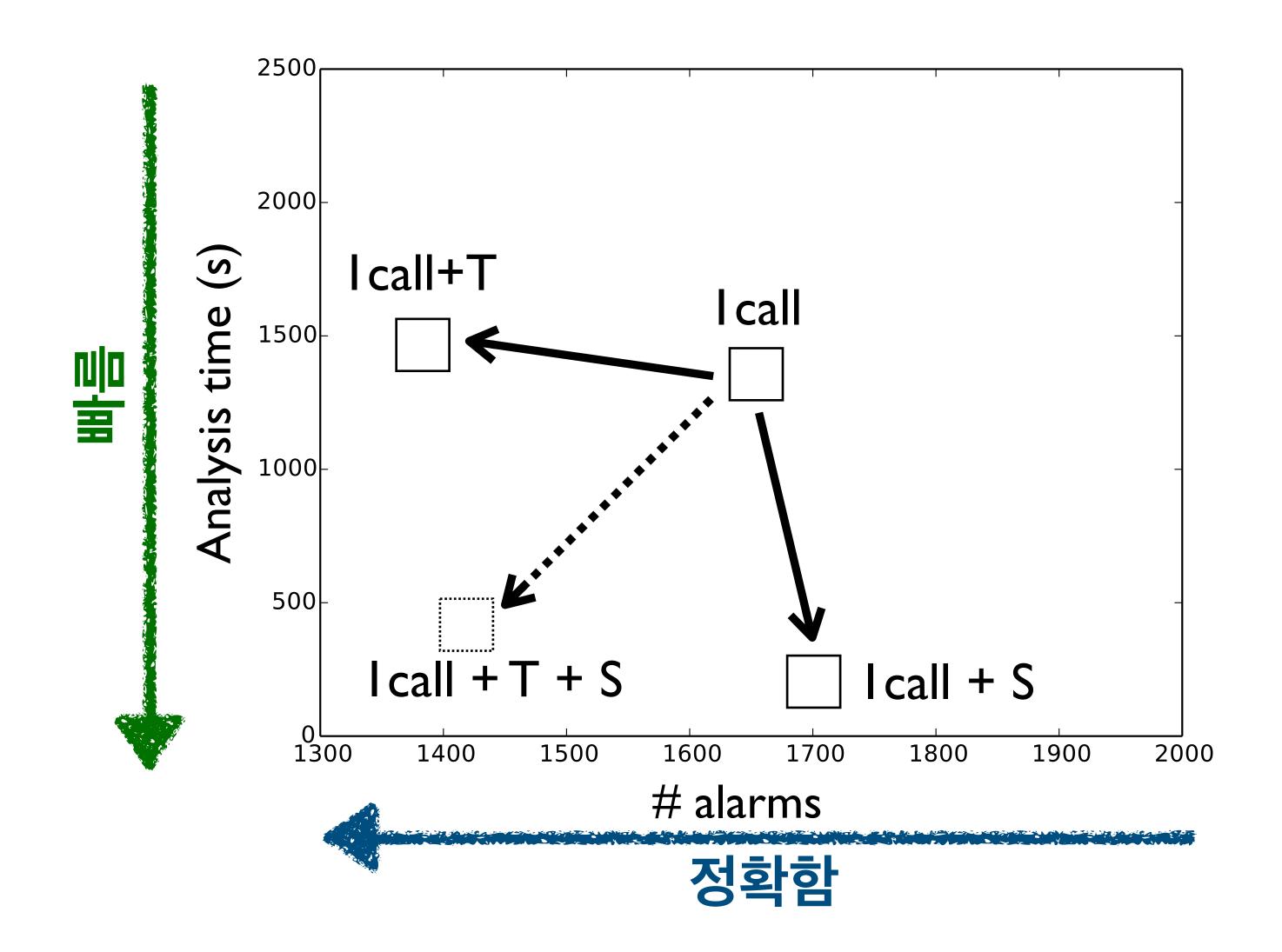
"We generated I call+T by applying context tunneling to I call..."



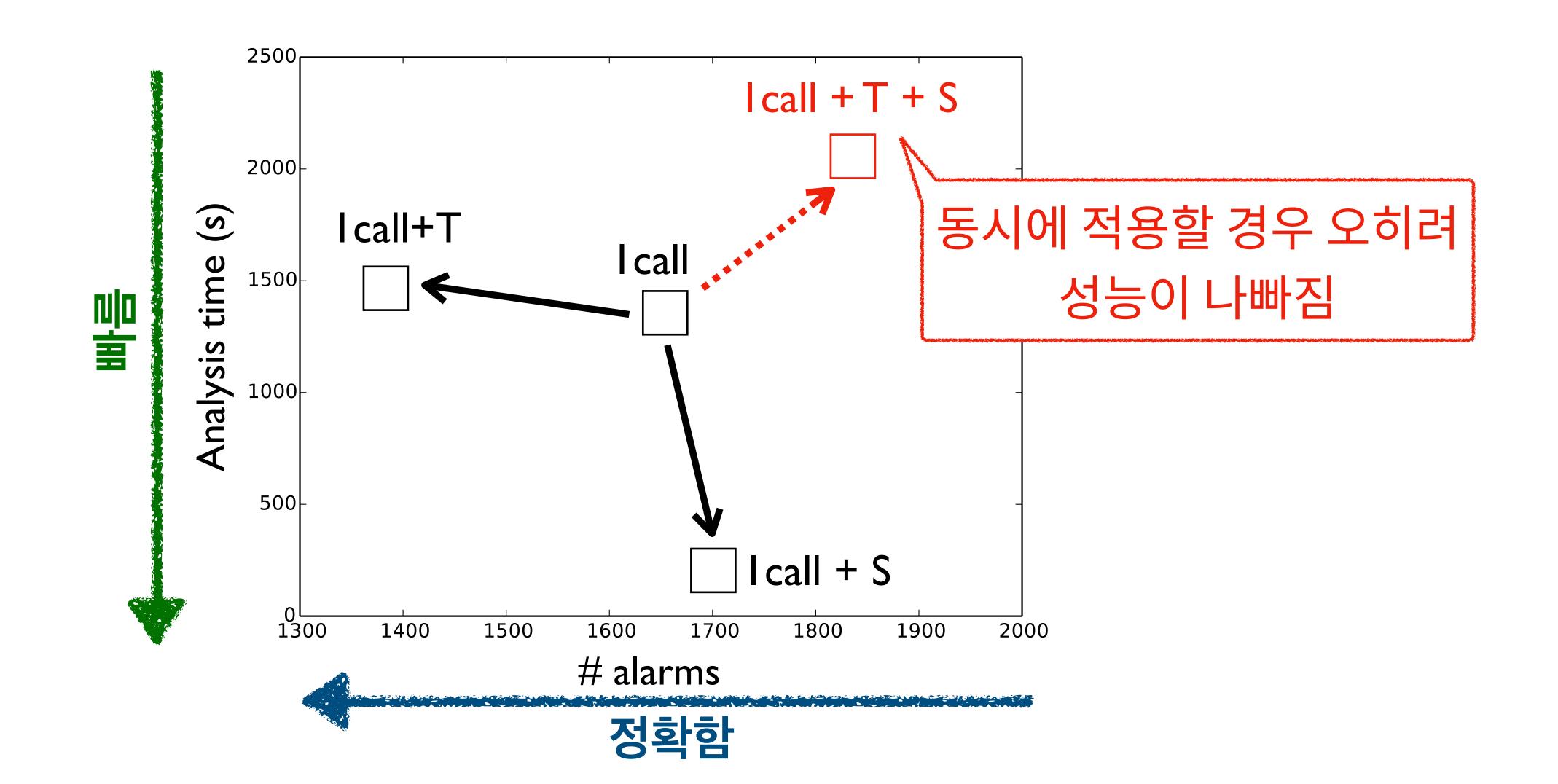
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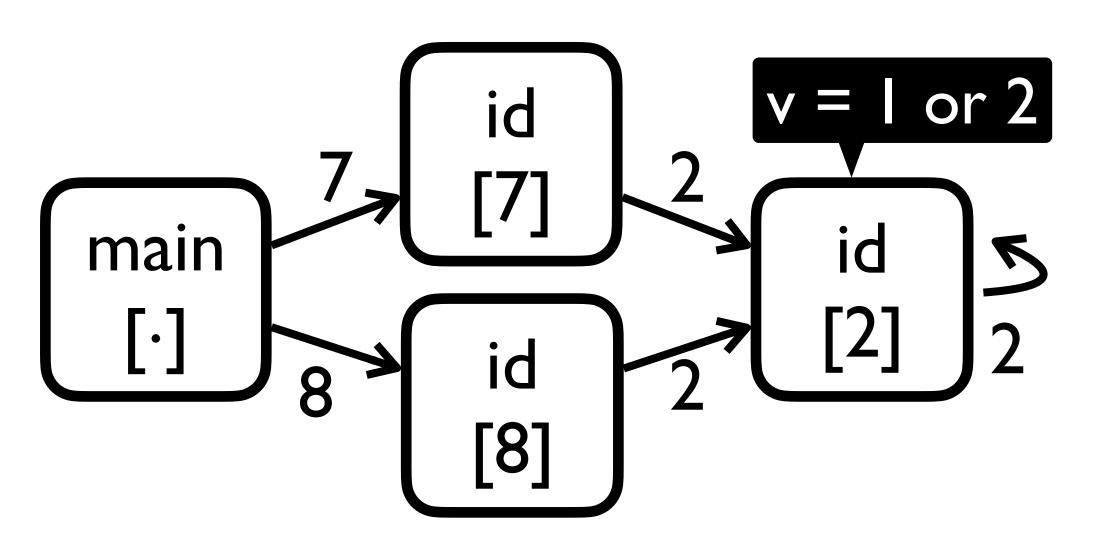
● 질문: 독립적으로 각각 개발한 기술들을 동시에 사용하면 궁극의 성능이 나올까?



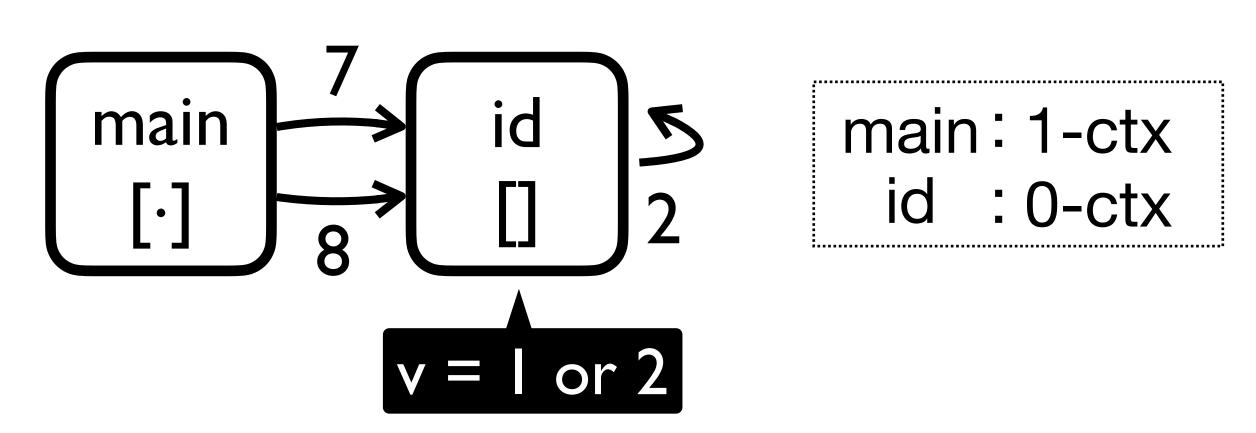
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```
0: id(v, i){
   if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
7: vI = id(I, i); //A
   v2 = id(2, i);//B
    assert (vI != v2);//query
10: }
    예제 프로그램
```

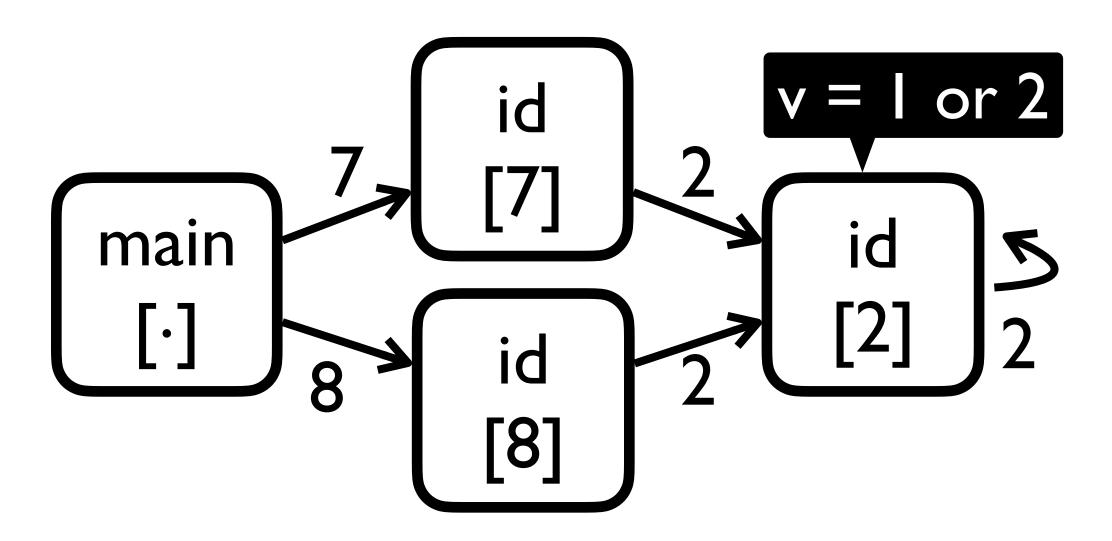


I-요소 기반 함수 호출 요약

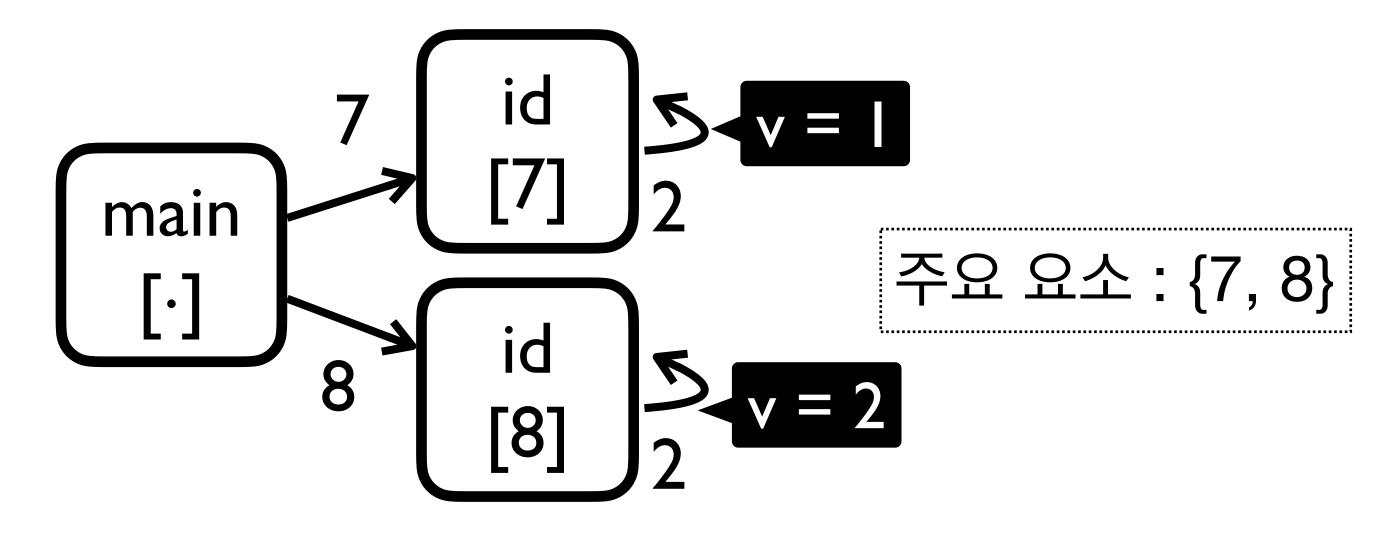


적당히 I-요소 기반 함수 호출 요약

```
0: id(v, i){
  if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
7: vI = id(I, i);//A
   v2 = id(2, i);//B
    assert (vI != v2);//query
10: }
    예제 프로그램
```

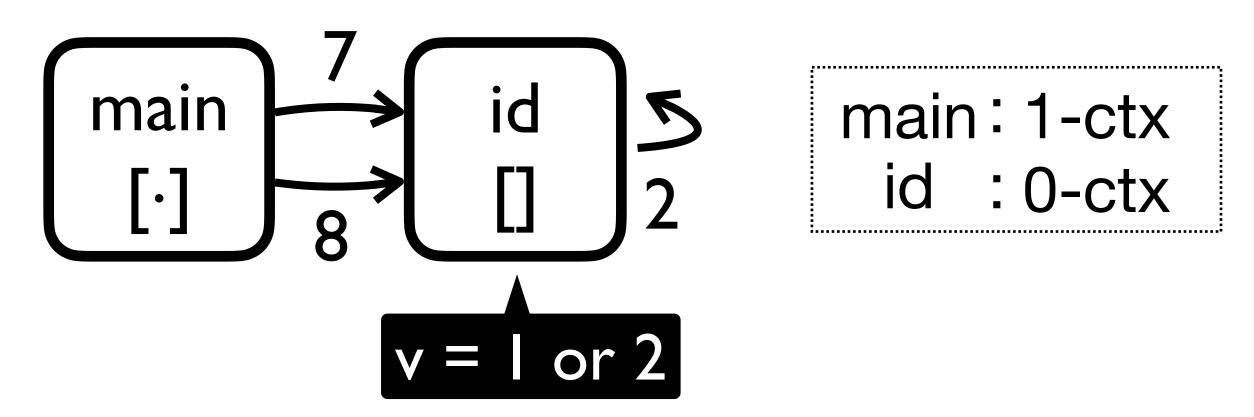


I-요소 기반 함수 호출 요약

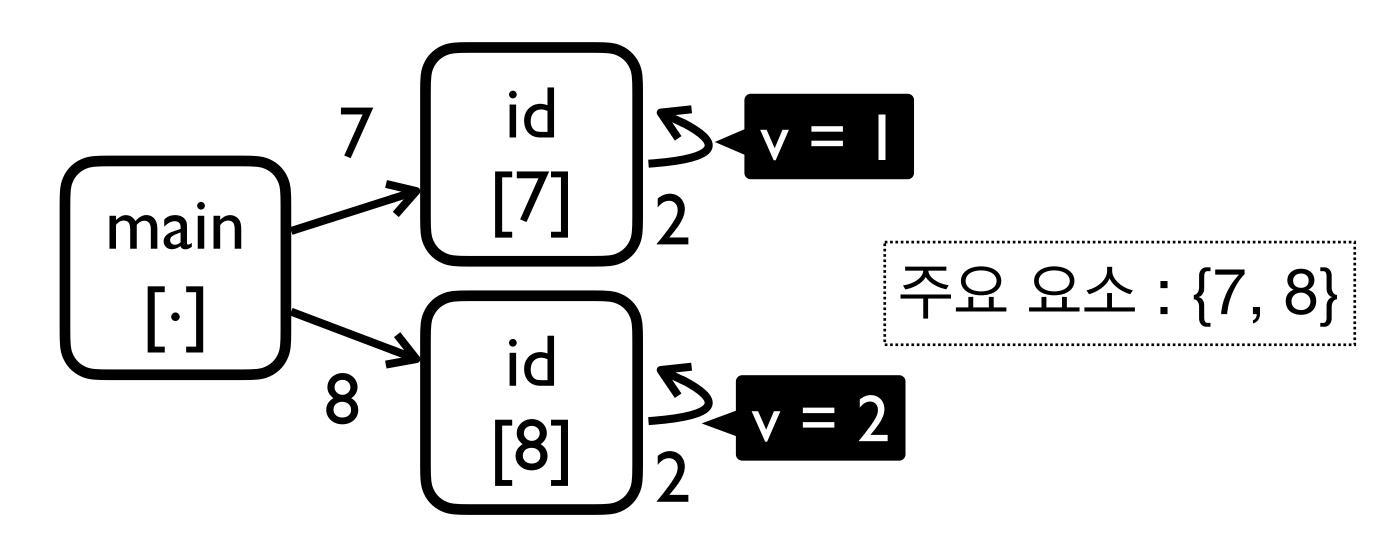


주요 I-요소 기반 함수 호출 요약

```
0: id(v, i){
   if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
   vI = id(I, i);//A
   v2 = id(2, i);//B
    assert (vI != v2);//query
10: }
    예제 프로그램
```

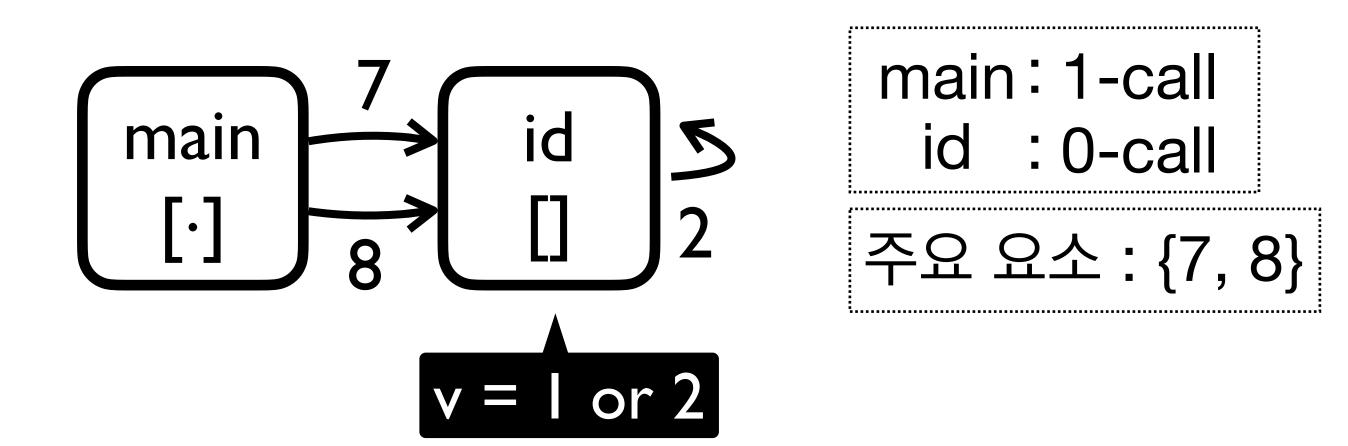


적당히 I-요소 기반 함수 호출 요약



주요 1-요소 기반 함수 호출 요약

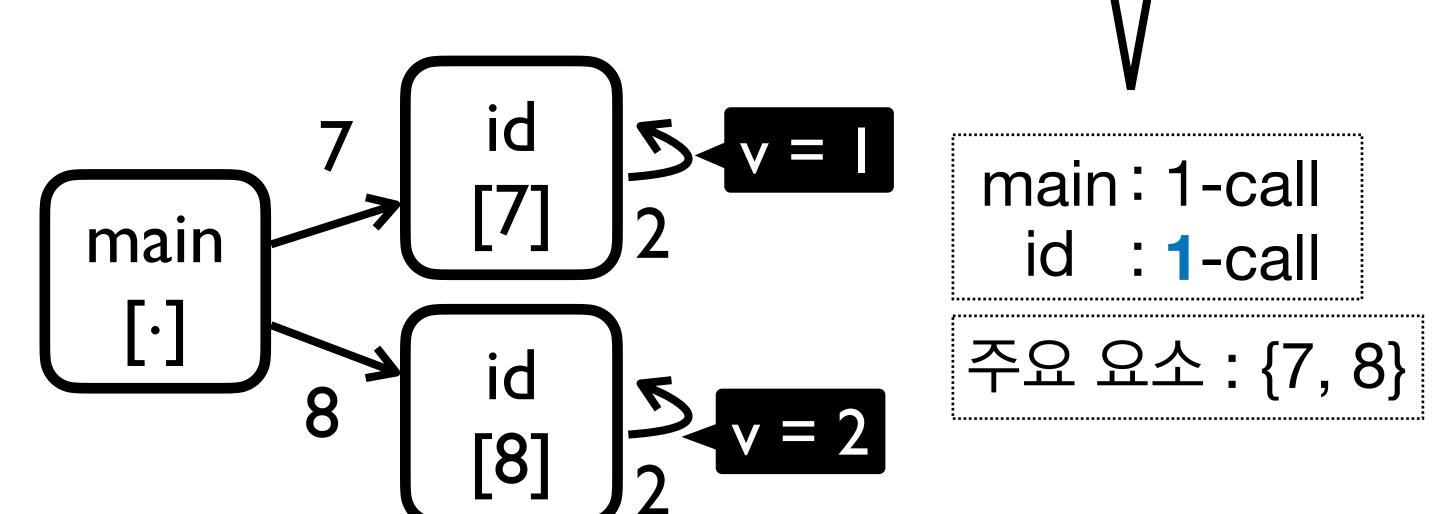
```
0: id(v, i){
   if (i > 0){
    return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
7: vI = id(I, i);//A
   v2 = id(2, i);//B
   assert (vI != v2);//query
9:
10: }
    예제 프로그램
```



적당히 주요 I-요소 기반 함수 호출 요약

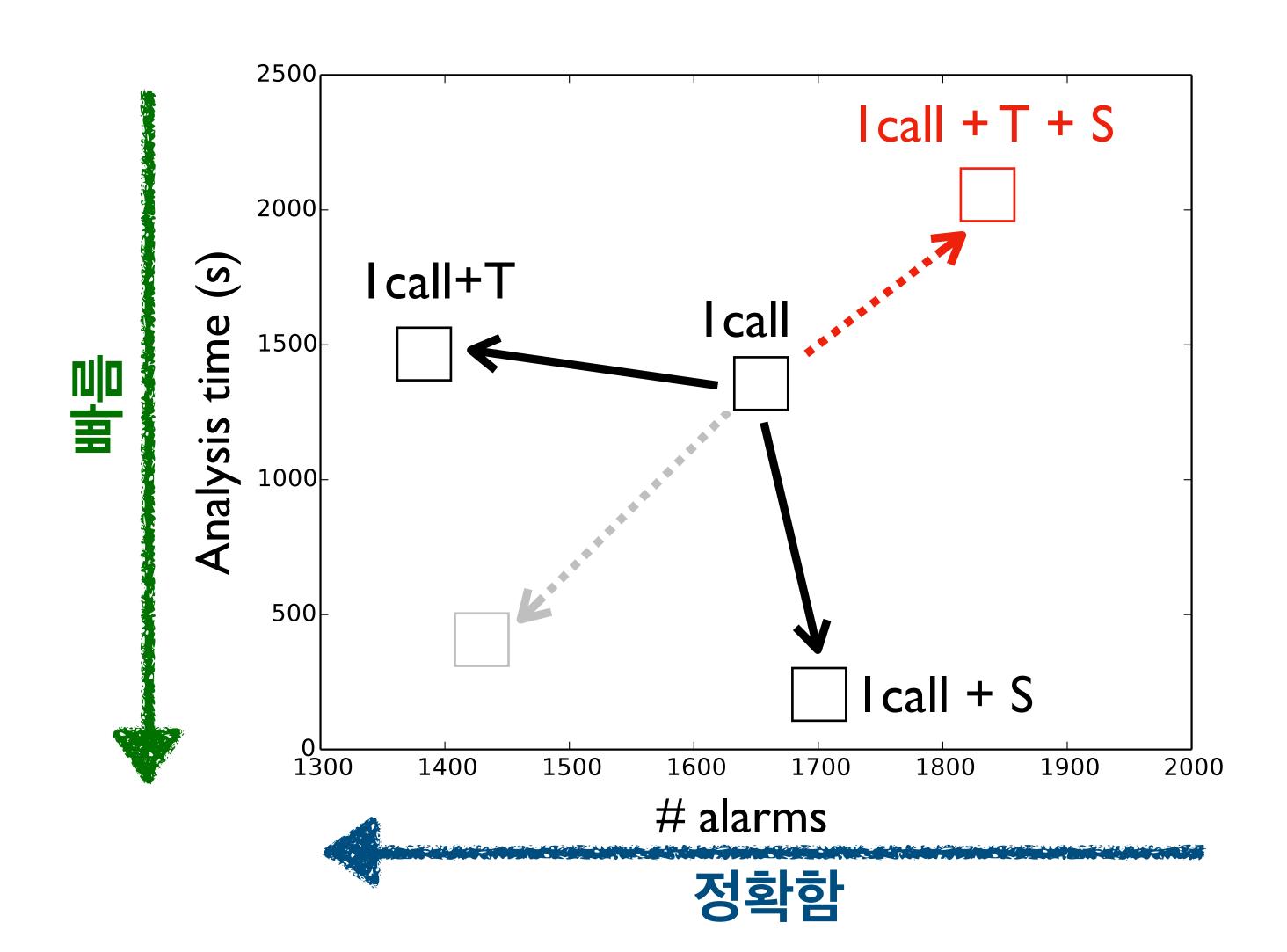
```
0: id(v, i){
   if (i > 0){
     return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
   vI = id(I, i);//A
   v2 = id(2, i);//B
    assert (vl != v2);//query
10: }
    예제 프로그램
```

같이 사용될 것을 고려해 분류해야 함

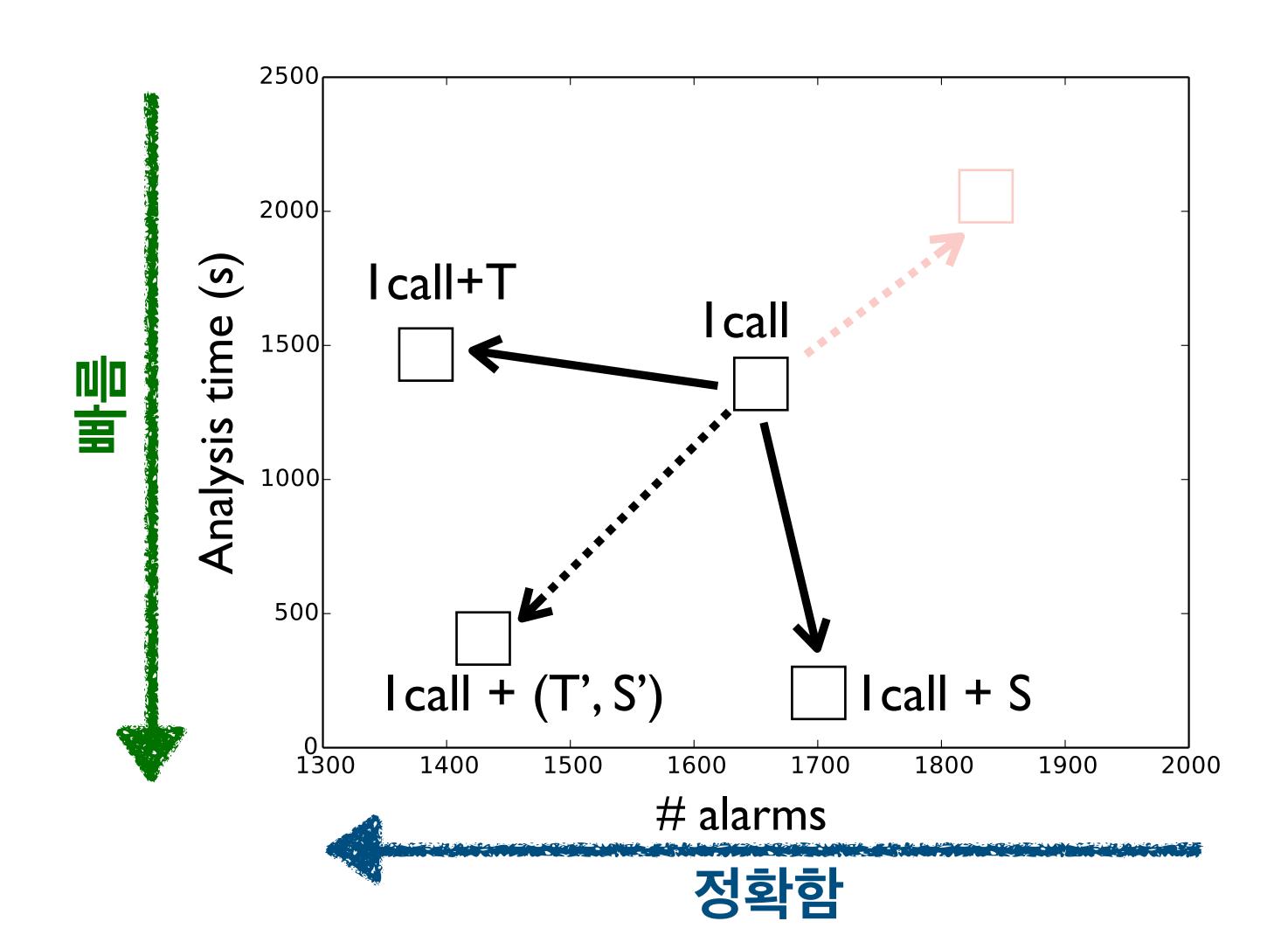


적당히 주요 1-요소 기반 함수 호출 요약

● 연구 트렌드를 따라 독립적으로 각각 개발한 기술들을 동시에 사용하면 성능이 오히려 나빠짐



• 궁극의 성능을 내기 위해선 서로가 미칠 영향을 고려해 동시에 만들어야 함



• 궁극의 성능을 내기 위해선 서로가 미칠 영향을 고려해 동시에 만들어야 함

Marriage of Context Tunneling and Selective Context Sensitivity in Pointer Analysis

ANONYMOUS AUTHOR(S)

In this paper, we identify a fundamental issue in the current trend of developing context sensitivity techniques in pointer analysis and present a way to efficiently address it. Context sensitivity is a key factor that significantly affects the performance of pointer analysis in object-oriented programs. In the literature, two major refinements—context tunneling and selective context sensitivity—have been developed, where context tunneling improves precision and selective context sensitivity enhances scalability. Though the two techniques can be used together to maximize both precision and scalability, they have been developed independently without considering whether individually optimized techniques will remain effective when combined. In this work, however, we demonstrate that combining independently developed context tunneling and selective context sensitivity techniques leads to suboptimal performance. To be an effective combination, the two techniques must be developed together, considering their interdependencies. Developing a pair of techniques, however, while accounting for all possible interactions is extremely challenging. To address this challenge, we present a framework that significantly reduces the complexity of developing an effective combination of the two techniques. Our evaluation results show that following our approach leads to the development of an effective combination, achieving a state-of-the-art performance, that outperforms combinations of independently developed context tunneling and selective context sensitivity techniques.

ACM Reference Format

1 INTRODUCTION

Context sensitivity plays a pivotal role in pointer analysis of object-oriented programs. It enhances precision by distinguishing between multiple invocations of the same method based on their calling contexts. However, tracking every possible context is impractical, leading to the widespread use of *k*-limited context sensitivity. This approach retains only the *k* most recent context elements—typically call sites in call-site sensitivity [Sharir and Pnueli 1981] or allocation sites in object sensitivity [Milanova et al. 2002]. Despite its adoption, this conventional technique frequently falls short in balancing precision and scalability in real-world applications.

Over the past decade, numerous techniques have been proposed to enhance the *k*-limited approach in context-sensitive pointer analysis [He et al. 2024; Jeon et al. 2018; Jeon and Oh 2022; Kastrinis and Smaragdakis 2013; Li et al. 2018a,b, 2020; Liang et al. 2011; Lu et al. 2021a,b; Milanova et al. 2002; Oh et al. 2015; Smaragdakis et al. 2011, 2014; Tan et al. 2021, 2017; Zhang et al. 2014]. Two prominent approaches that excel in maximizing precision or scalability are:

Context tunneling [Jeon et al. 2018; Jeon and Oh 2022] seeks to maximize precision while
adhering to a k-context limit. Instead of relying solely on the k most recent context elements,
it adopts a more flexible strategy by prioritizing the k most significant context elements.
Jeon and Oh [2022] demonstrated that context tunneling can markedly improve analysis

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0004-5411/2018/8-ART111 \$15.00

https://doi.org/XXXXXXXXXXXXXXXX

분석 기술들을 각각 개발

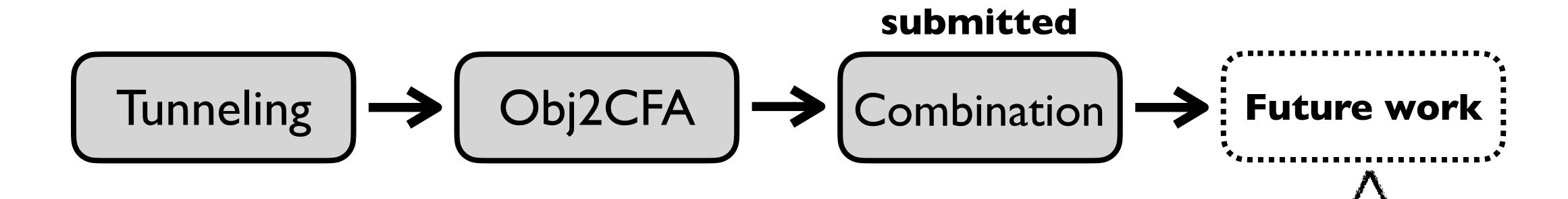
• We identify a fundamental issue in the current trend of developing context sensitivity techniques in pointer analysis and present a way to efficiently address it.

분석 기술들을 동시에 개발하는 법

• We present a framework that significantly reduces the complexity of developing an effective combination of the two techniques

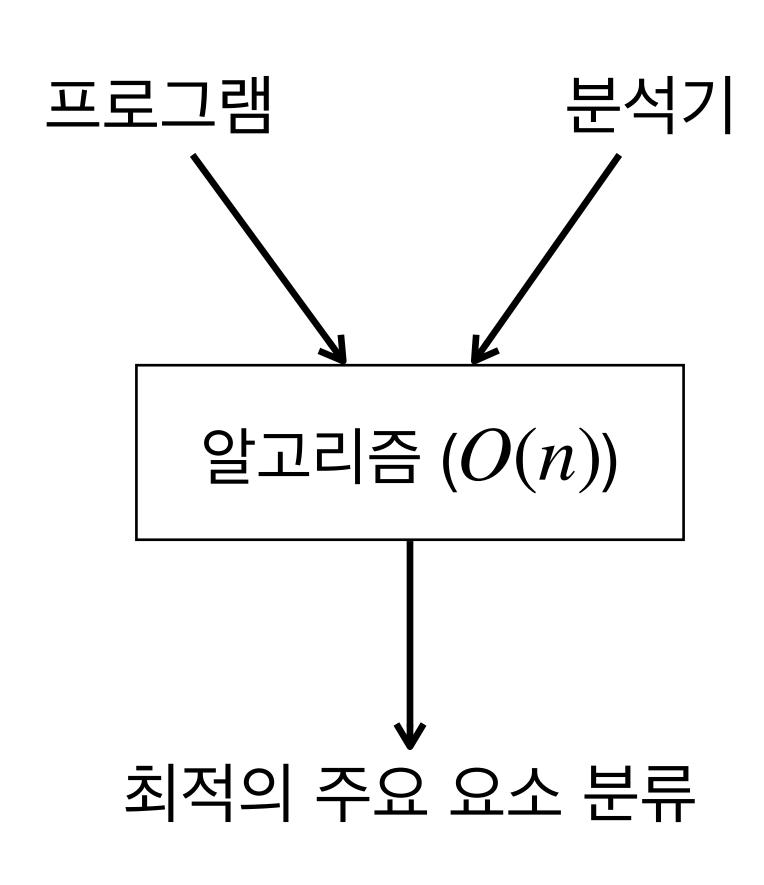
컨텍스트 터널링: 고정관념에 도전하기

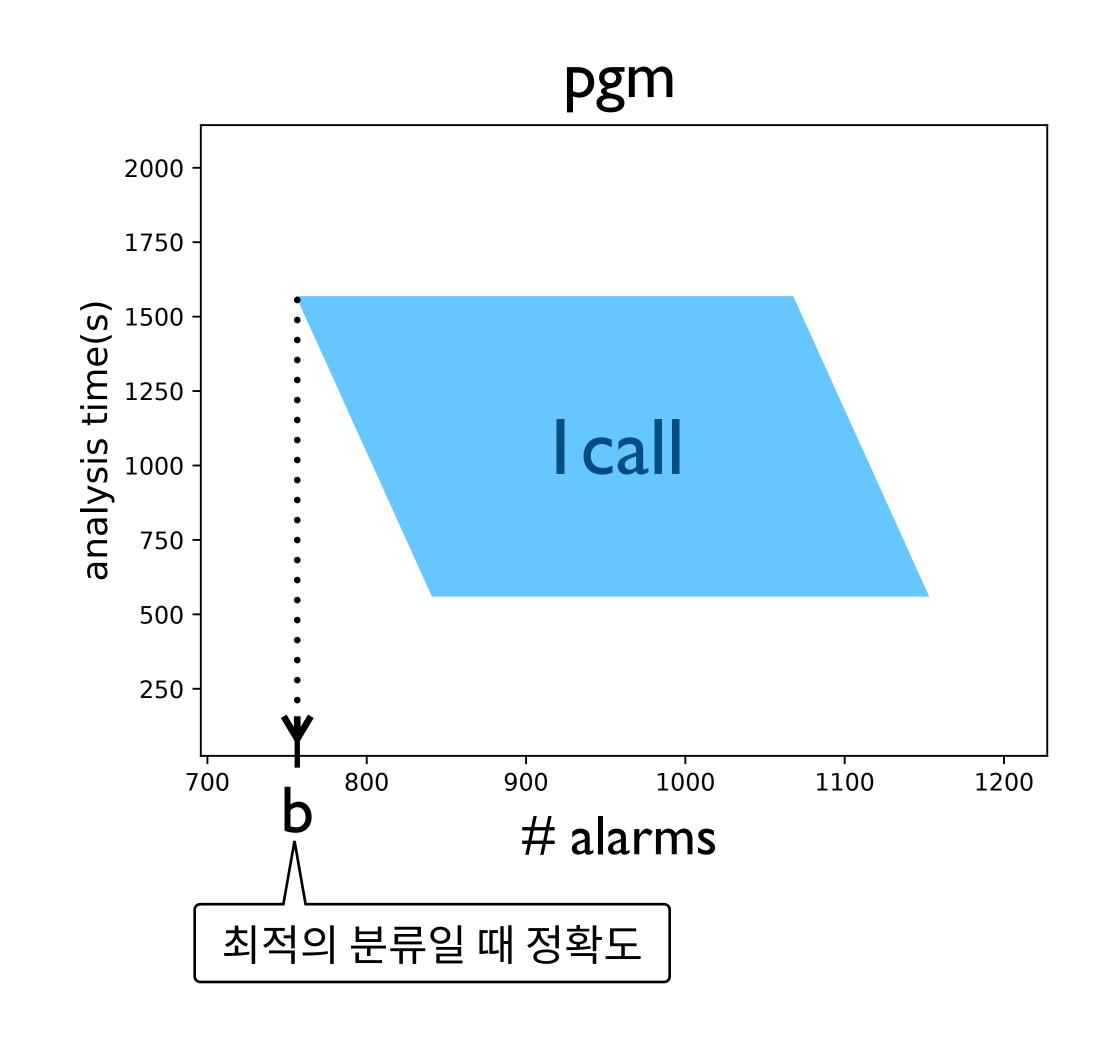
• 목표: 주요 k기반 요약 방식을 표준으로 만들기



- 효율적으로 최적의 주요 요소 분류를 찾아주는 알고리즘
- 쉽고 간단한 주요 요소 분류방법
- CFA의 Obj 대비 이론적 우수성 보이기
- 타 언어에서 주요 k기반 요약 방식의 효과성 보이기

후속 연구 1: 최적의 주요 요소 분류 찾기 알고리즘





후속 연구 2: 쉽고 간단한 주요 요소 분류 방법

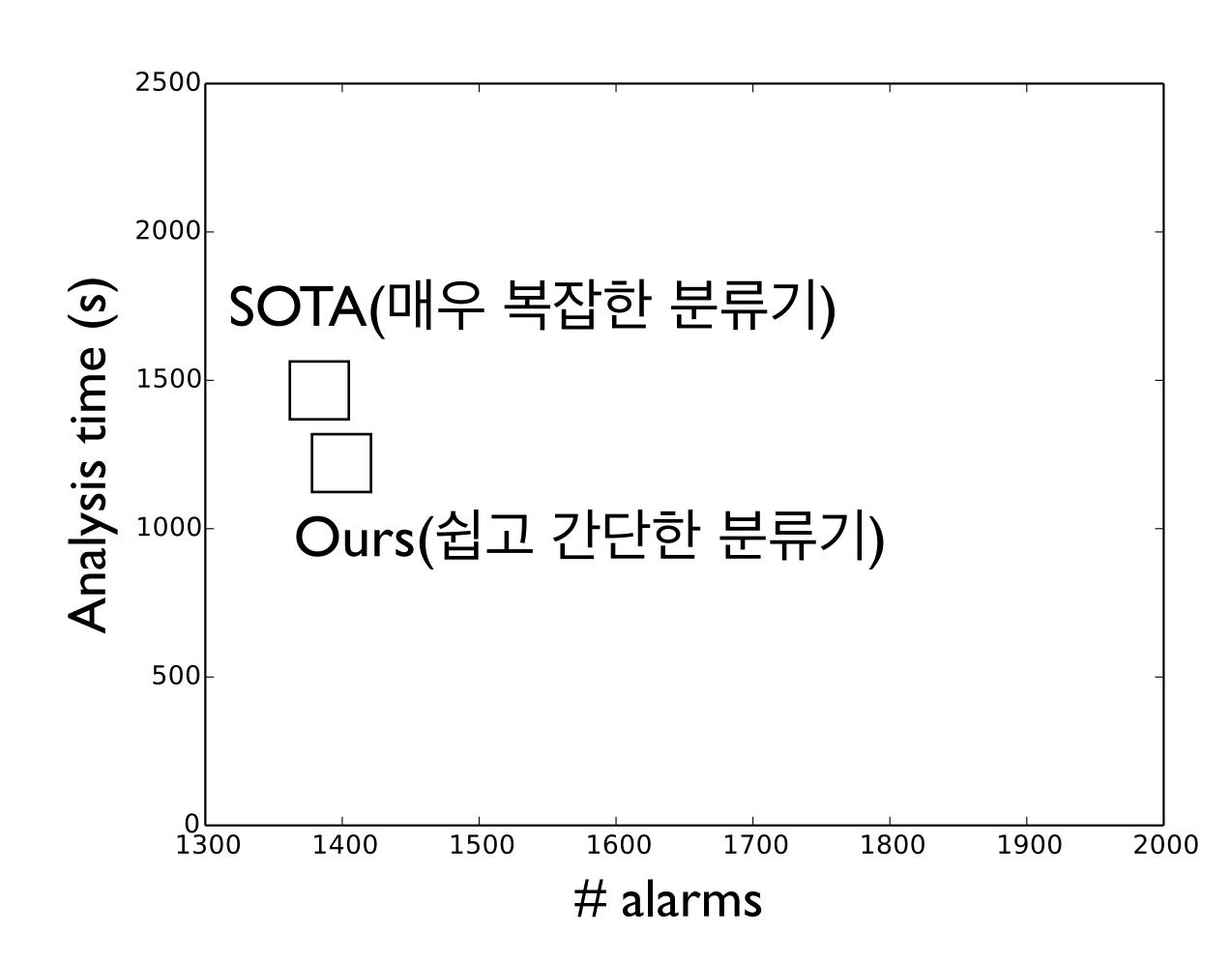
classifier(e):

if (<u>??</u> (쉽고 간단한 조건)):

return true //주요 요소임

else:

return false //부수적 요소임



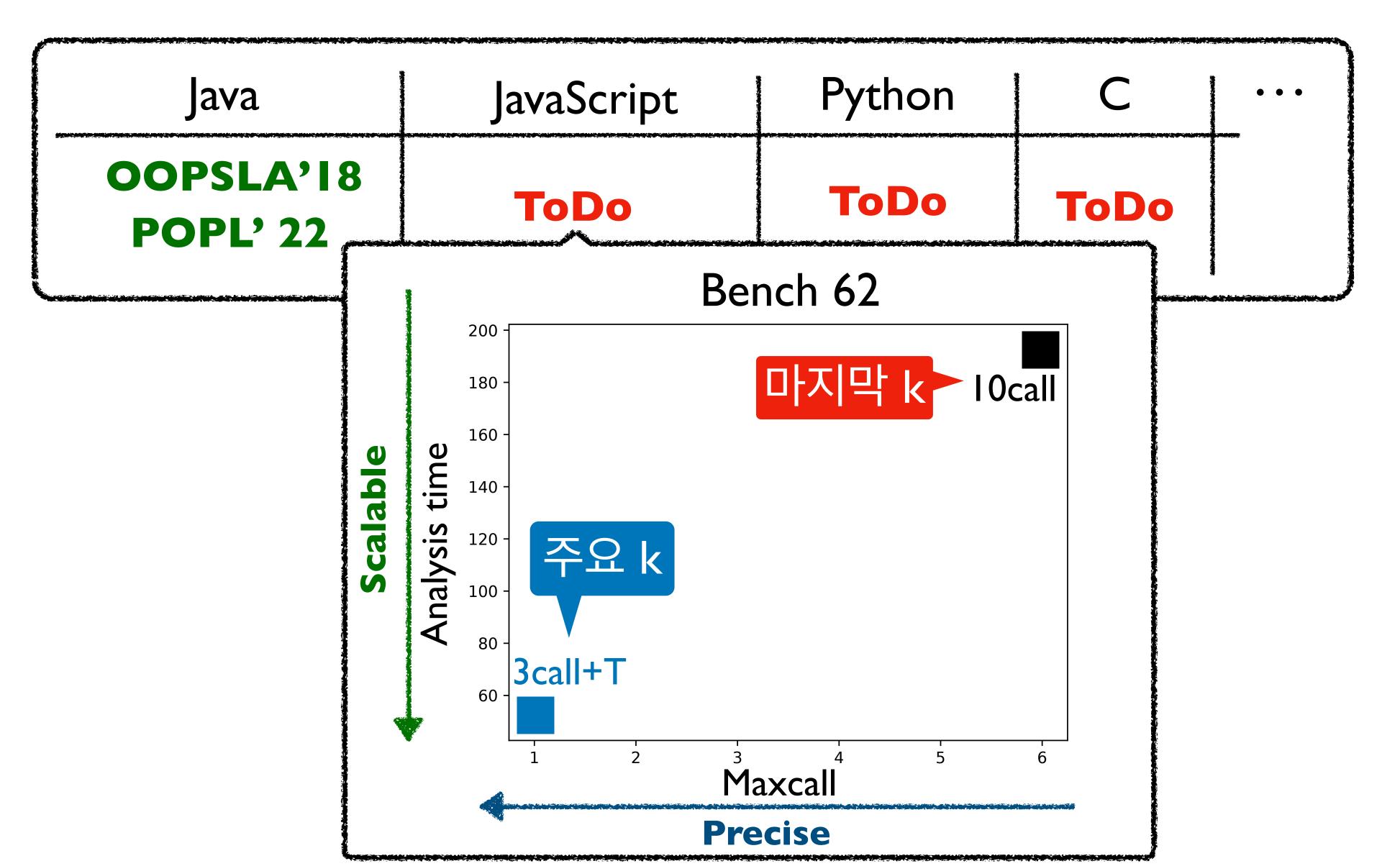
후속 연구 3: CFA의 Obj 대비 우수성을 이론적으로 보이기

임의의 프로그램과 k-obj가 내놓은 분석 결과에 대하여, 더 정확한 분석 결과를 내놓는 k-CFA가 항상 존재하는가?

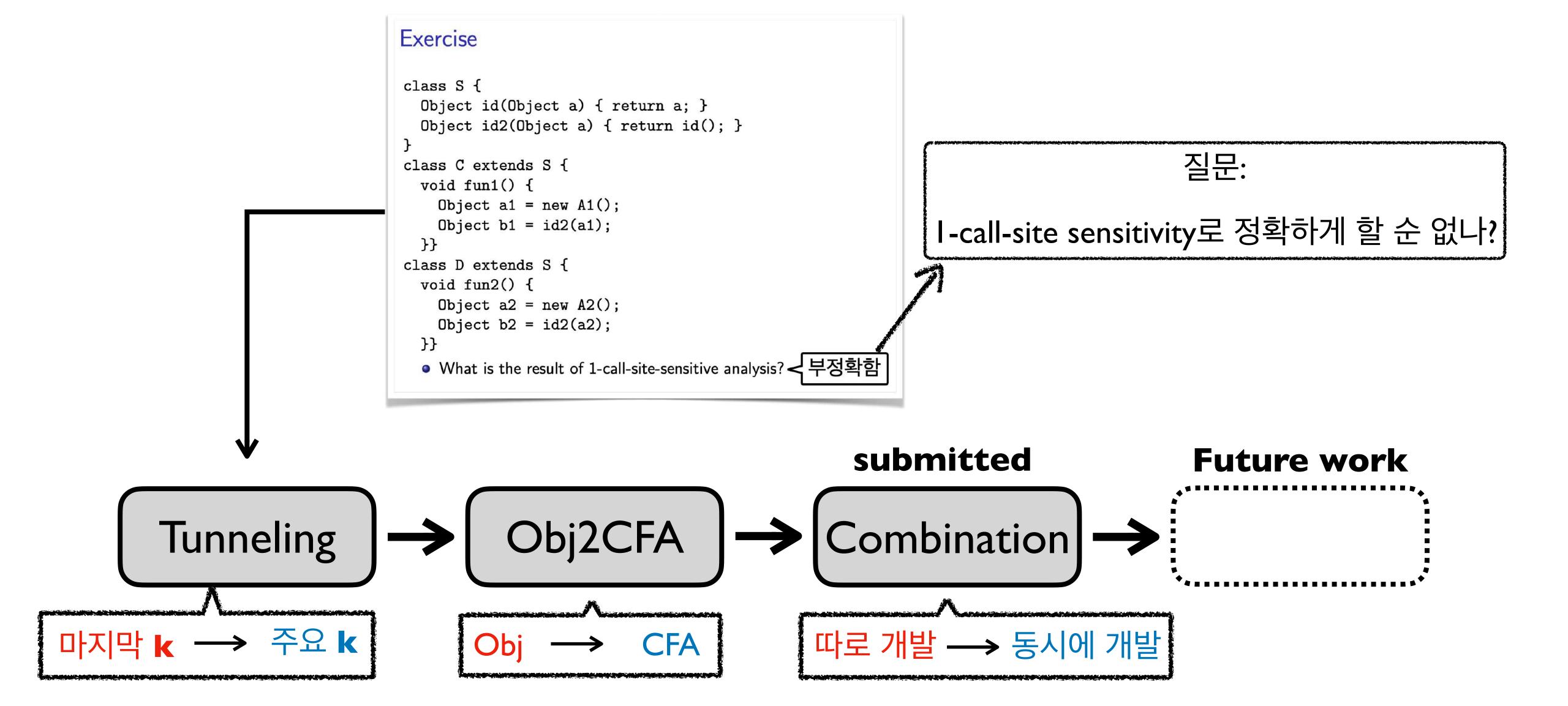
Definition 7.1 (Superiority of Call-Site Sensitivity). Let \mathbb{P} be a set of target programs. Let \mathbb{S} be a context-tunneling space for the target programs. We say call-site sensitivity is superior to object sensitivity with respect to \mathbb{S} if is always possible to simulate object sensitivity via call-site sensitivity:

 $\forall P \in \mathbb{P}. \forall T_{obj} \in \mathbb{S}. \exists T_{call} \in \mathbb{S}. \forall k \in [0, \infty]. \ fixF_{P,k}^{T_{call}, U_{call}} \geq \text{ (more precise than)} \ fixF_{P,k}^{T_{obj}, U_{obj}}$ (5)

후속 연구 4: 타 언어에 적용하기

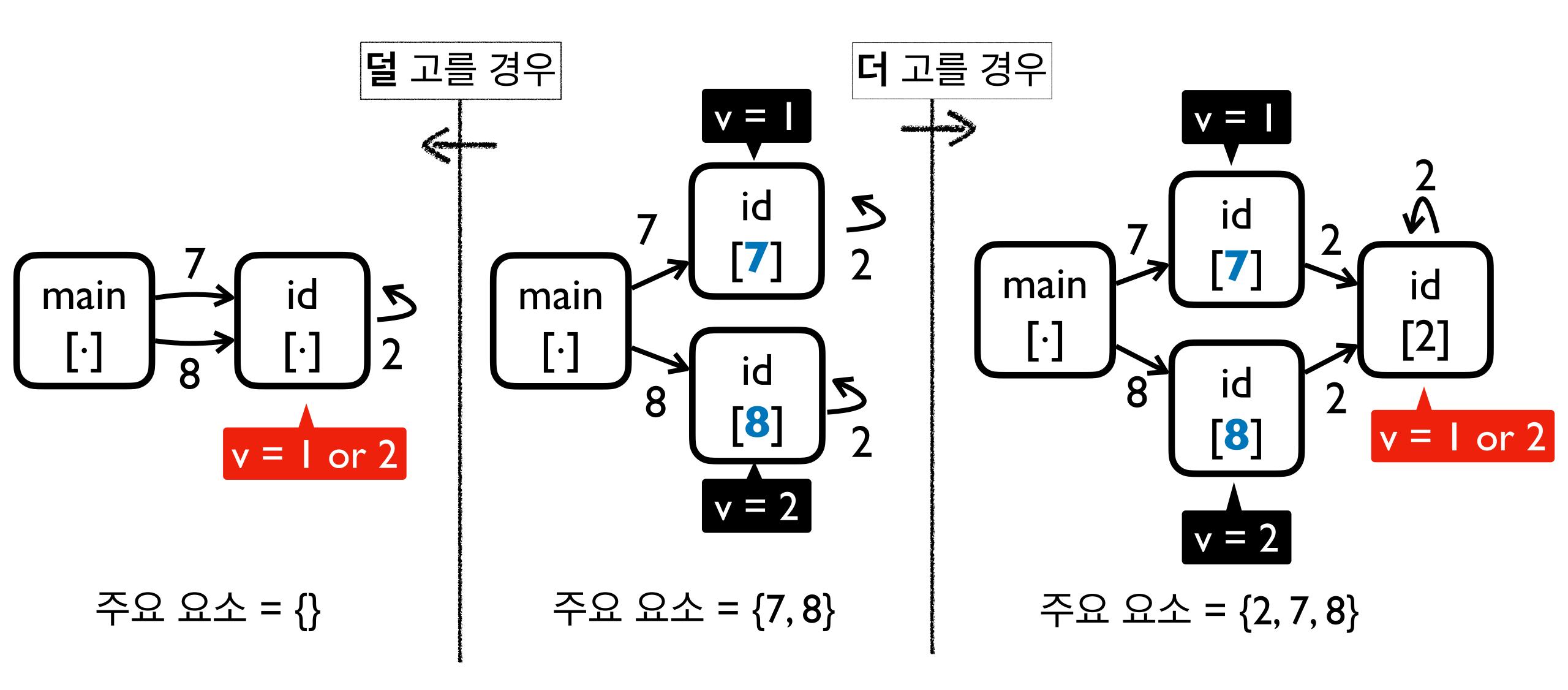


마무리: 고정관념에 도전하기

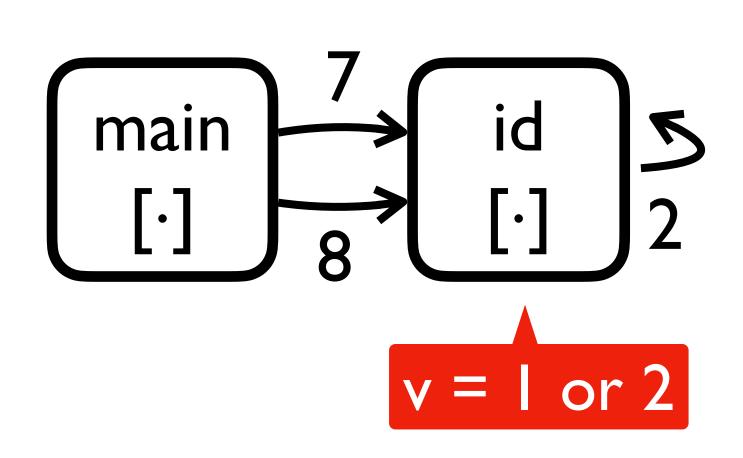


Back up

• 주요 I-요소 기반 함수 호출 요약

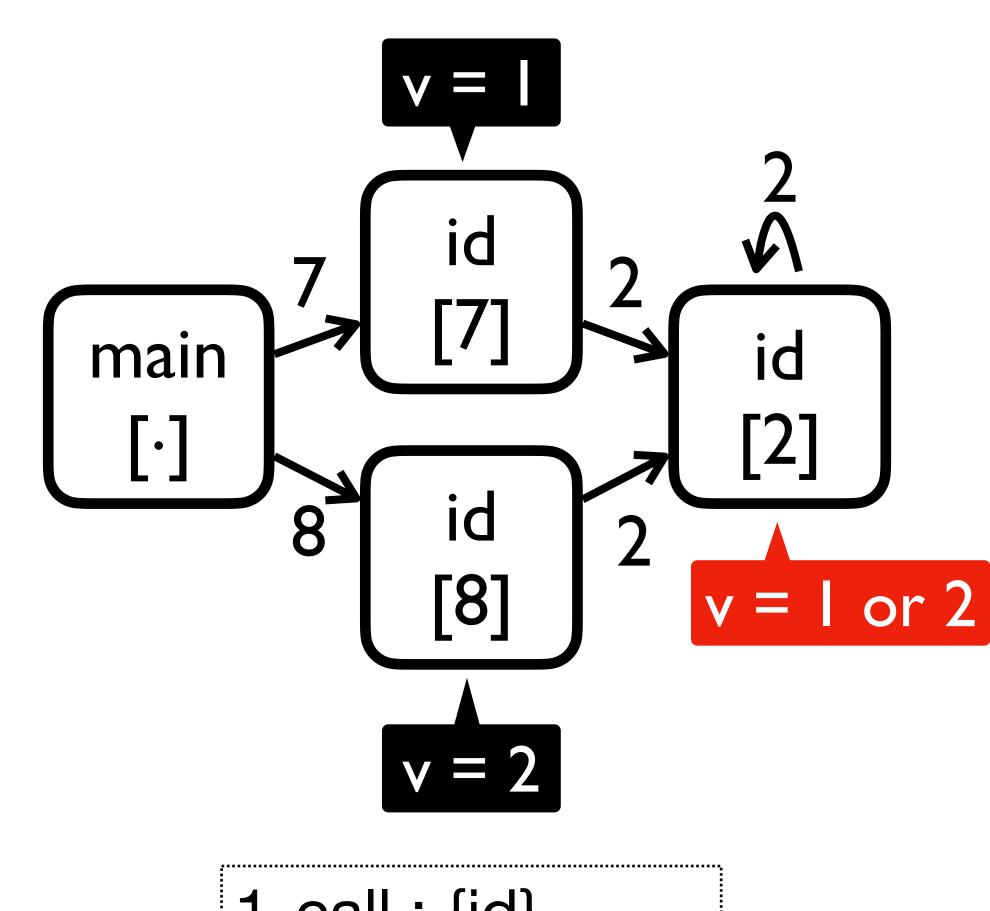


• 선택적 1-요소 기반 함수 호출 요약



1-call : {}

0-call: {main, id}



1-call : {id}

0-call: {main}

주요 요소 = {7,8}

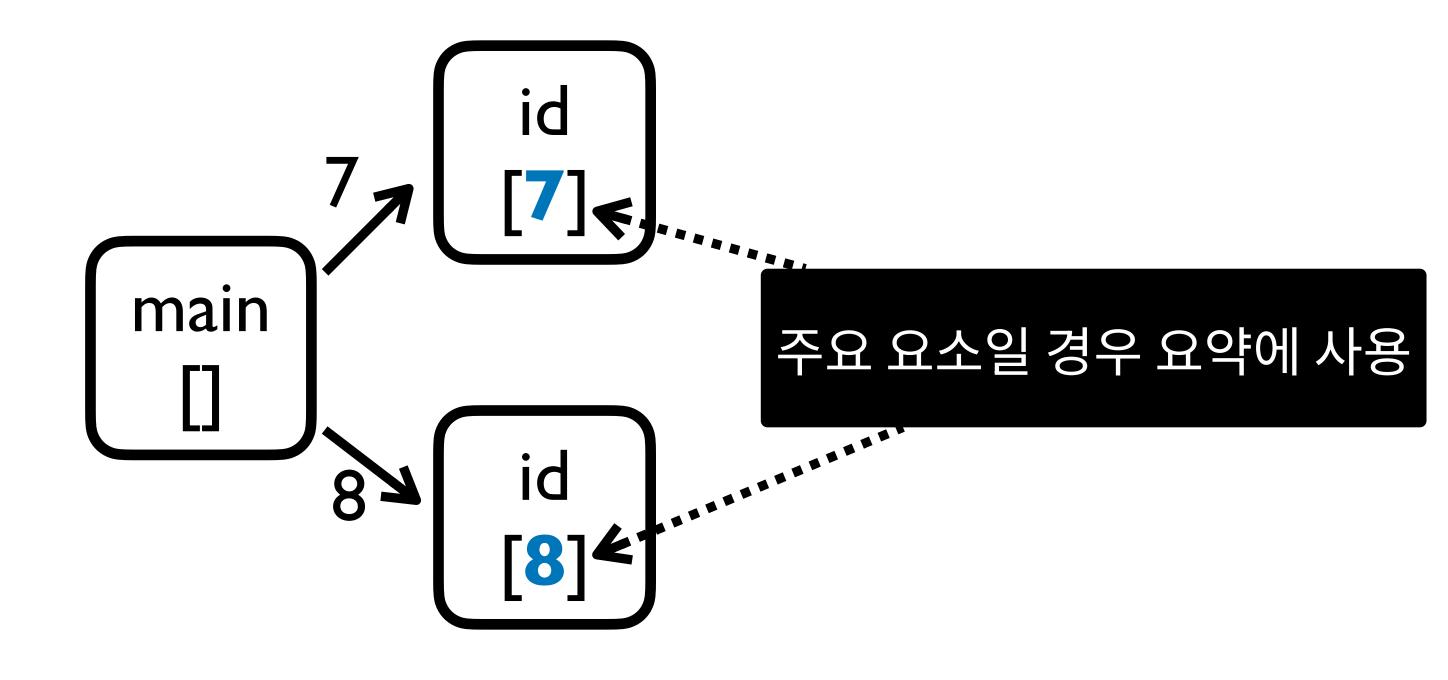
```
0: id(v, i){
I: if (i > 0)
   return id(v, i-1);}
    return v;}
4:
5: main(){
6: i = input();
7: vI = id(I, i);
   v2 = id(2, i);
8:
9: assert (vI != v2);//query
```

```
주요 요소인지 확인
 7 \in \{7,8\}??
         main
                        id
주요 요소인지 확인
  8 \in \{7,8\}??
```

예제 프로그램

주요 요소 = {7,8}

```
0: id(v, i){
I: if (i > 0)
   return id(v, i-1);}
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5: main(){
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7: vI = id(I, i);
   v2 = id(2, i);
8:
9: assert (vl != v2);//query
   예제 프로그램
```



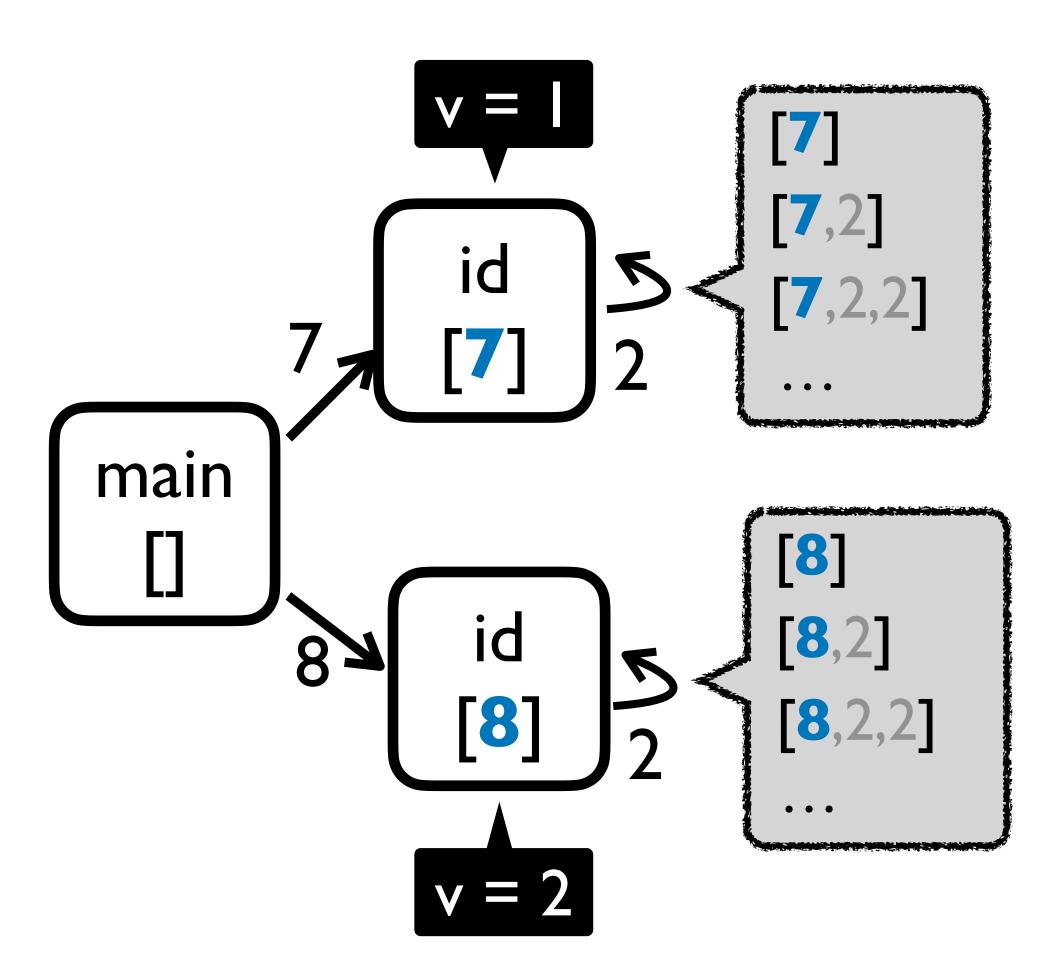
```
0: id(v, i){
I: if (i > 0)
    return id(v, i-1);}
   return v;}
5: main(){
6: i = input();
7: vI = id(I, i);
8: v2 = id(2, i);
9: assert (vI != v2);//query
```

```
주요 요소 = {7,8}
                    주요 요소인지 확인
                      2 \in \{7,8\}??
main
```

```
0: id(v, i){
                                             주요 요소 = {7,8}
1: if (i > 0)
    return id(v, i-1);}
   return v;}
5: main(){
                                 main
                                                                     주요 요소가 아닐 경우
6: i = input();
                                                                         요약에 사용 X
7: vI = id(I, i);
8: v2 = id(2, i);
9: assert (vI != v2);//query
```

예제 프로그램

```
0: id(v, i){
  if (i > 0){
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4:
5: main(){
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   v2 = id(2, i);
8:
    assert (vI != v2);//query
9:
   예제 프로그램
```



I개 주요 요소 기반 함수 호출 요약 (주요 요소 = {7,8})