람다 계산법에 관한 퍼즐

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재미 삼아 람다 계산법에 관한 다음의 문제를 풀어 보세요. 해답은 다음에 알려 드리겠습니다.

- 1. Find a term M such that M M $\rightarrow *$ z. $\lambda x.z$ is an obvious solution. Is there a solution in which the z on the right descends from a free occurrence of z in the second occurrence of M?
- 2. Given any n >= 2, and any i in 2 ... n, find a context C[] such that $C[z_1] \ C[z_2] \ ... \ C[z_n] \ \to * \ z_i$

The extra condition is that C[] is closed. For i=1 it is trivially solvable by $C[x] = \lambda x_2...x_n.x$. Find a non-trivial case.

3. For any given lambda expression G, find a lambda expression F satisfying

$$F \times (F y) \rightarrow * G \times y$$

4. More generally, given any $n \ge 1$ and a lambda expression G, find a lambda expression F such that

$$(F z_1) \dots (F z_n) \rightarrow * G z_1 \dots z_n$$

The problem 3 is the case of n=2.